

# CINC CÈNTIMS DE GEOMETRIA...

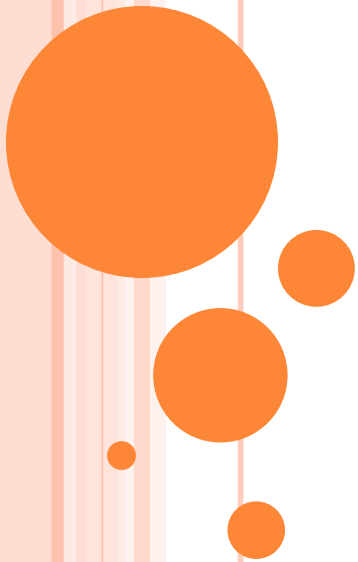
Lleida 4 de febrer del 2023

**CINC CÈNTIMS  
DE GEOMETRIA...  
I UN CÈNTIM  
D'ALTRES COSES**

Lleida 4 de febrer del 2023

**JOAN FOLGUERA FARRÉ**

**PROFESSOR JUBILAT**



# QUADRATS MÀGICS

15

|   |   |   |
|---|---|---|
| 8 | 1 | 6 |
| 3 | 5 | 7 |
| 4 | 9 | 2 |



# QUADRATS MÀGICS

15

|   |   |   |
|---|---|---|
| 8 | 1 | 6 |
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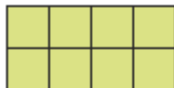

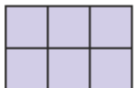

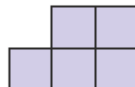


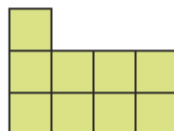

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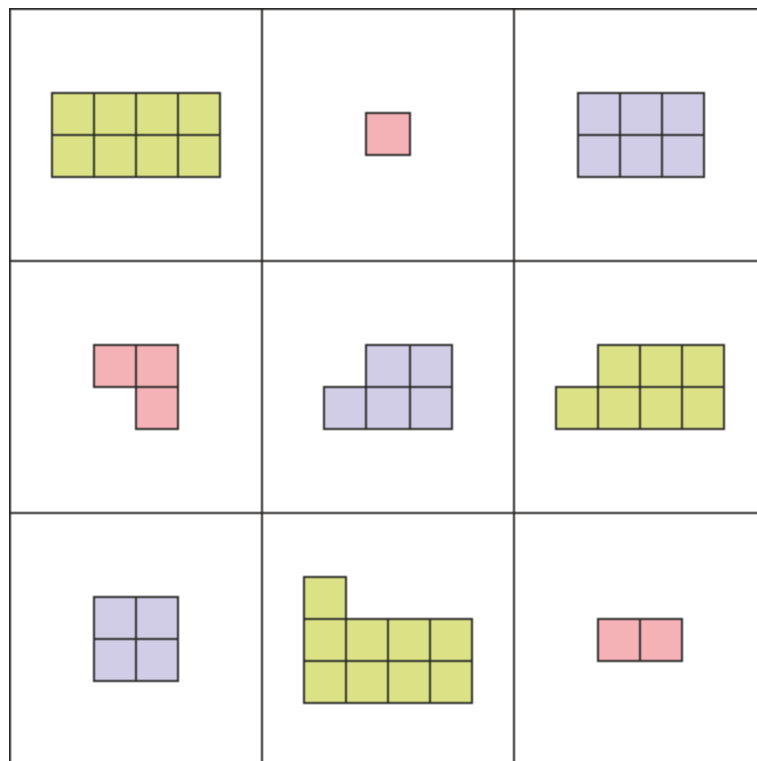
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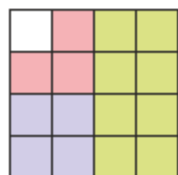
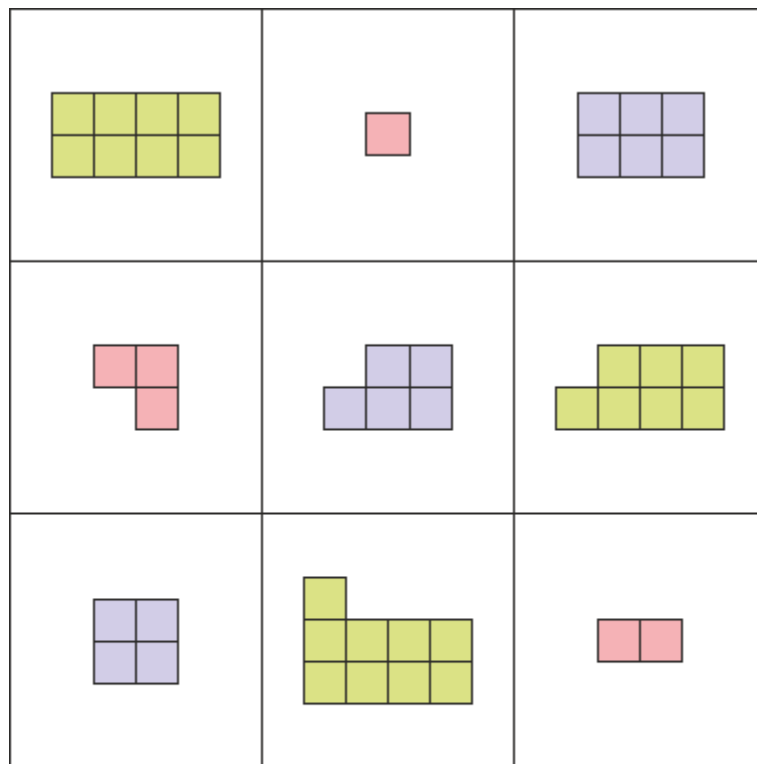
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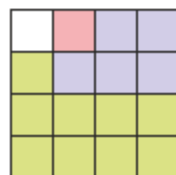
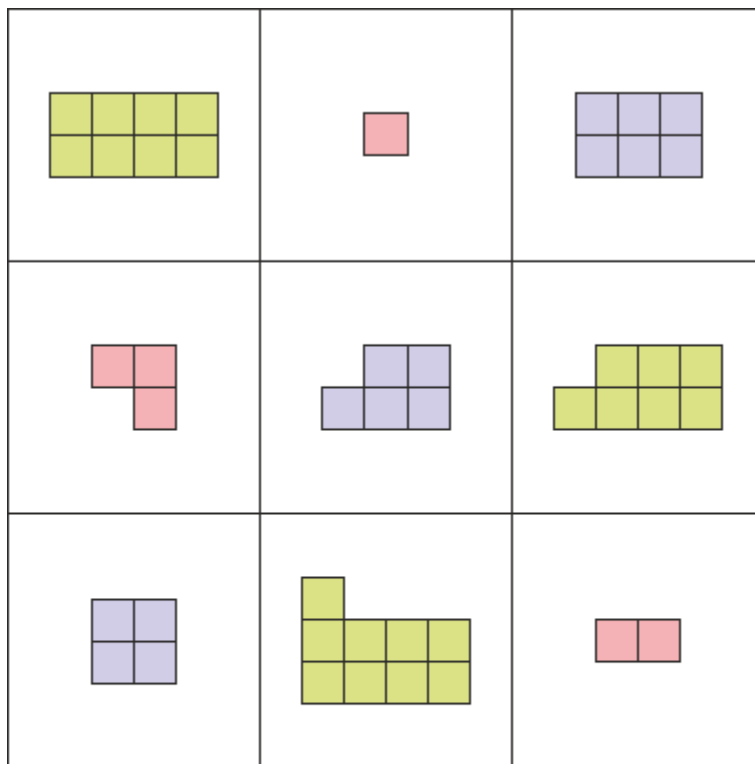
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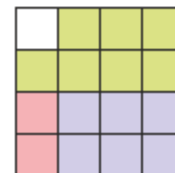
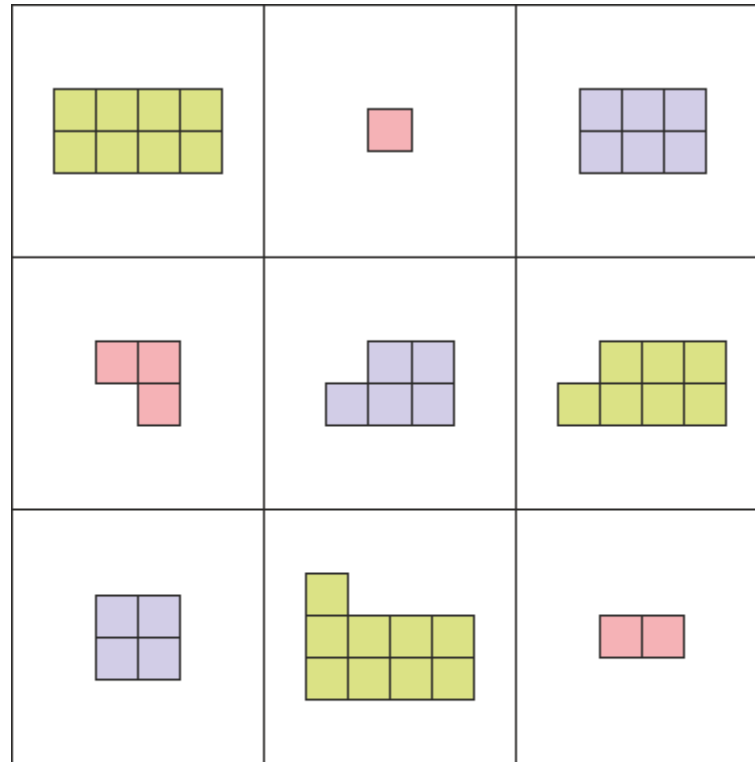
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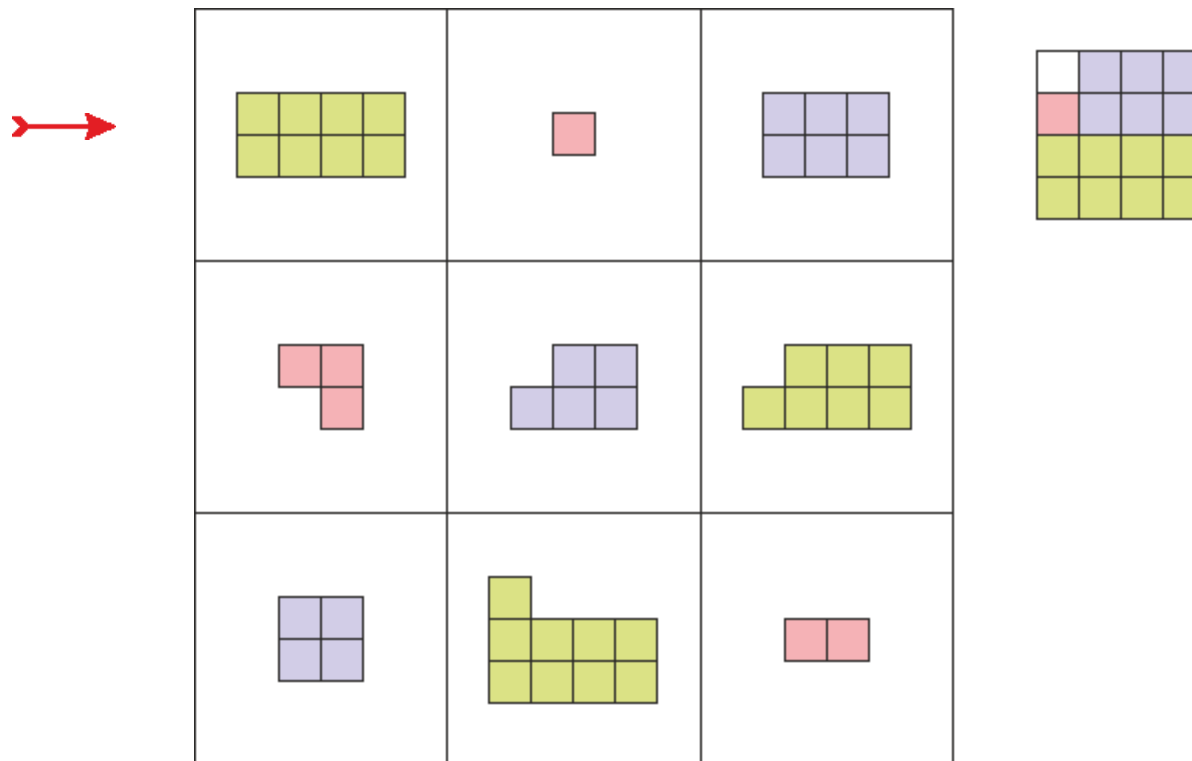
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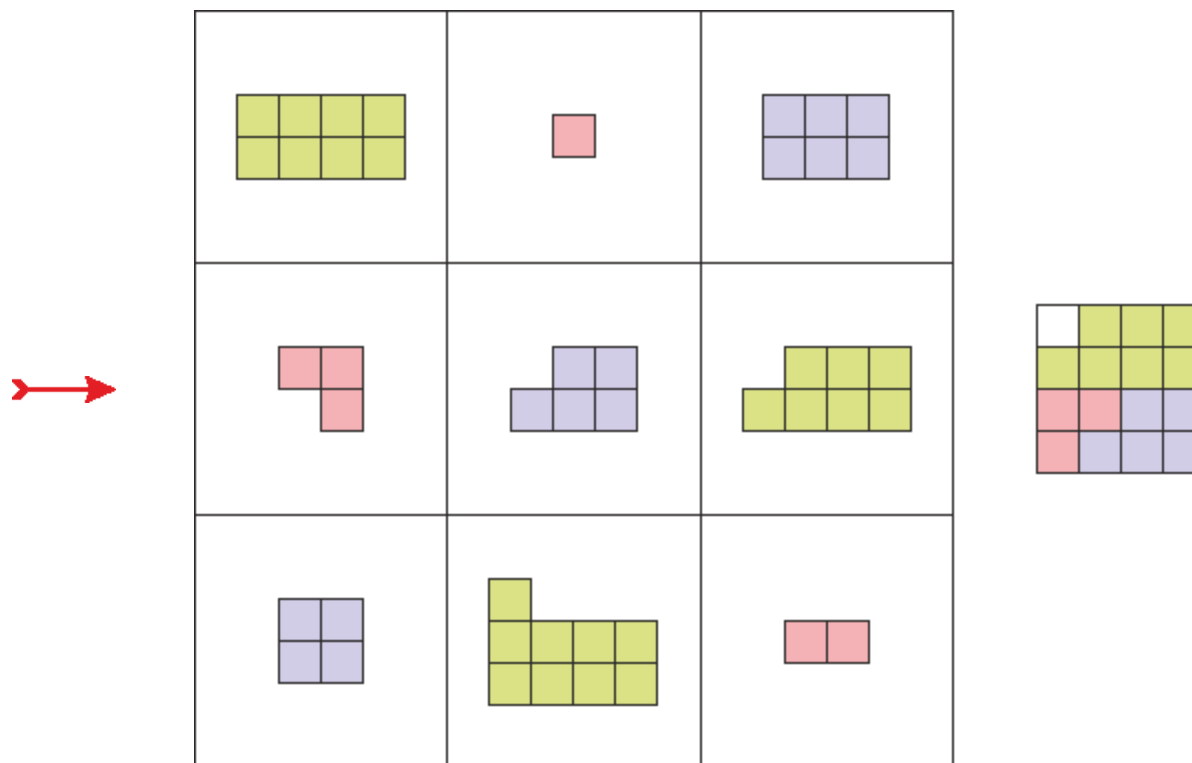
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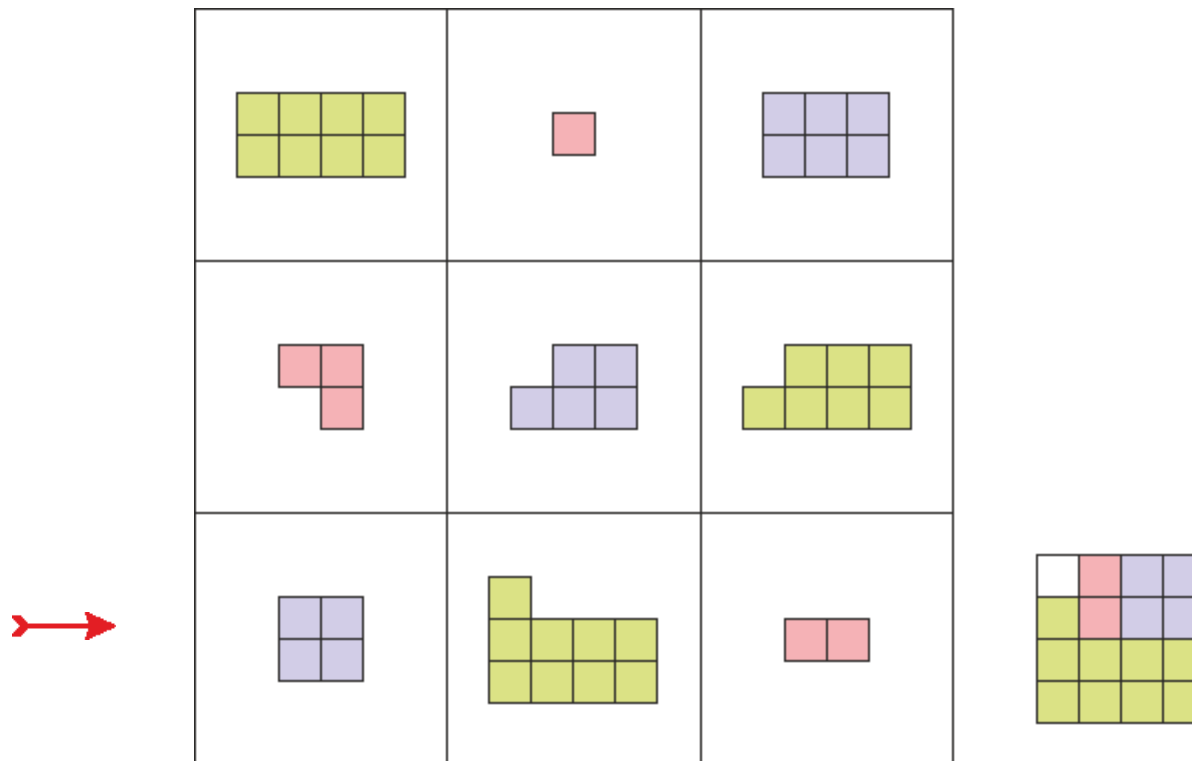
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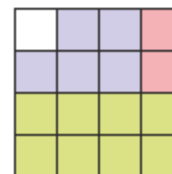
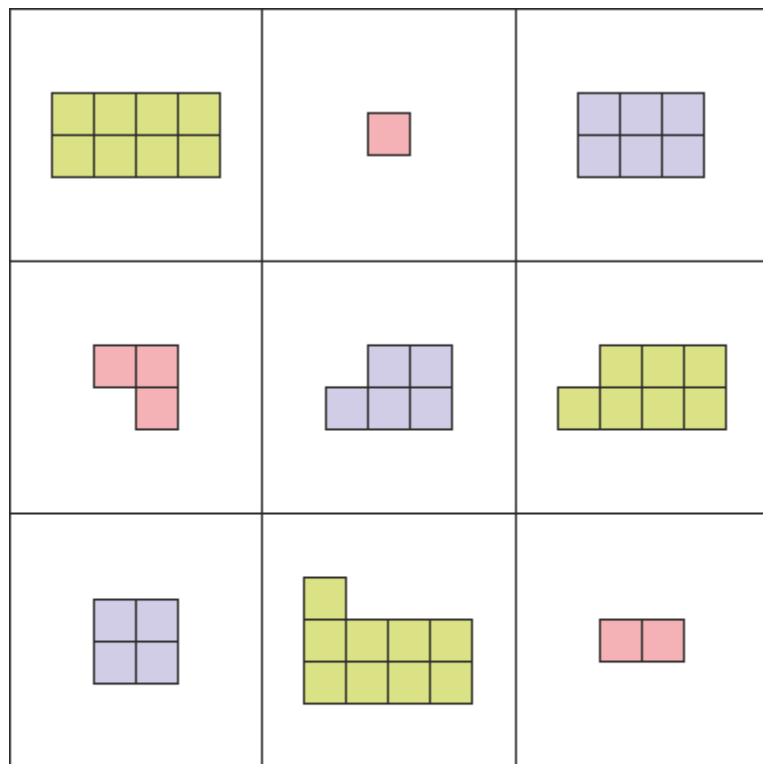


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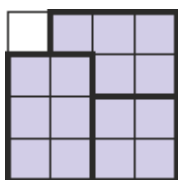
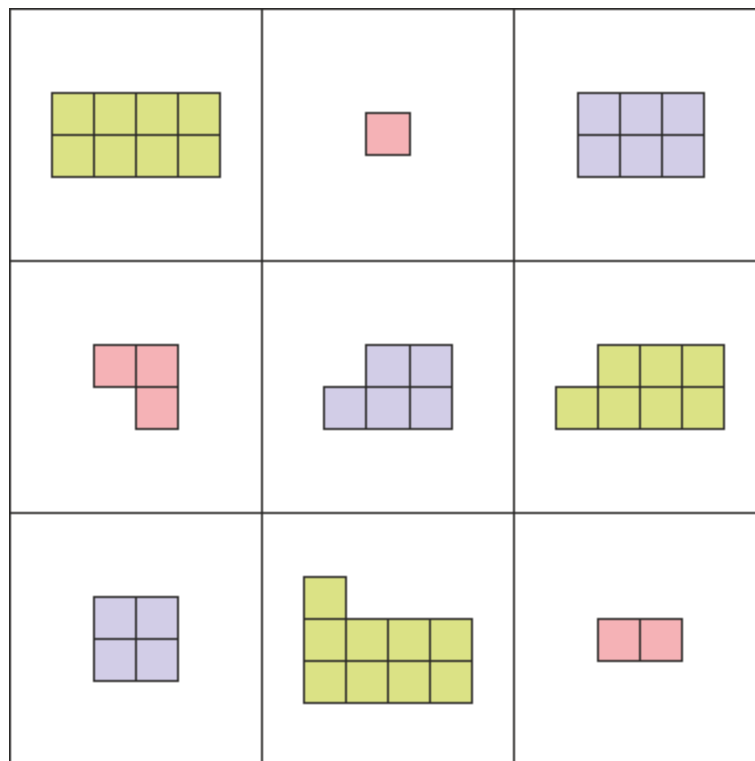




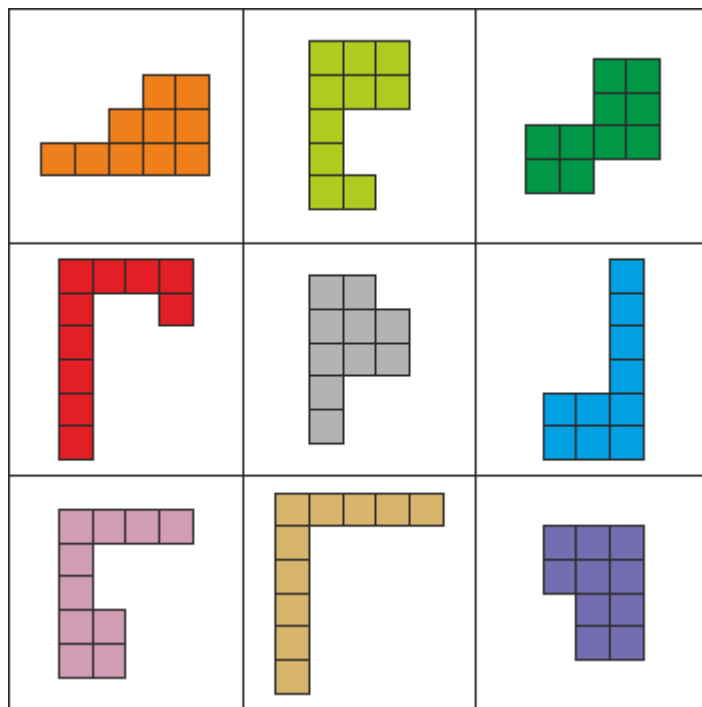
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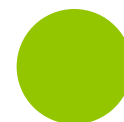
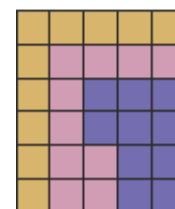
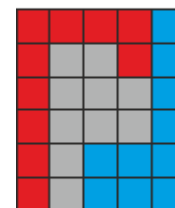
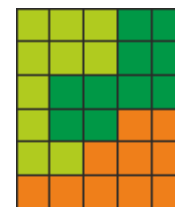
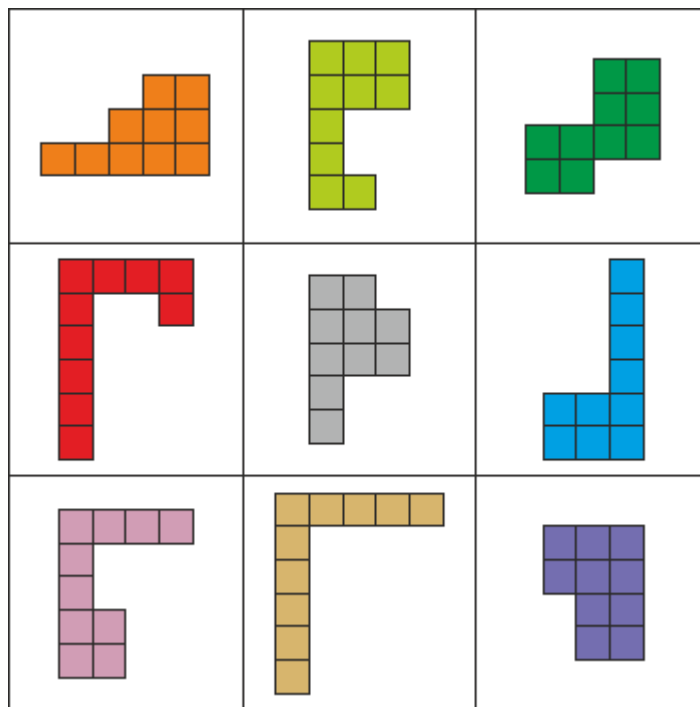
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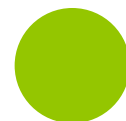
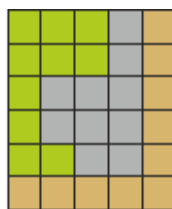
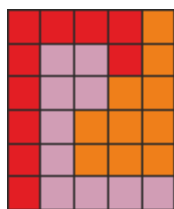
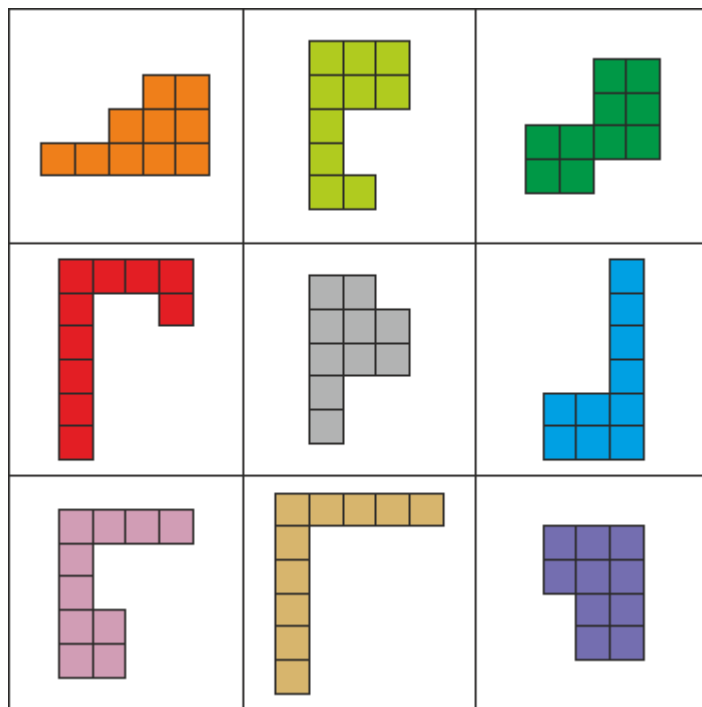
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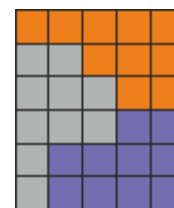
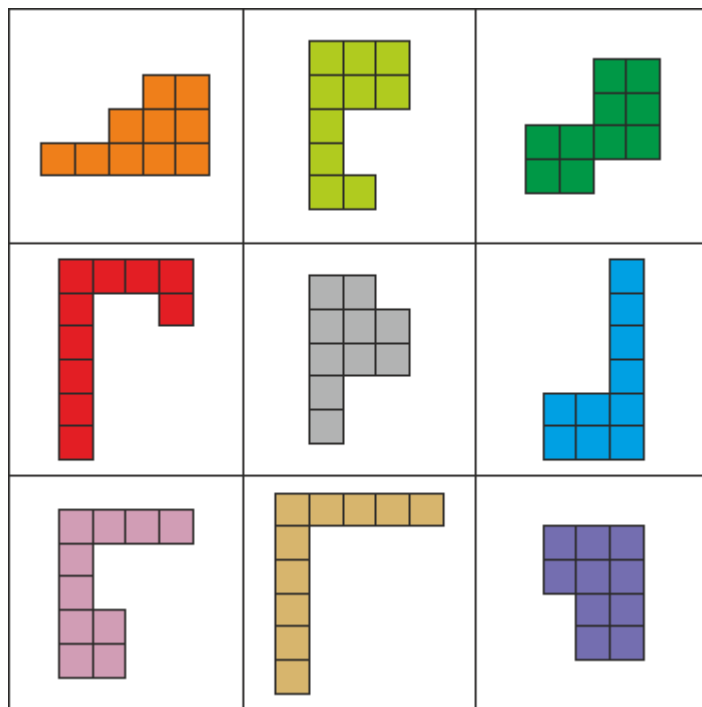
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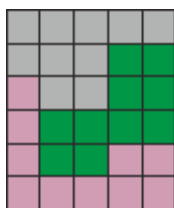
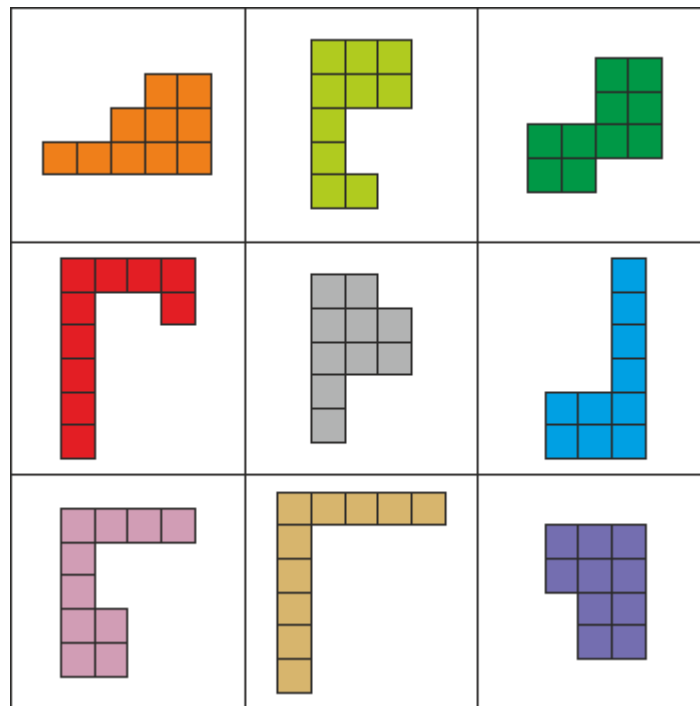
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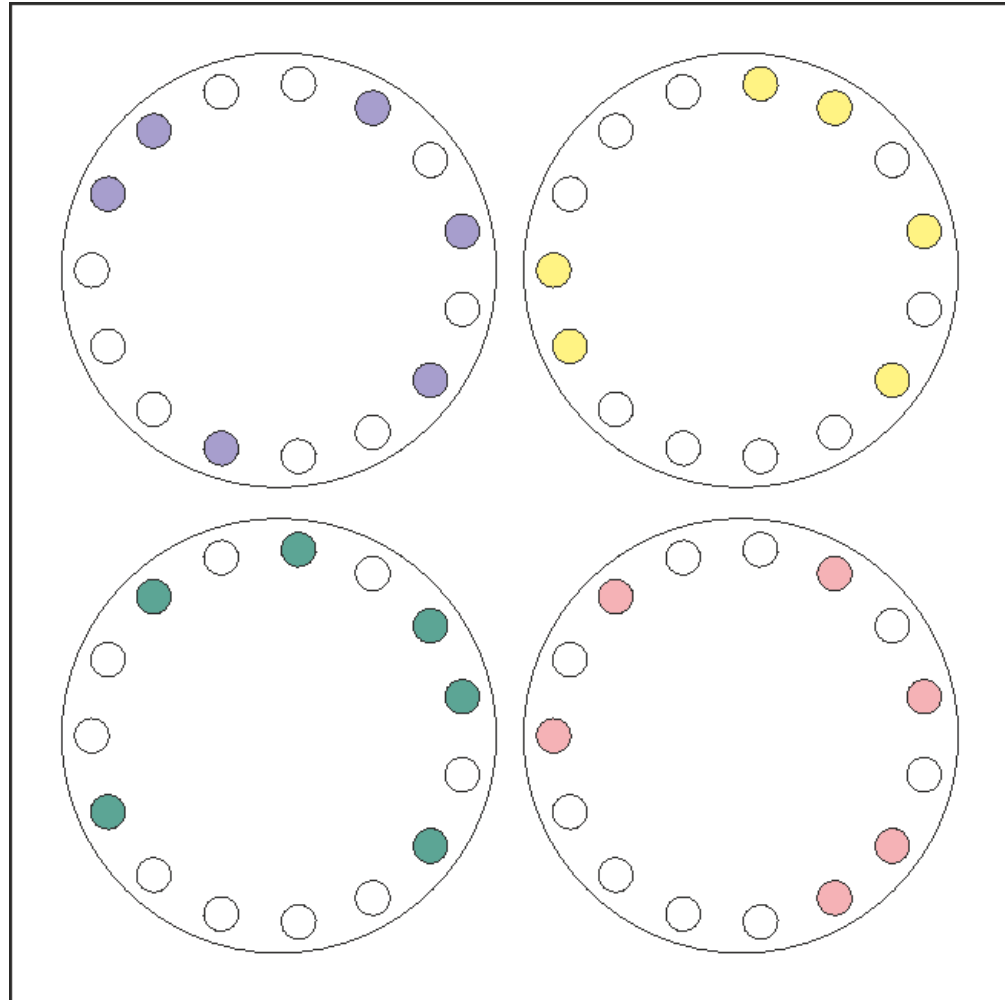
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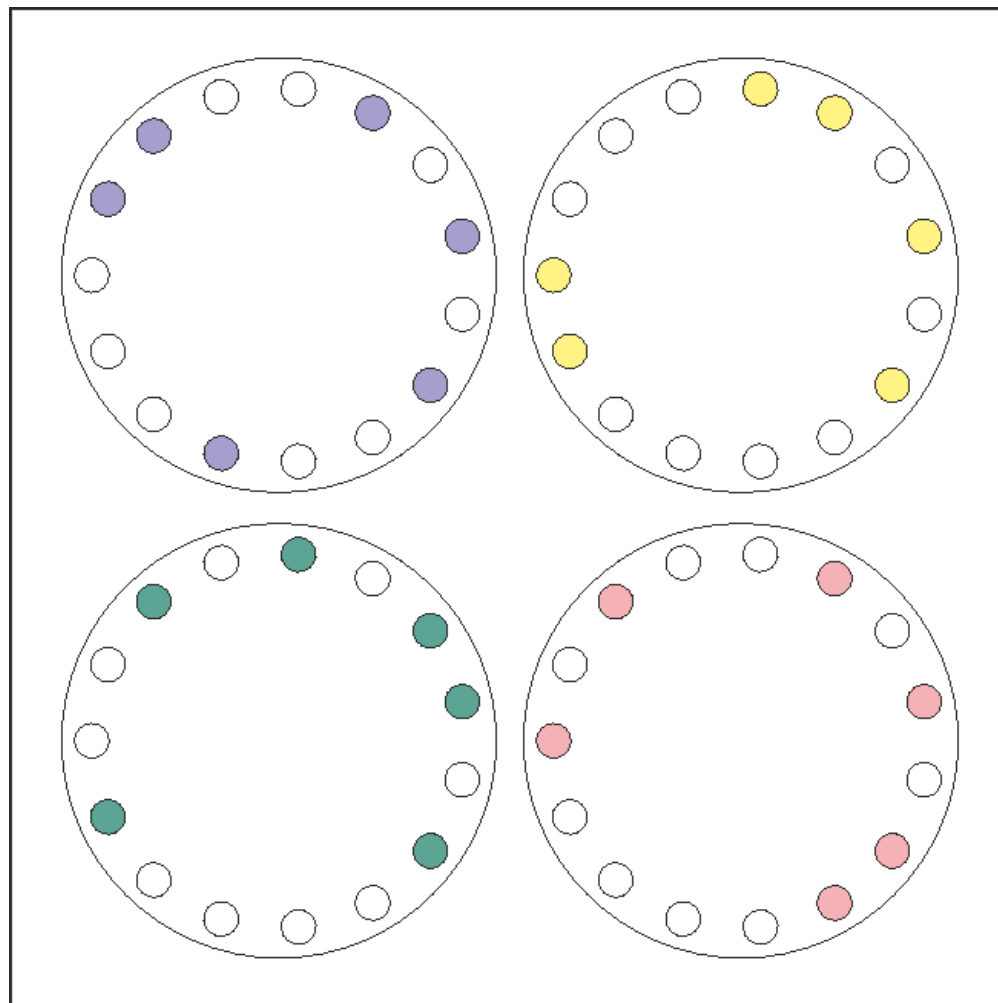
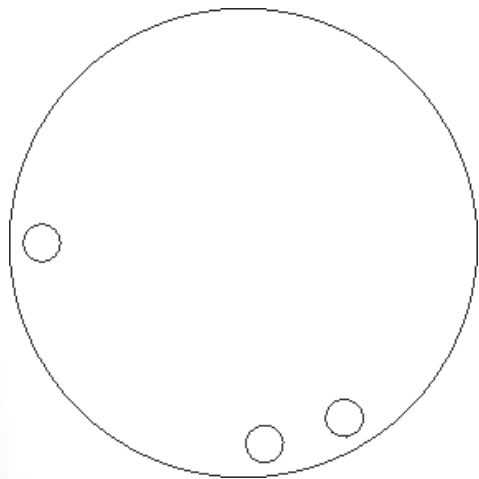


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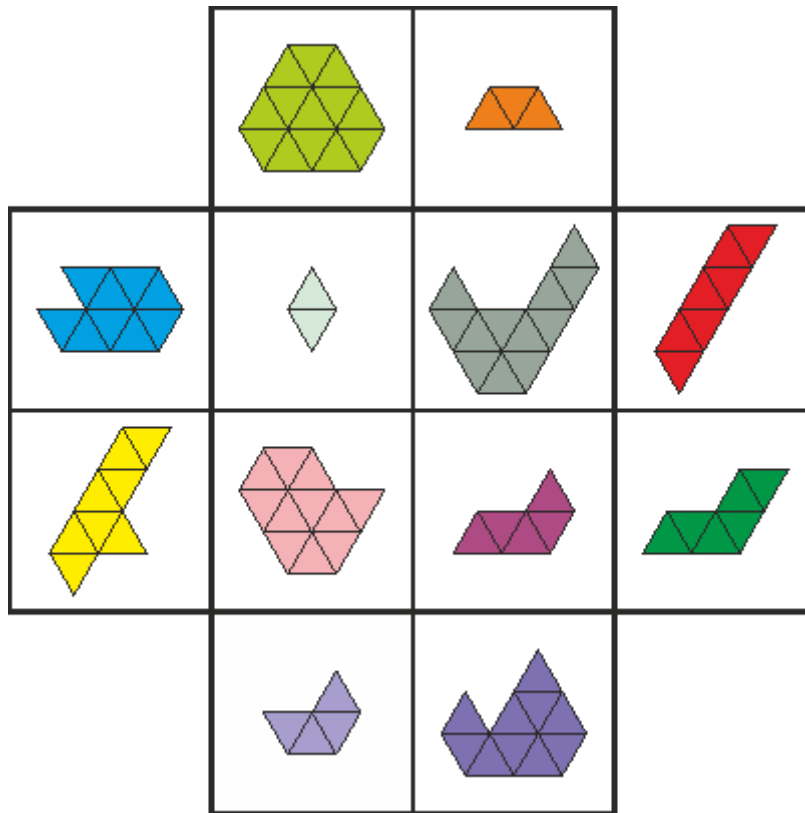




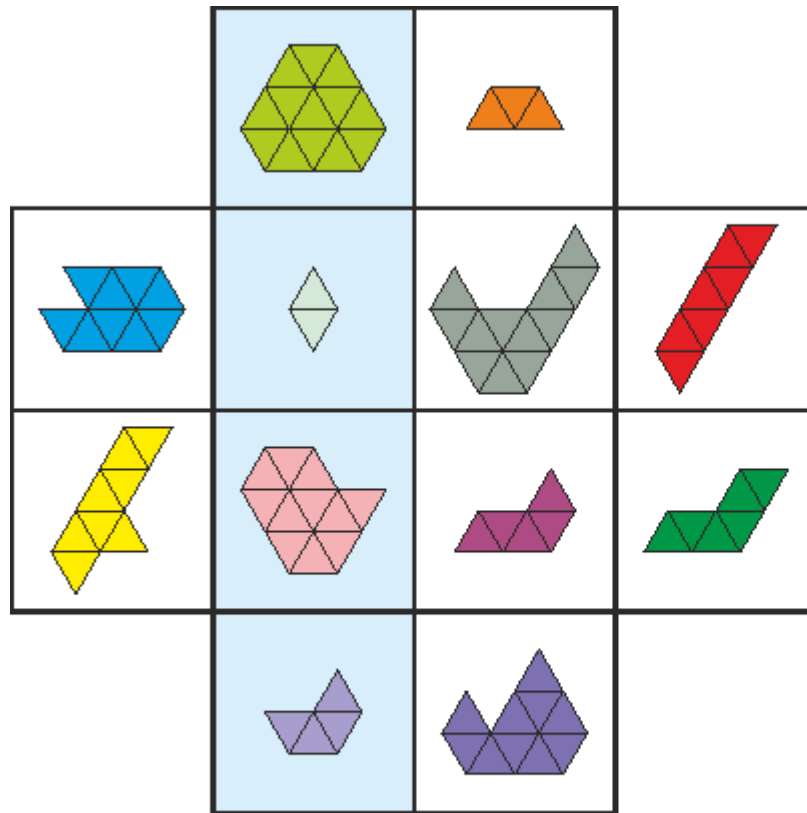
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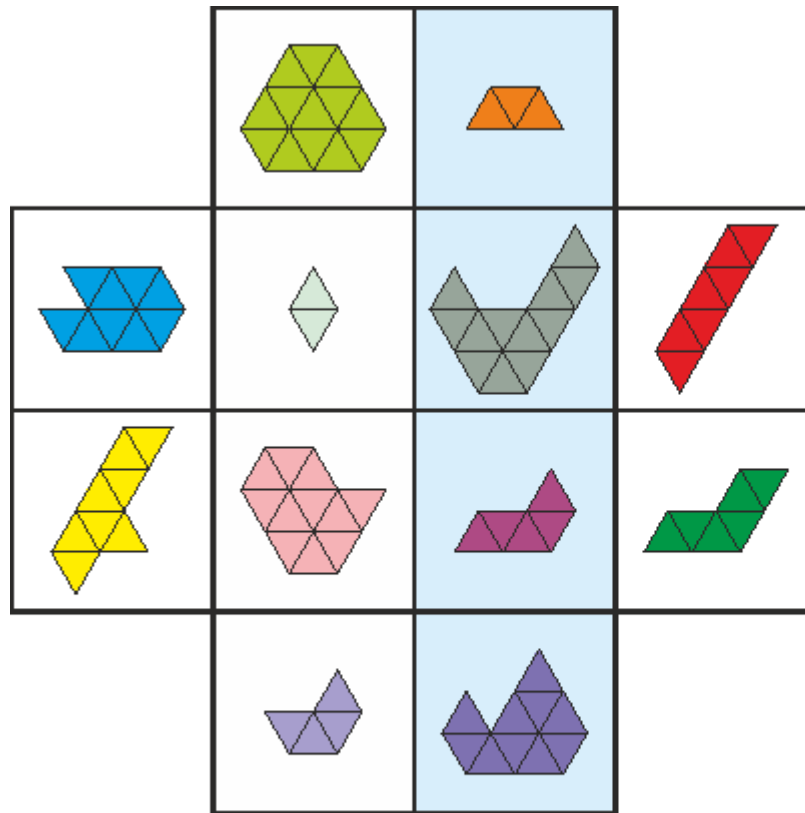
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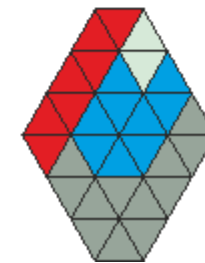
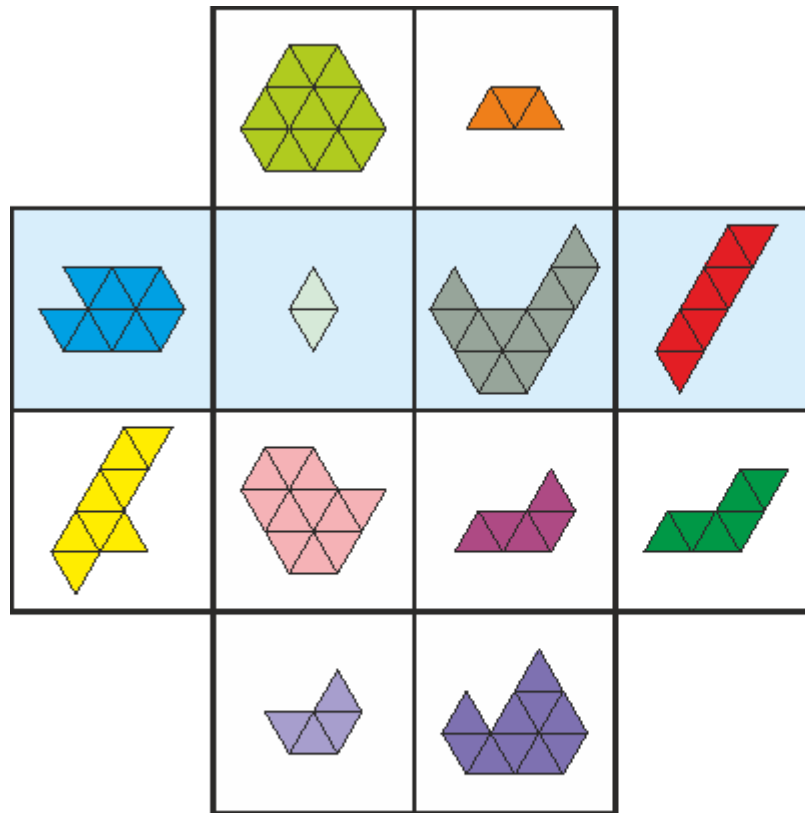
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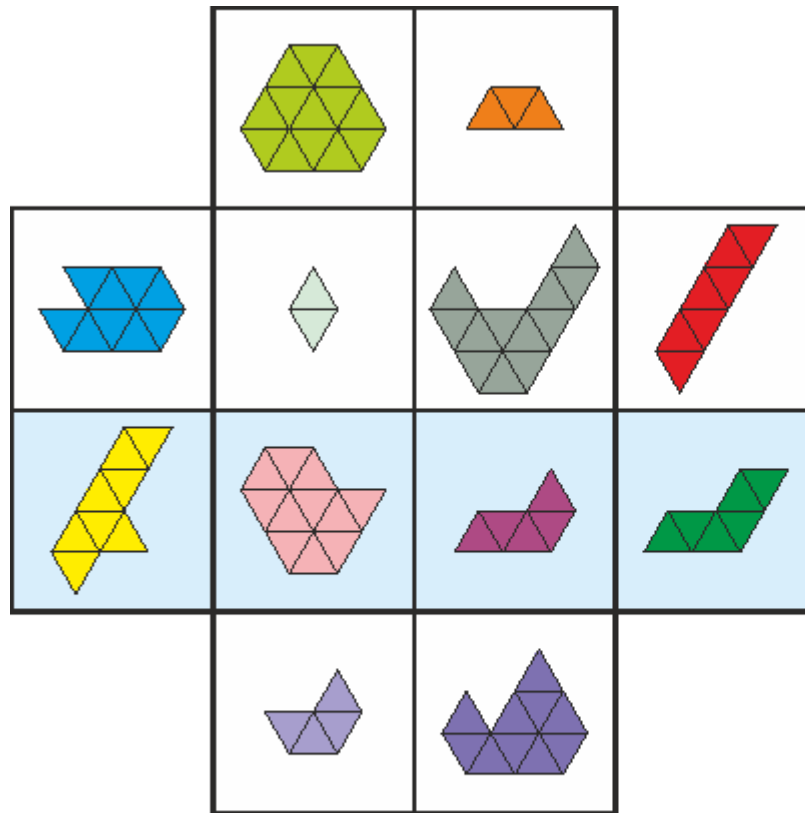
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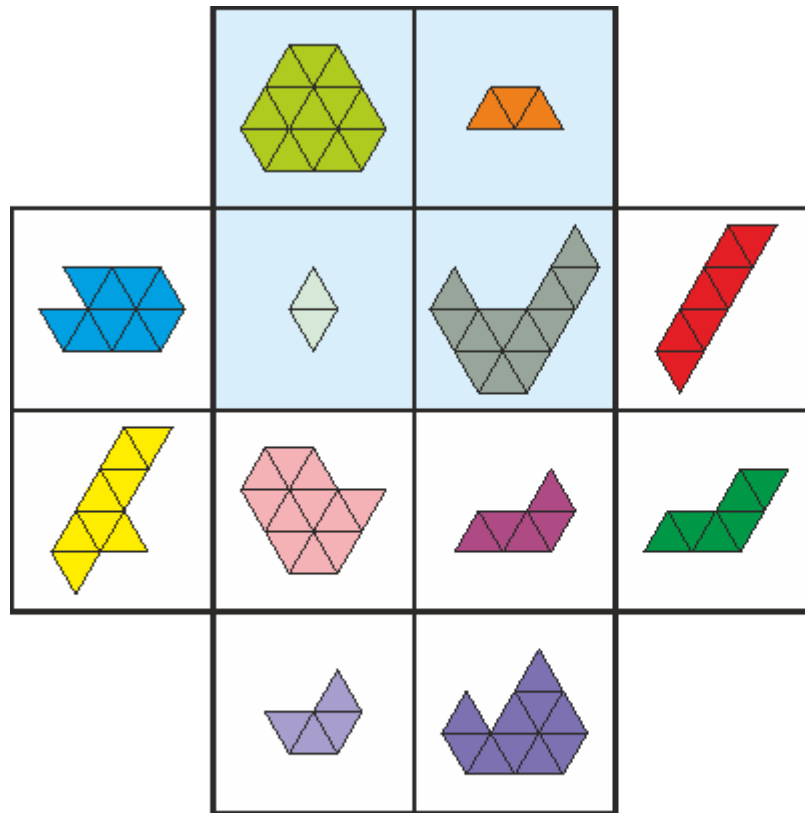
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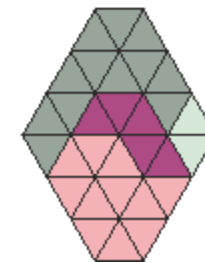
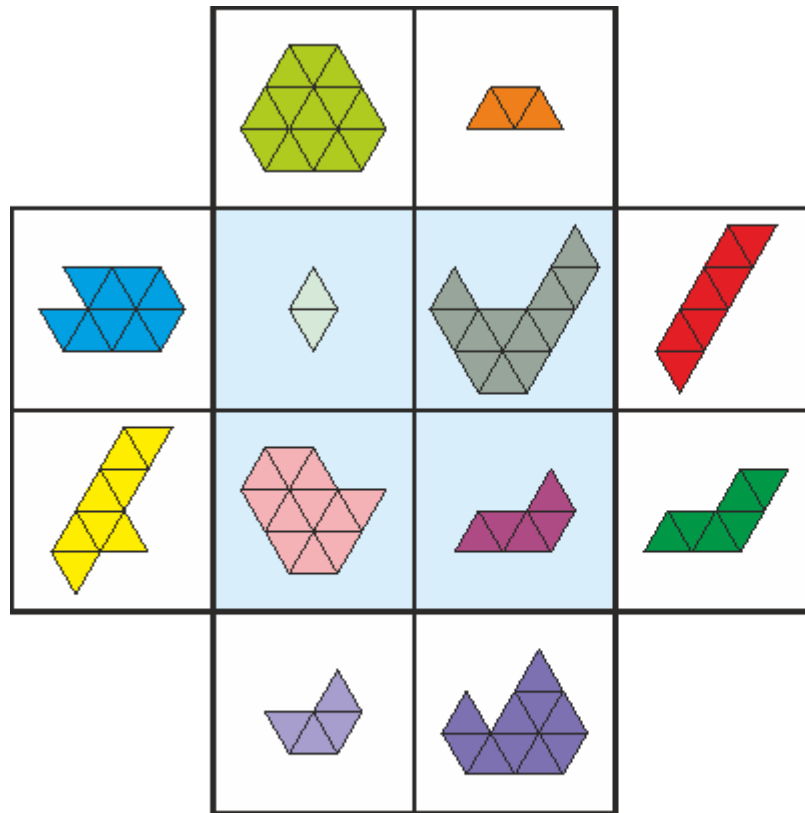
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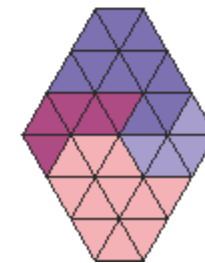
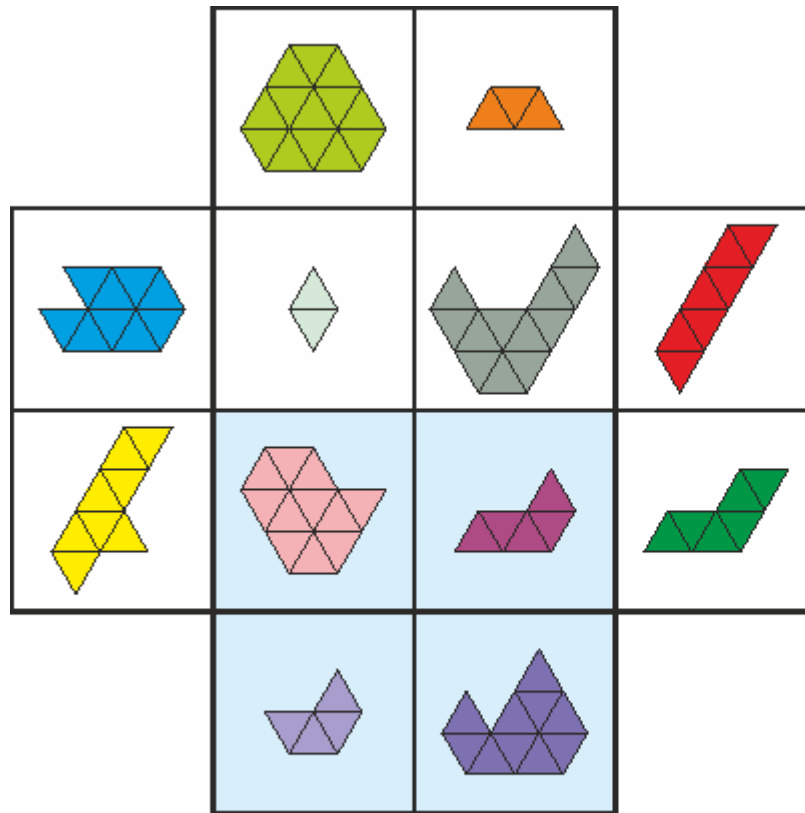


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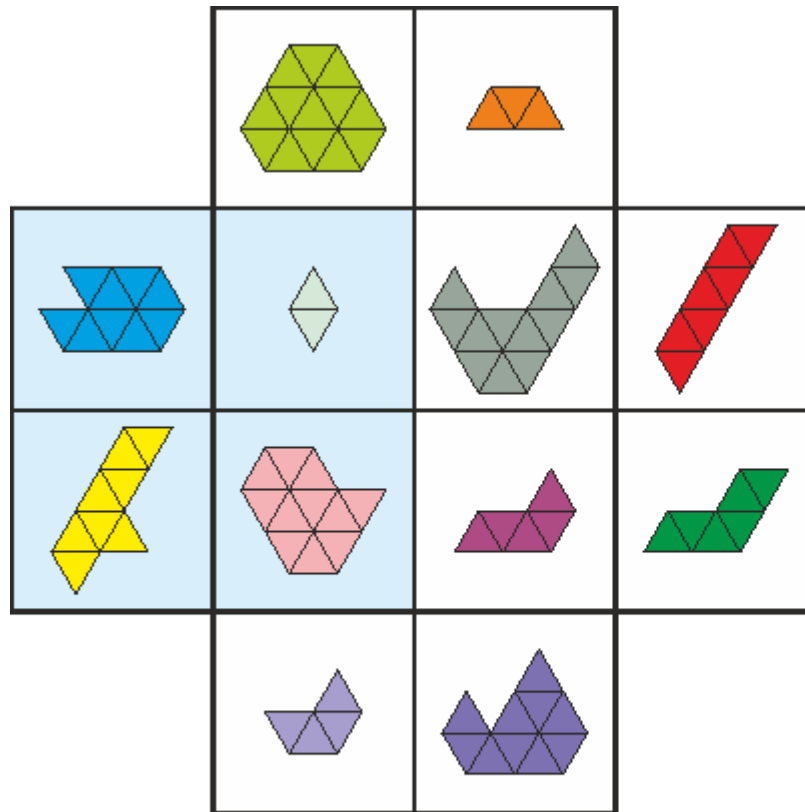




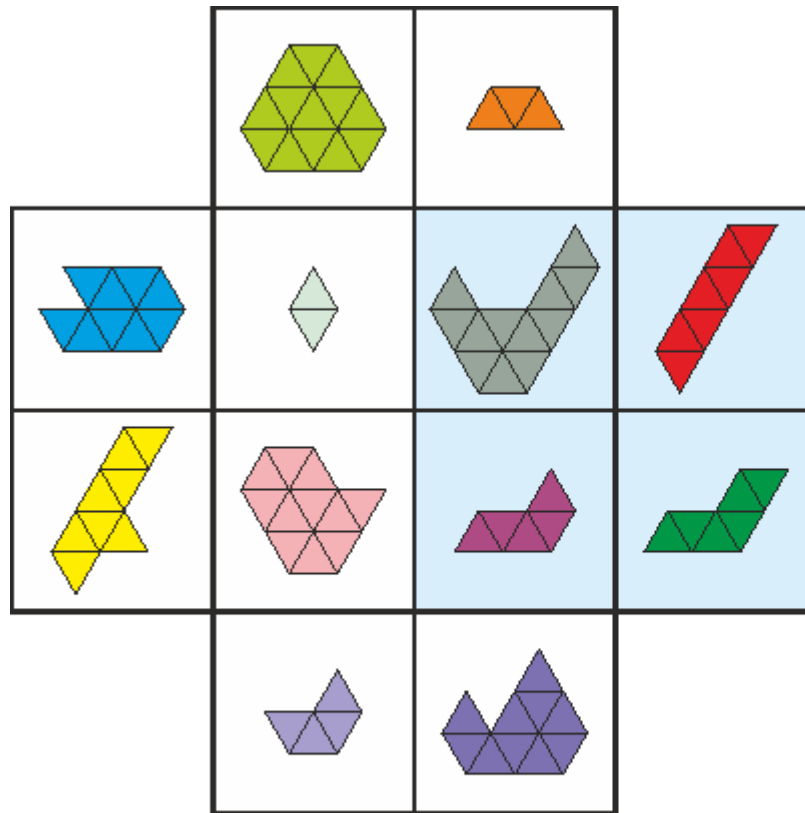
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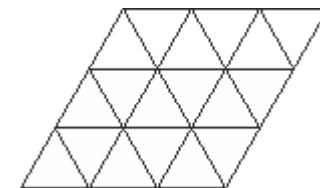
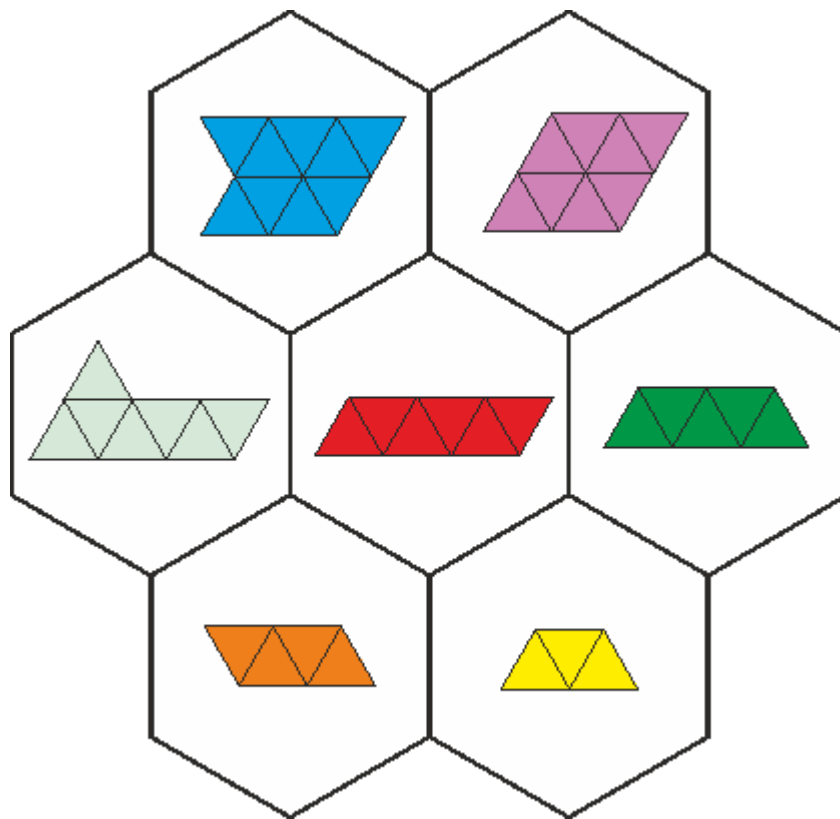
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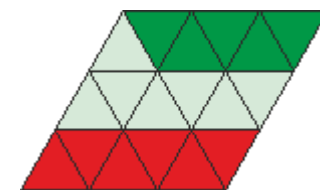
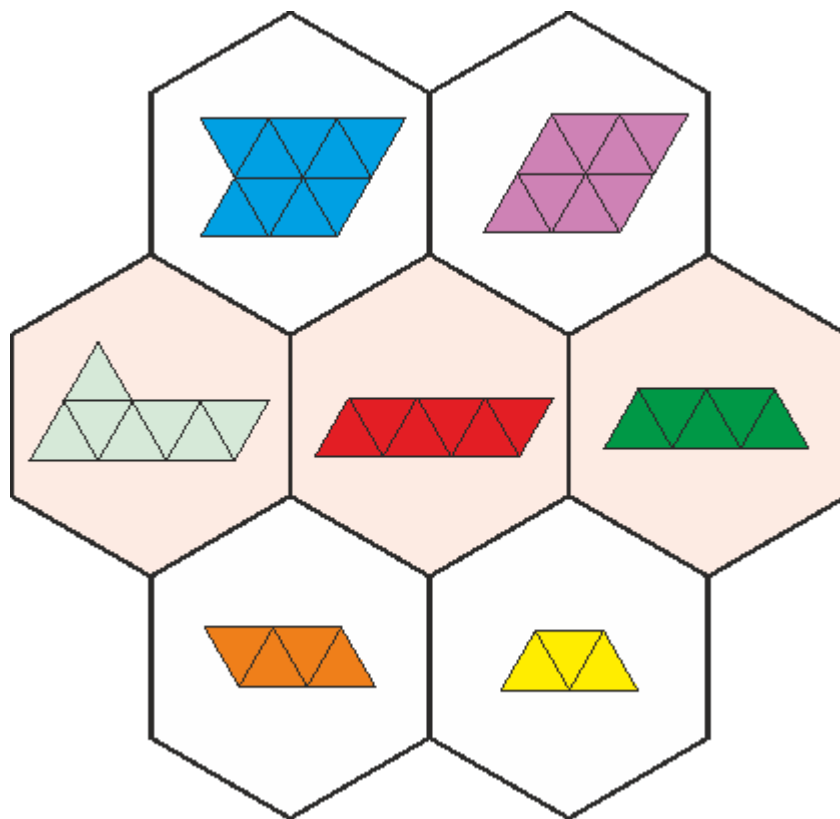
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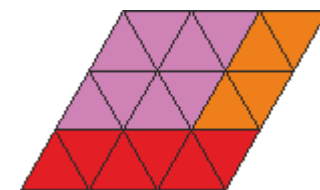
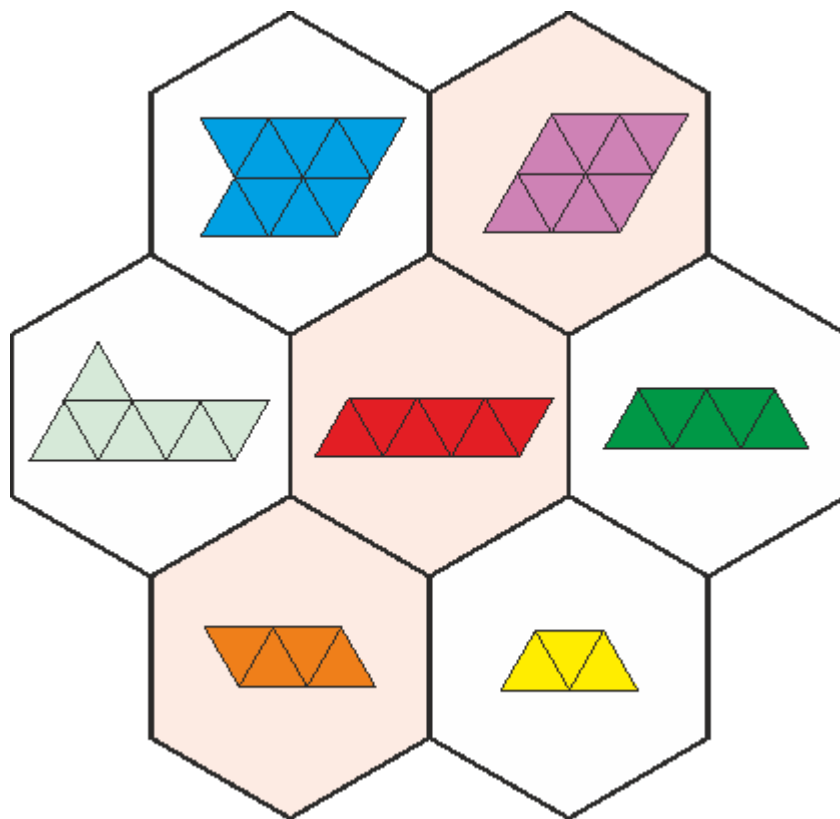
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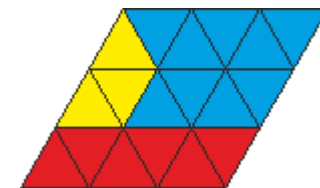
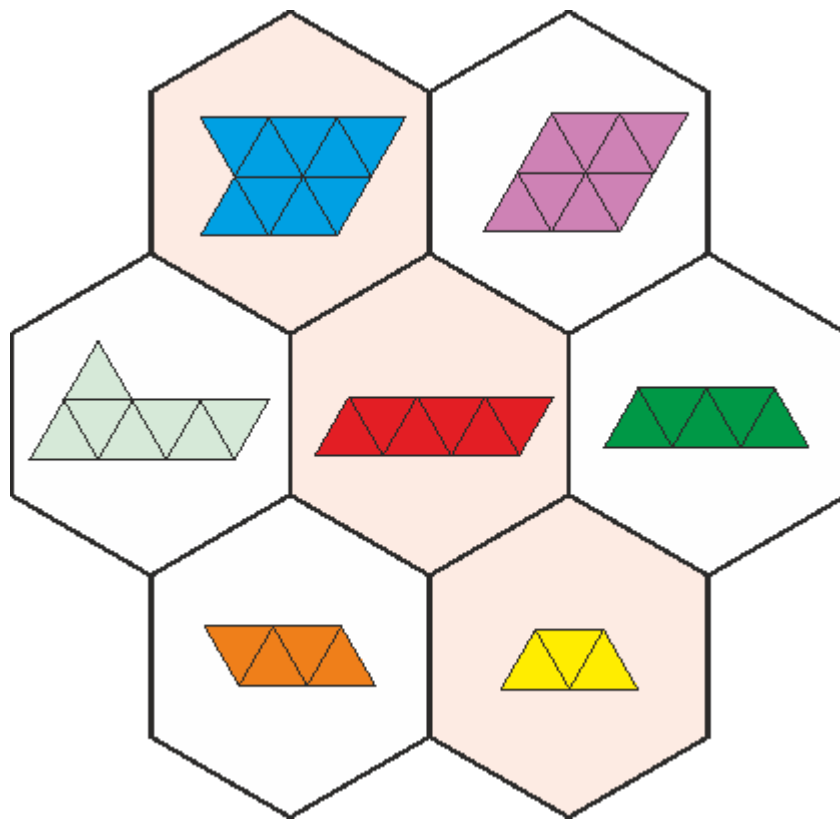
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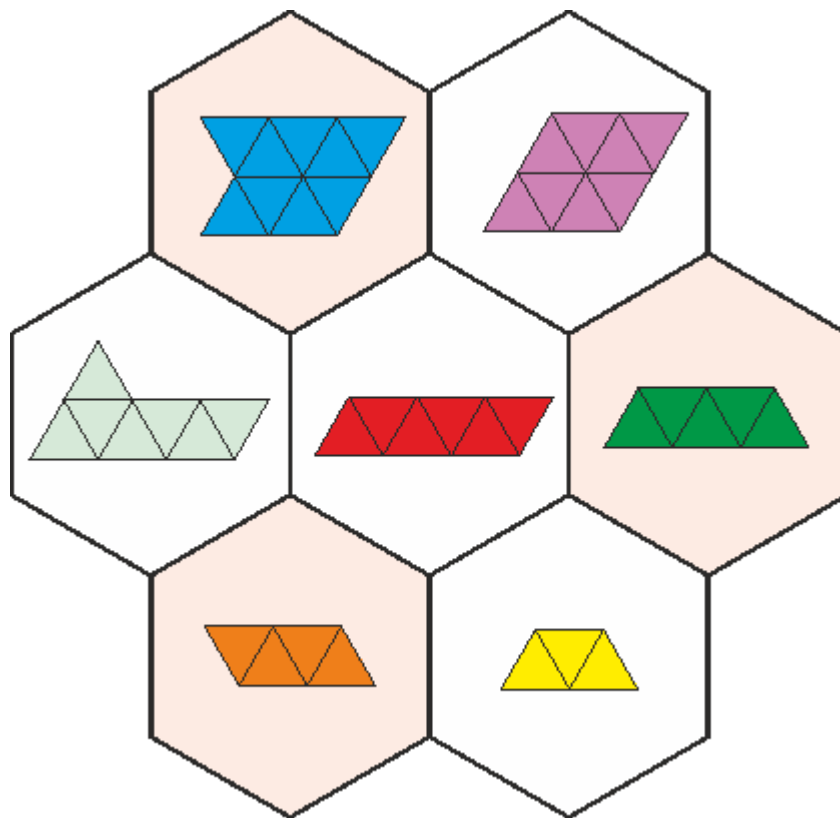
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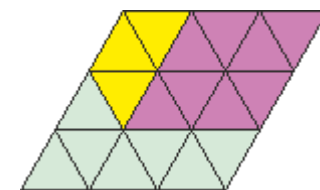
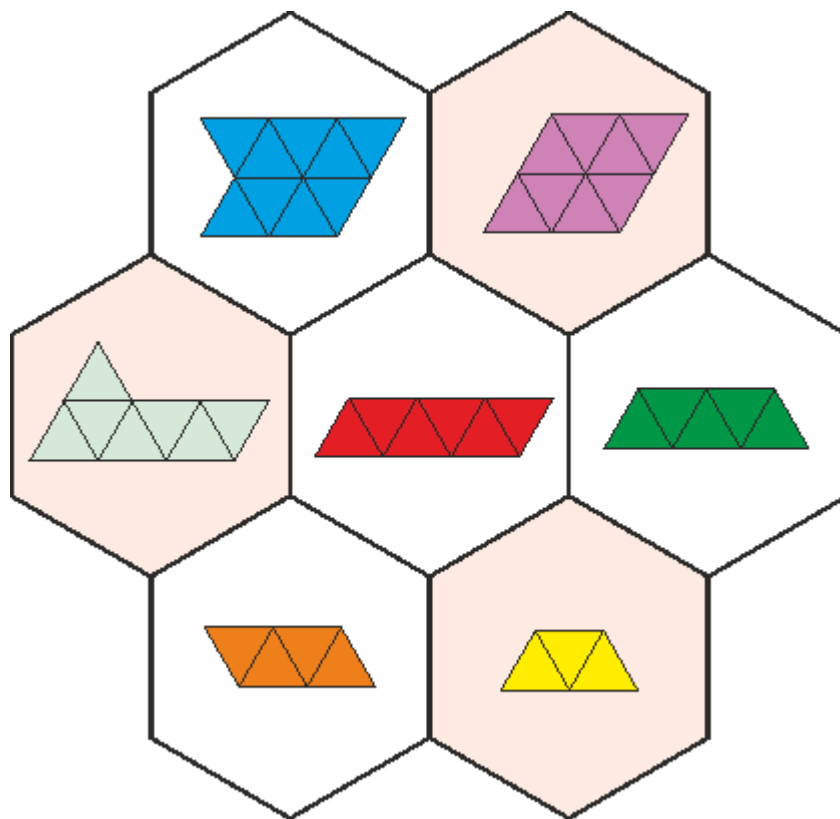


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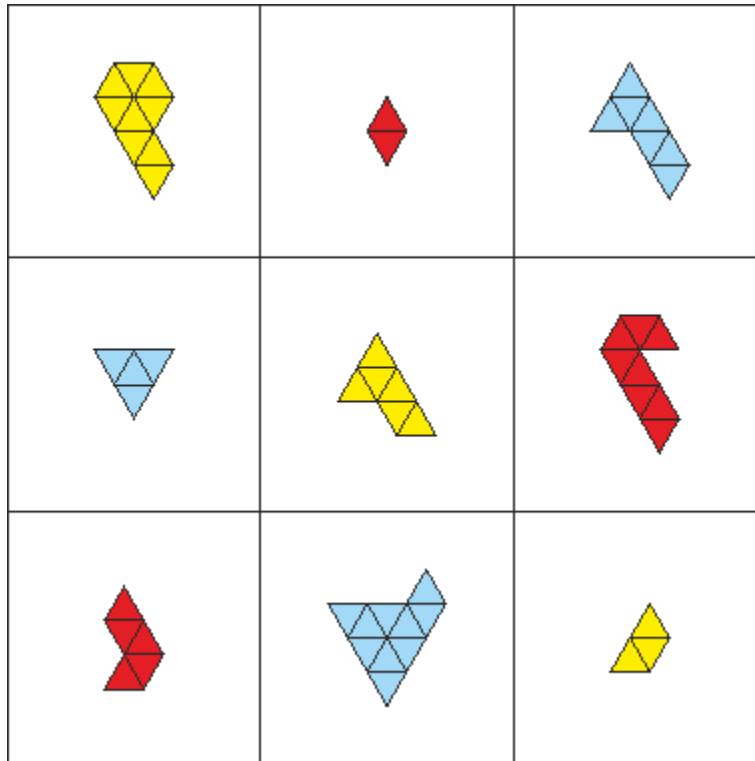




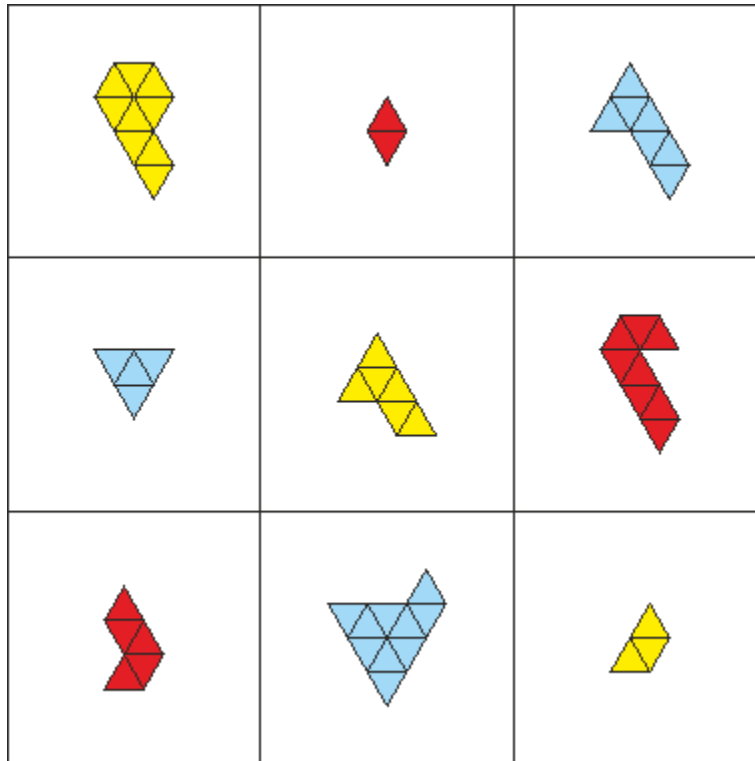
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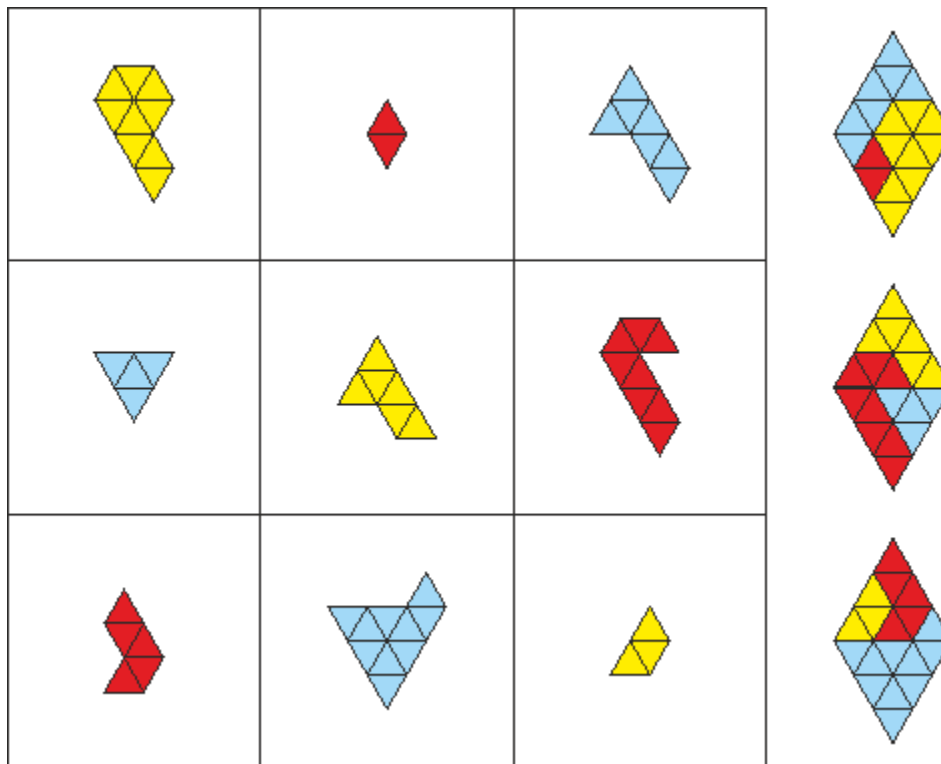
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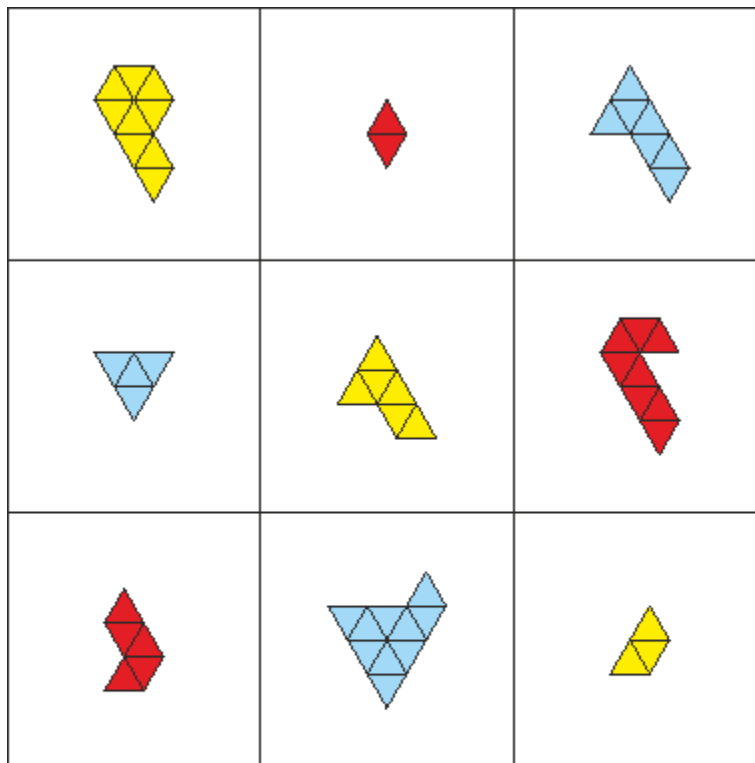
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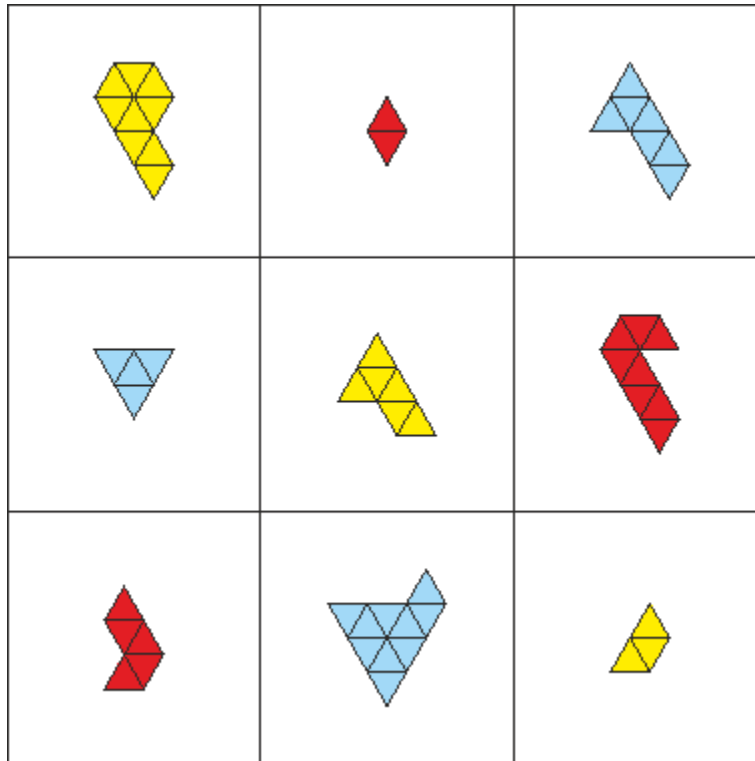
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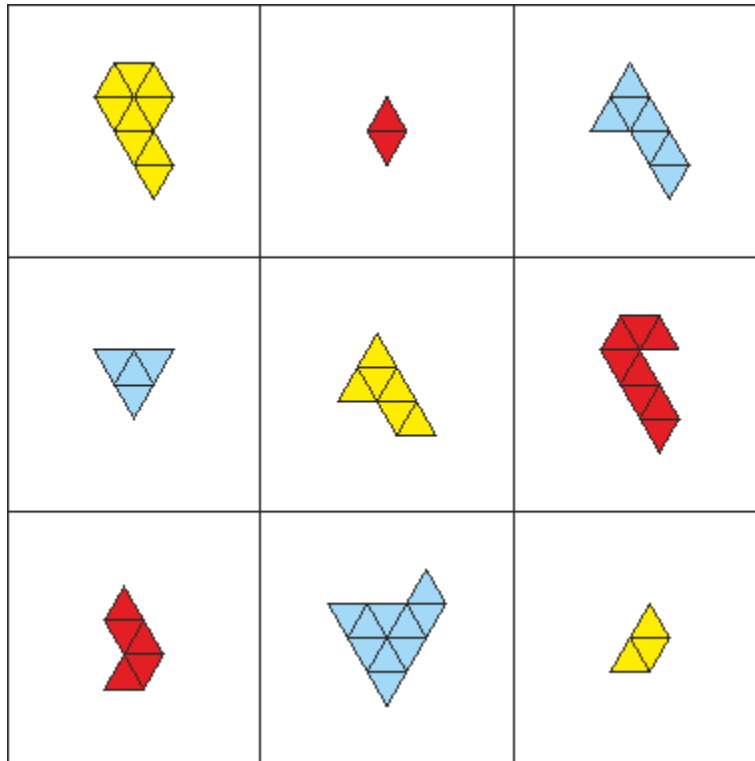
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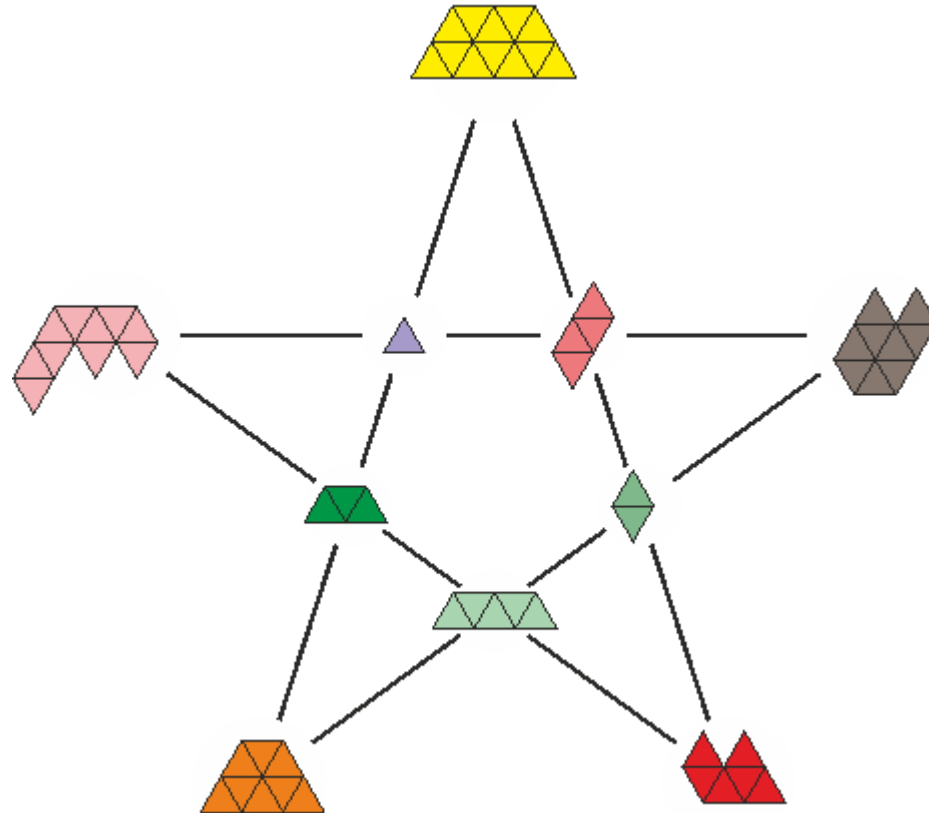
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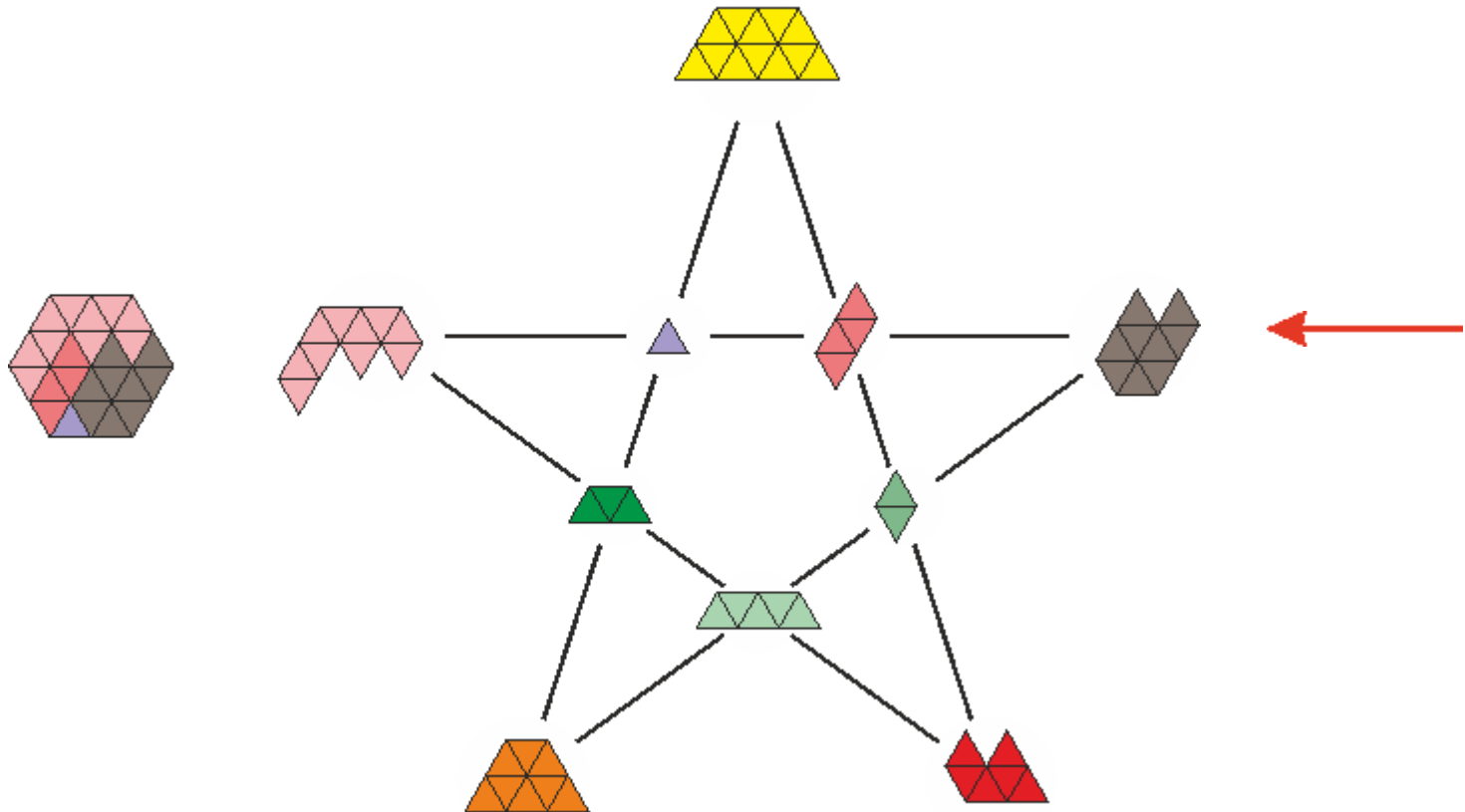


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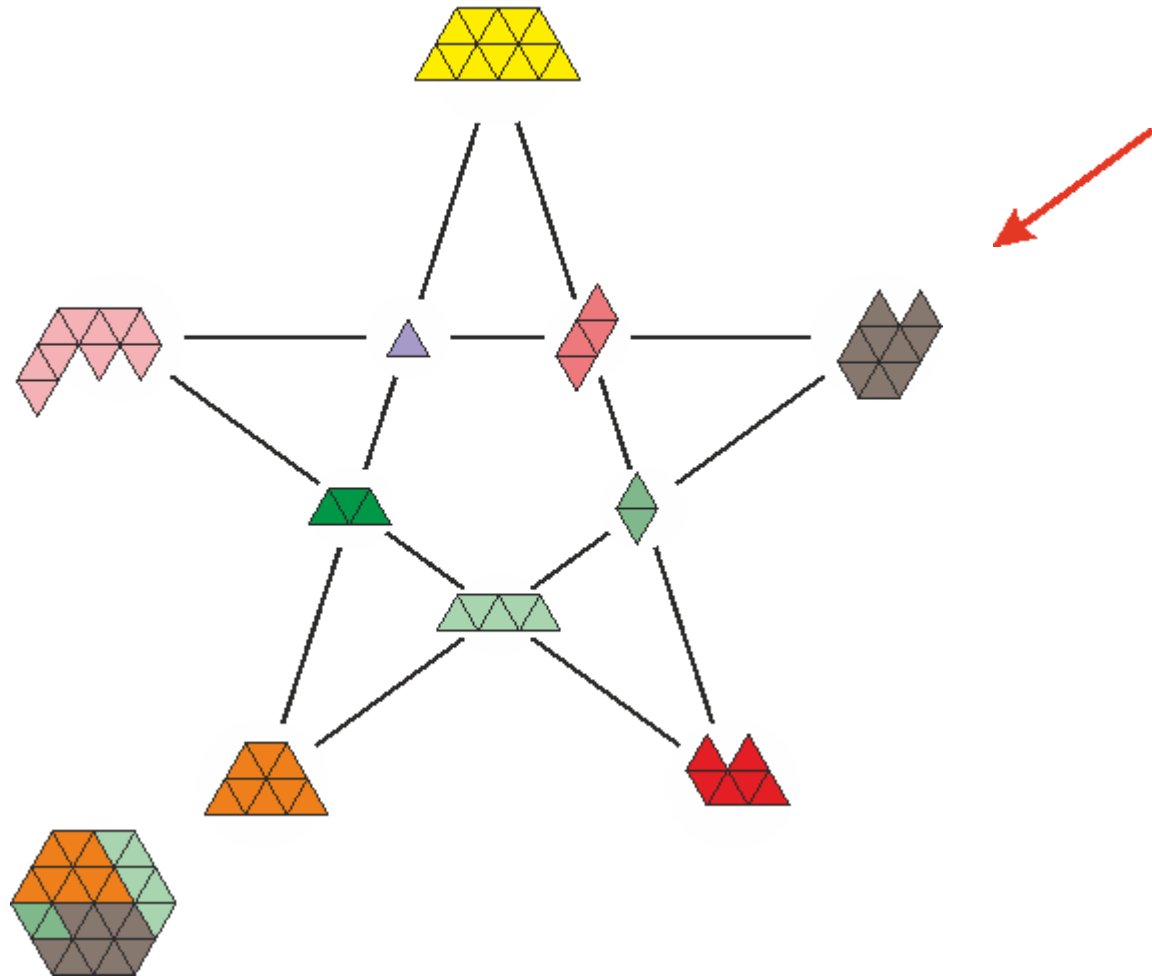




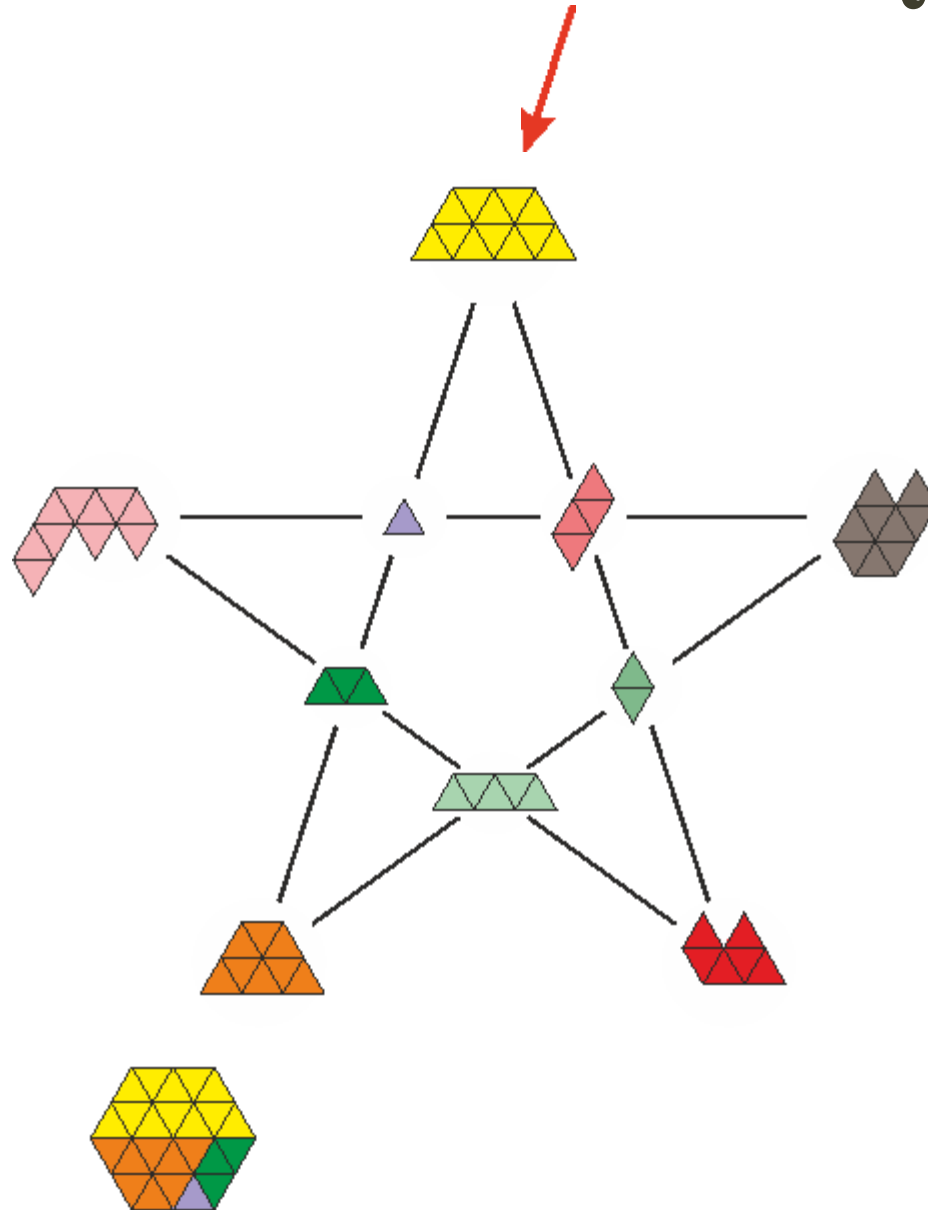
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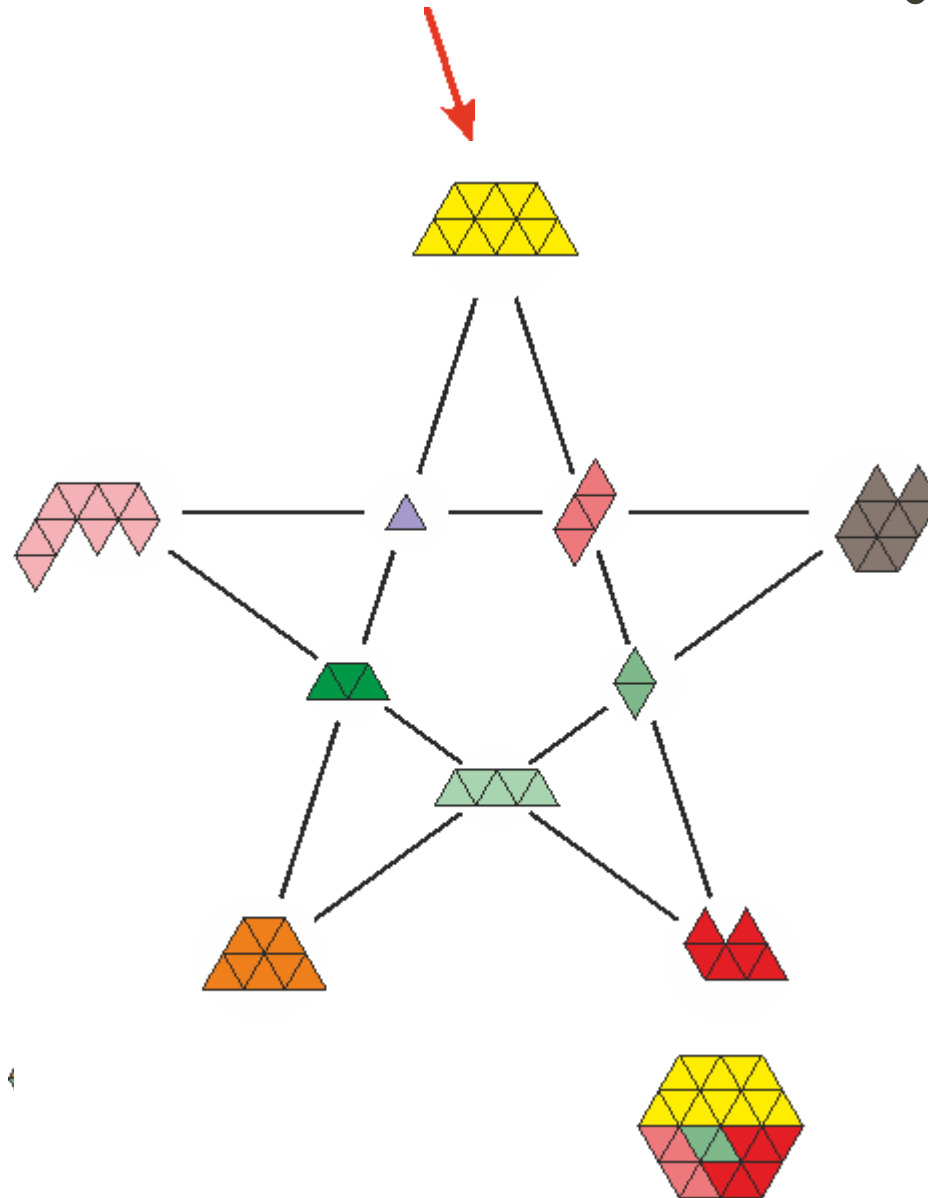
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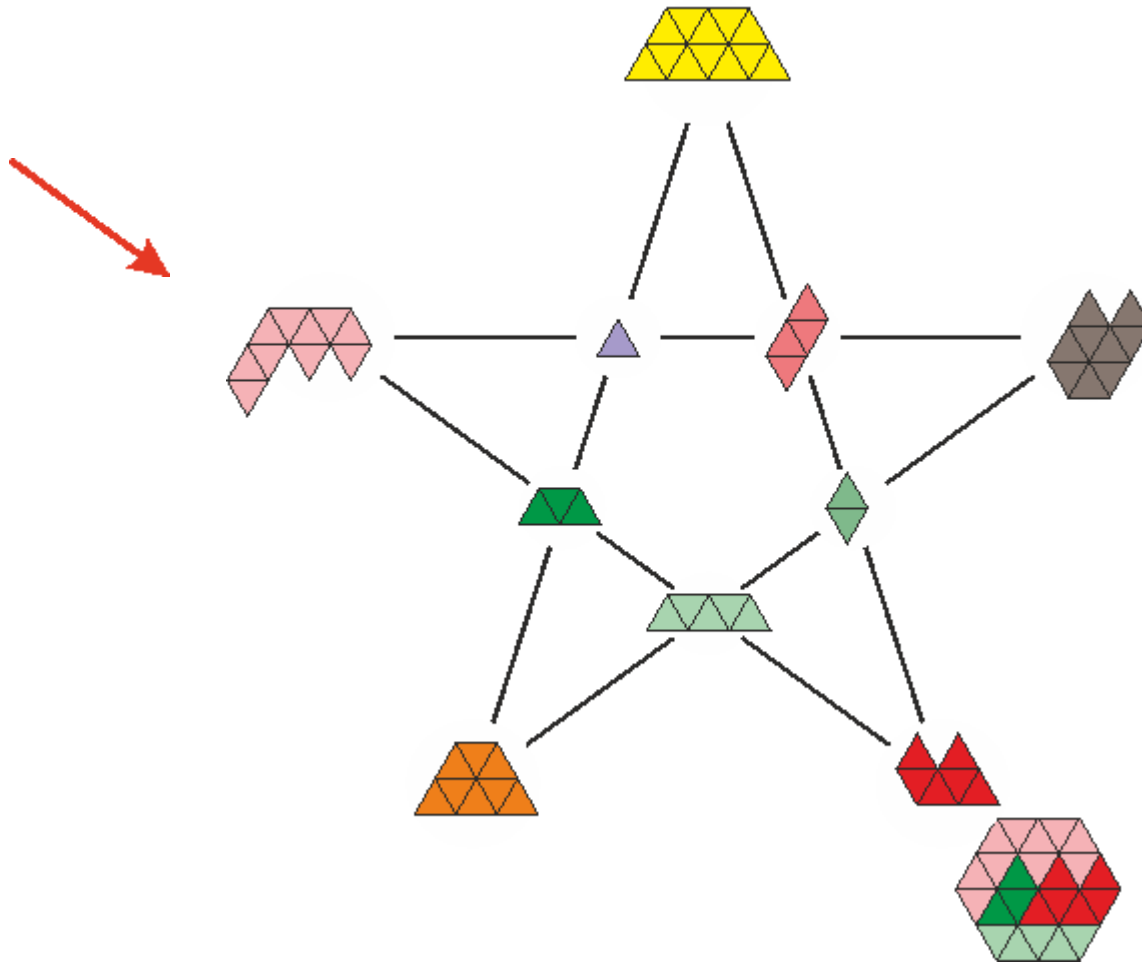
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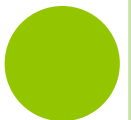
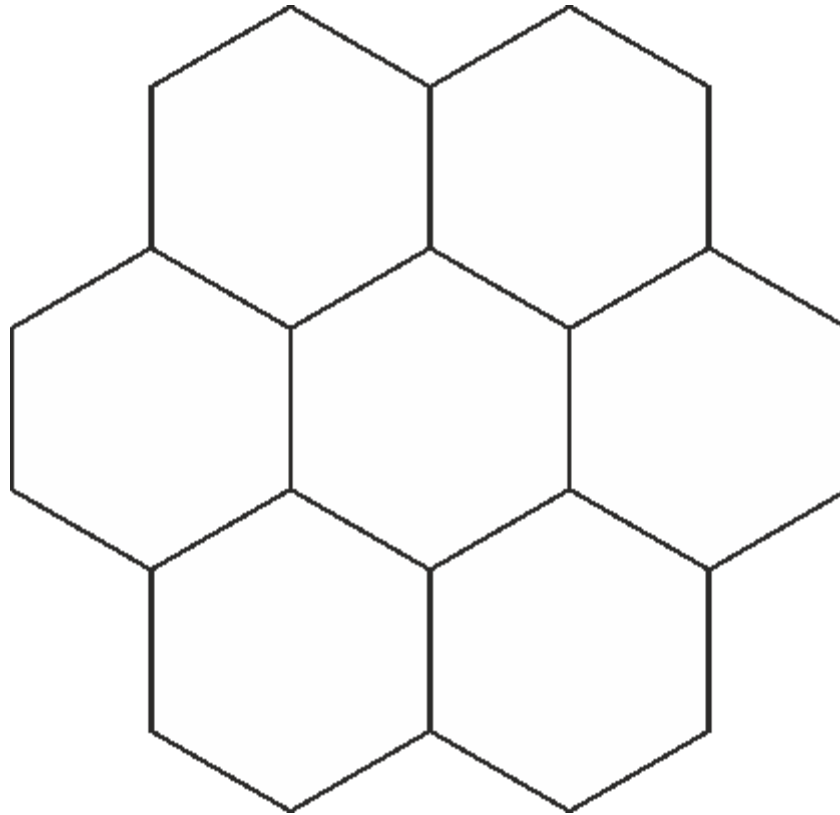
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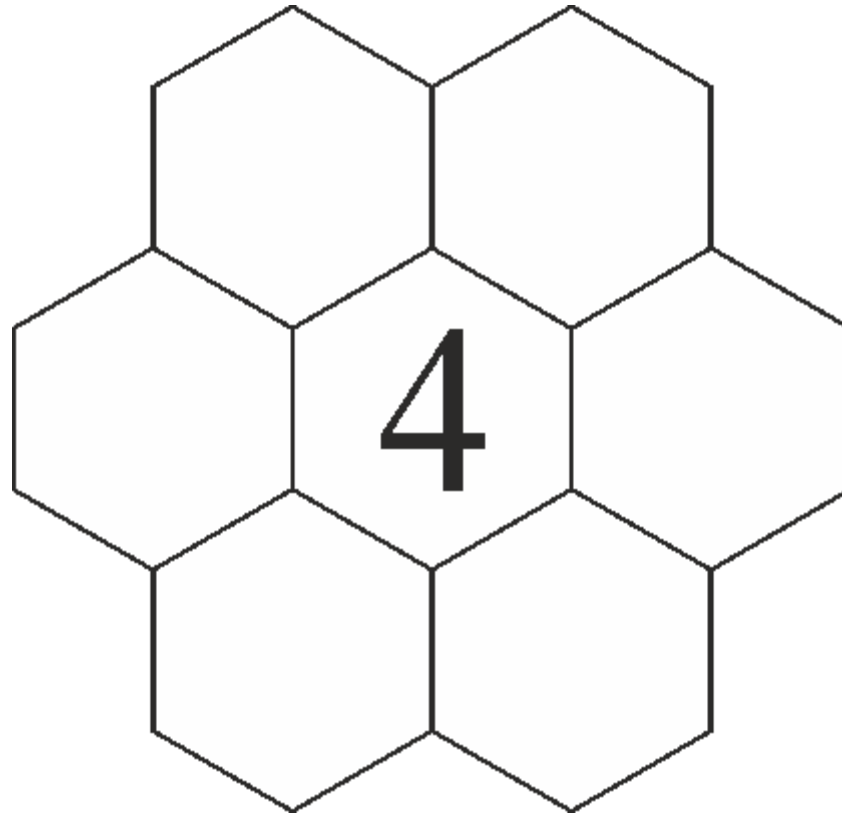
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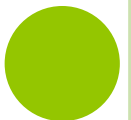
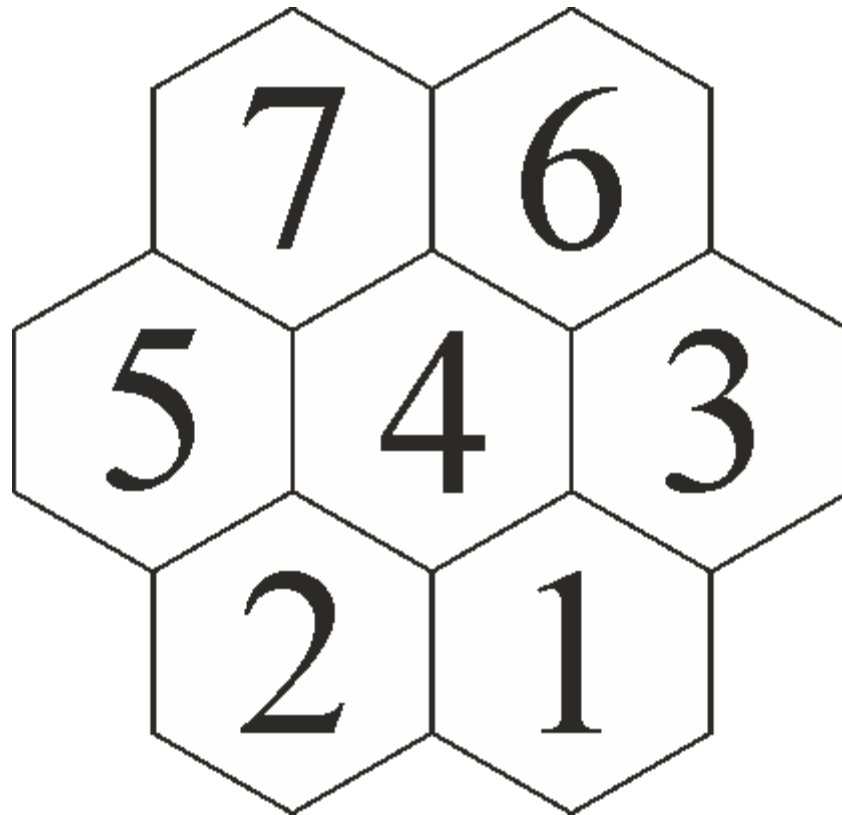
# HEXÀGON MÀGIC



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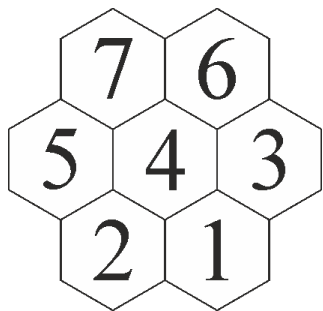


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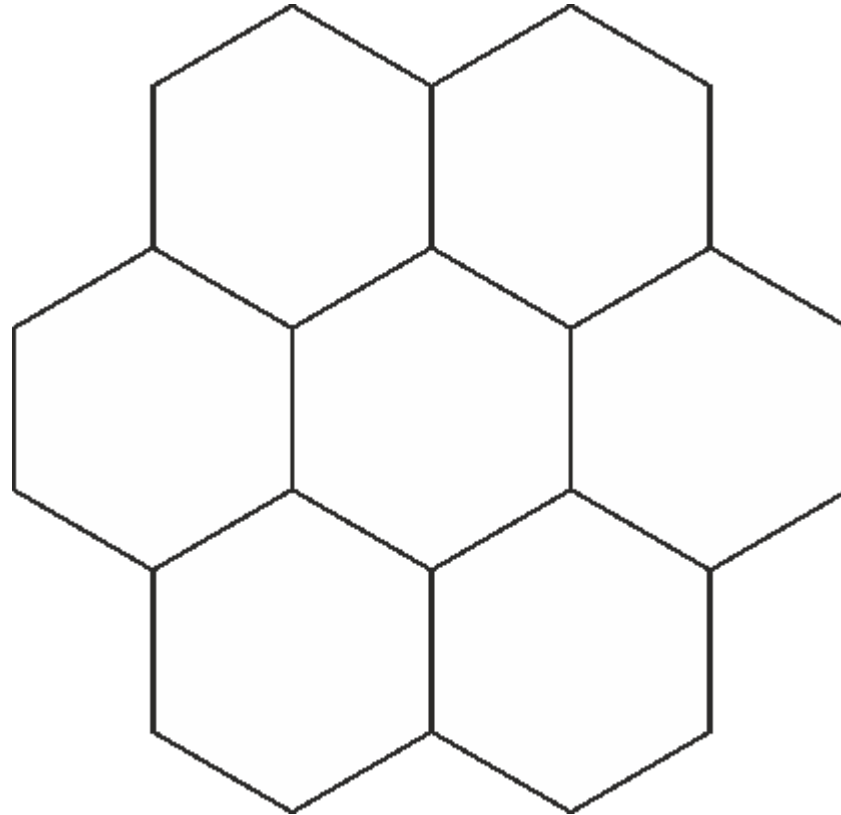
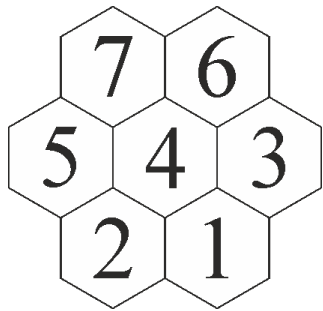




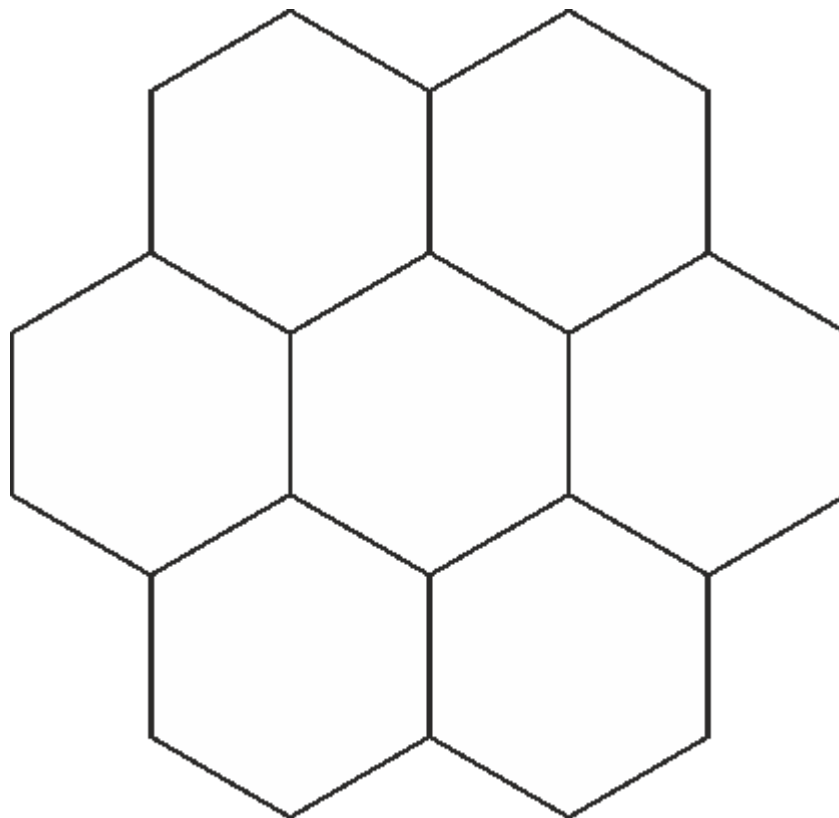
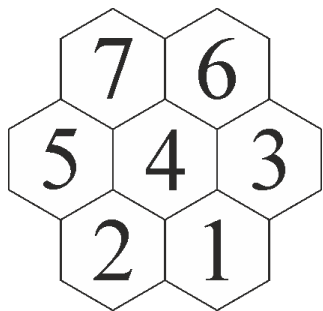
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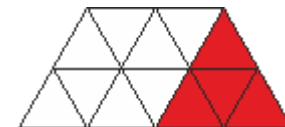
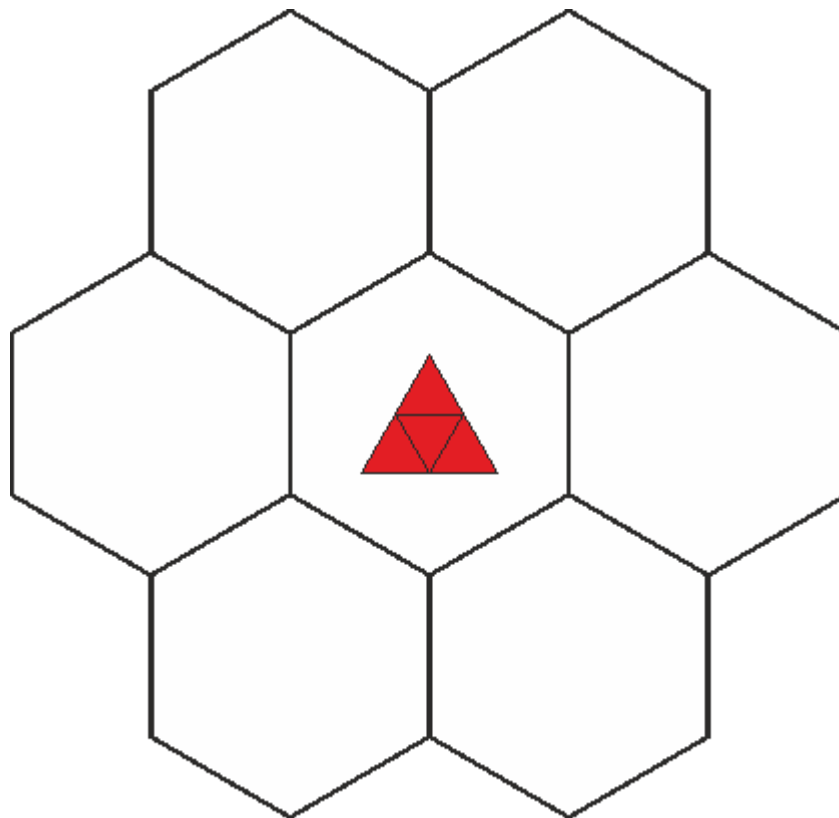
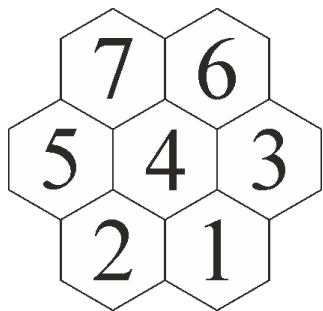
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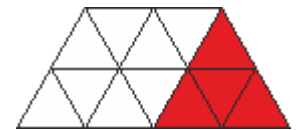
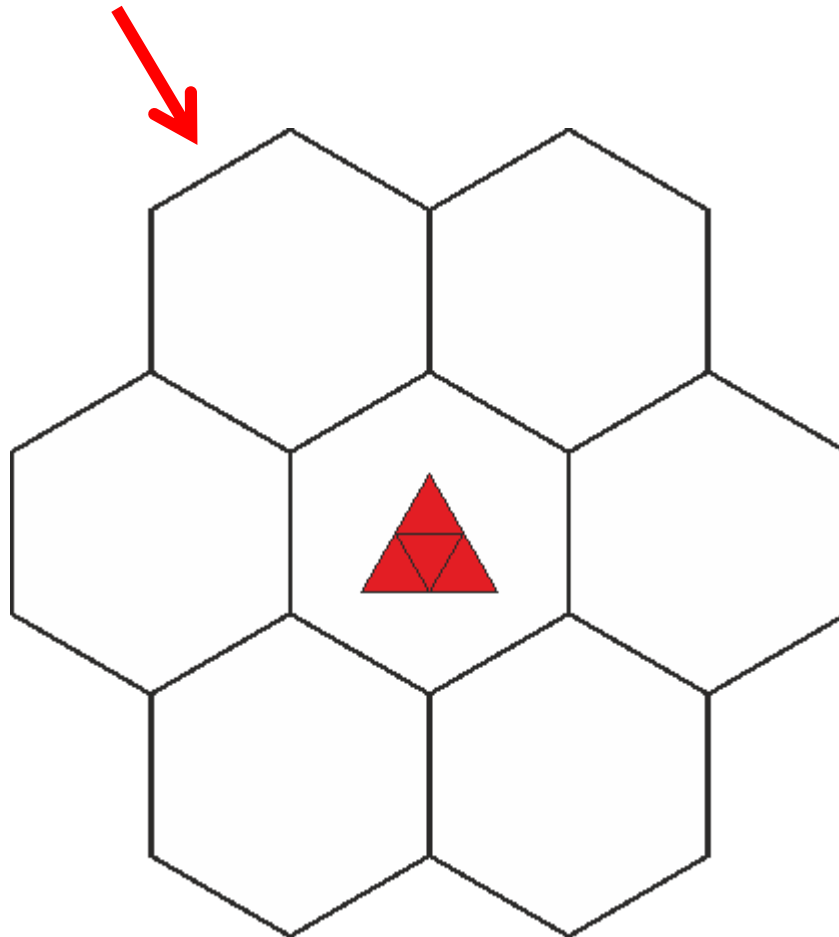
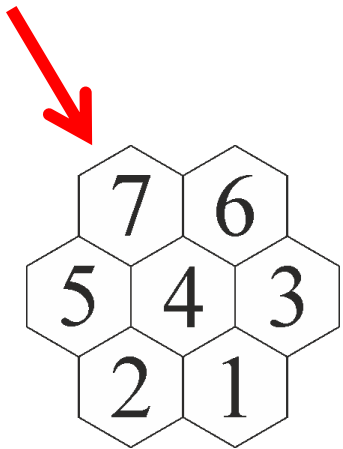
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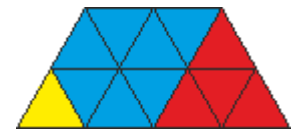
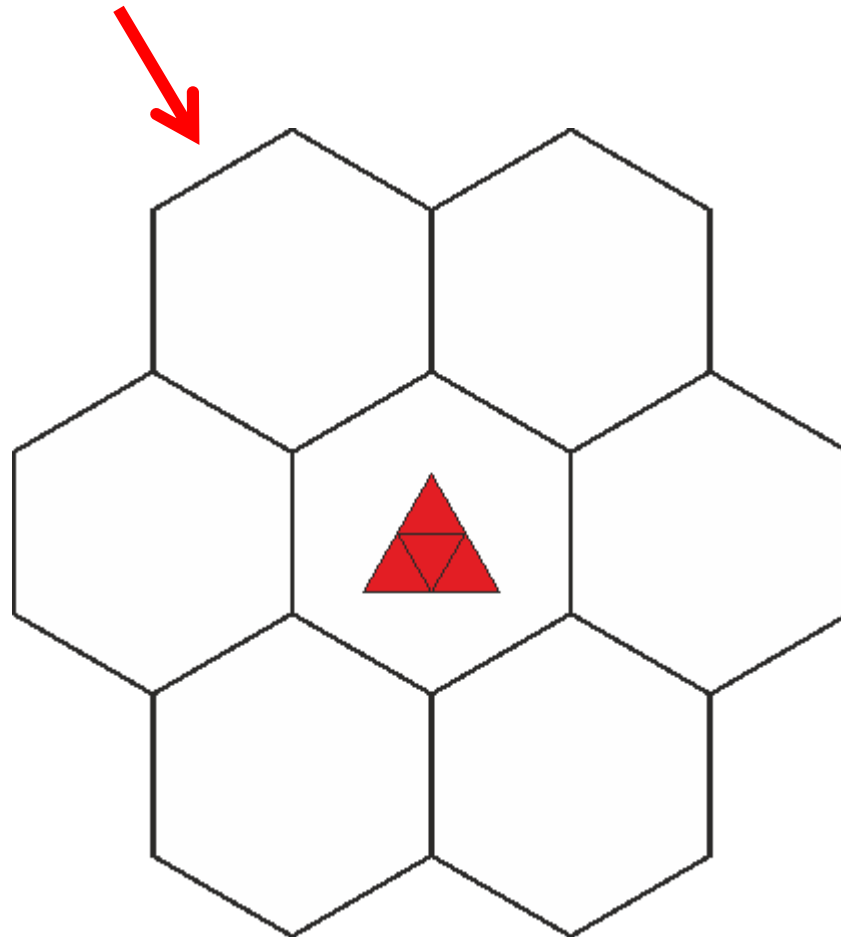
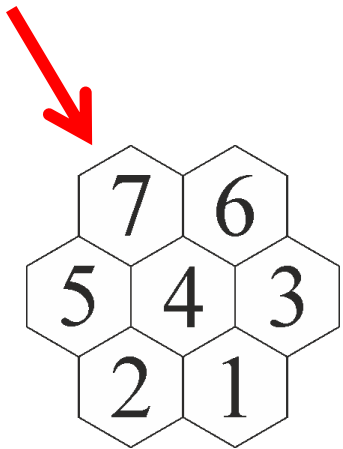
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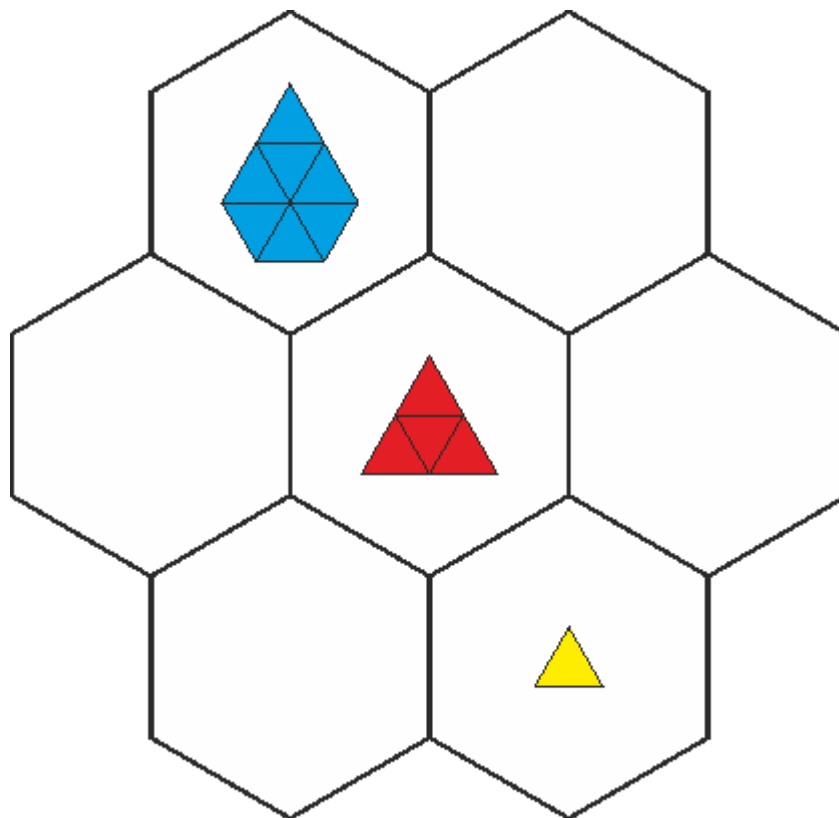
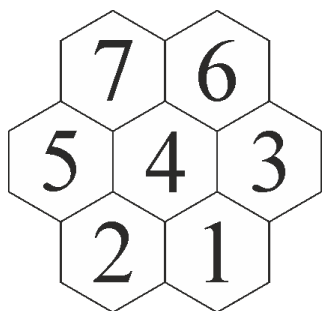
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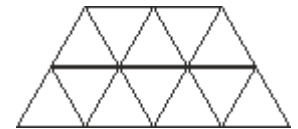
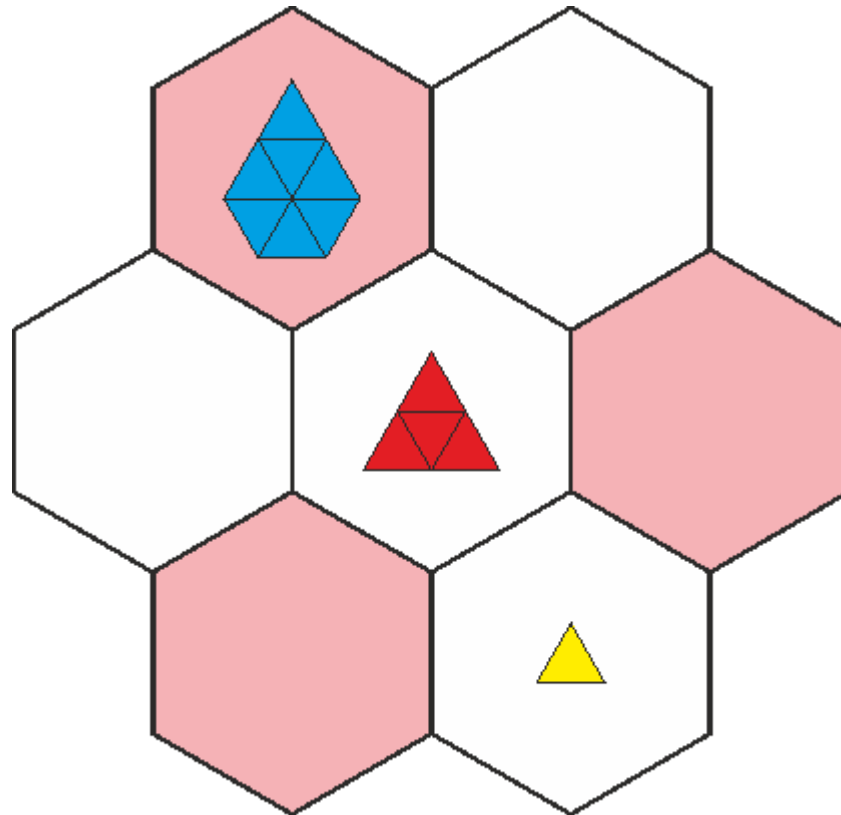
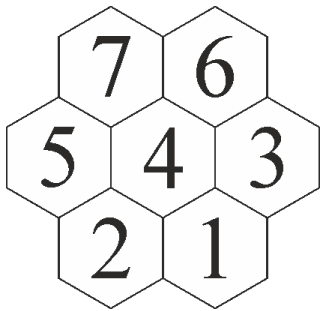
# HEXÀGON GEOMÀGIC



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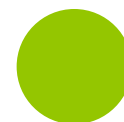
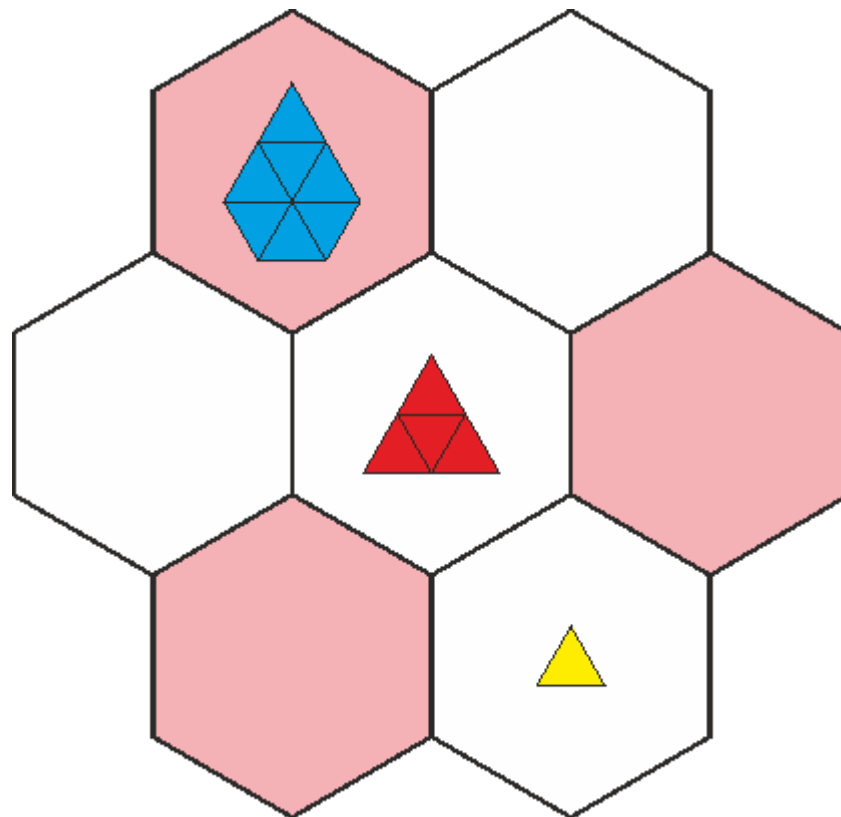
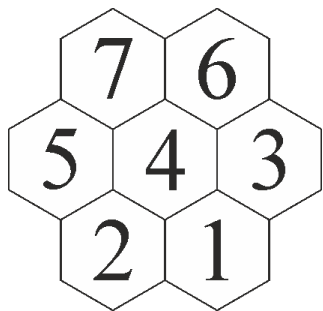


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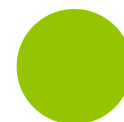
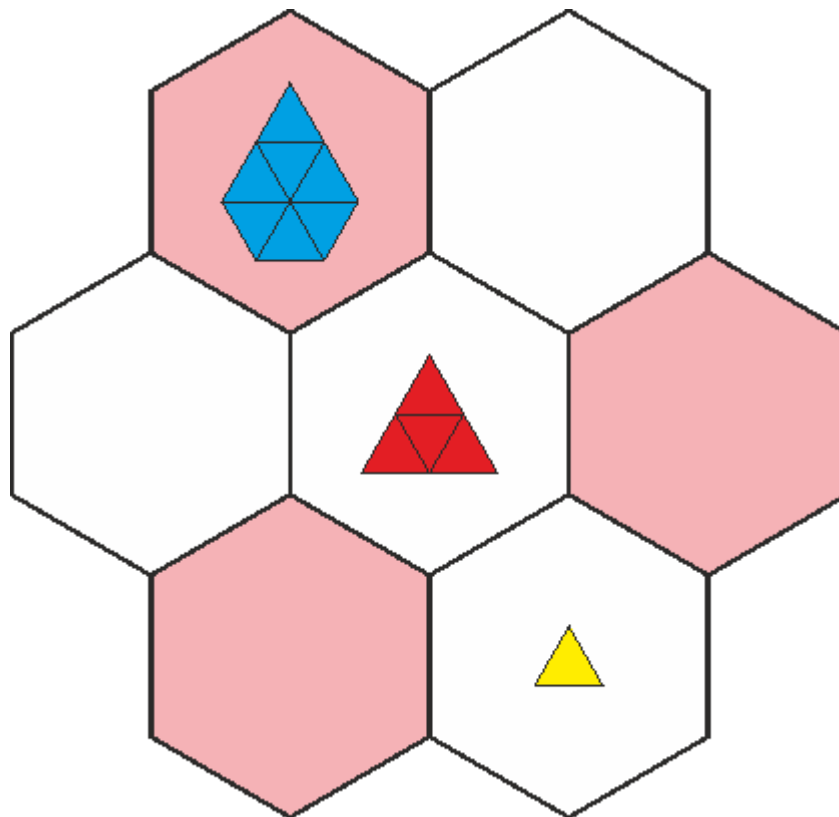
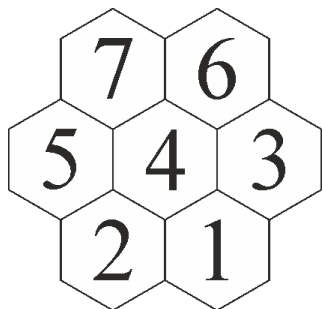




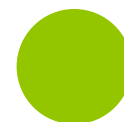
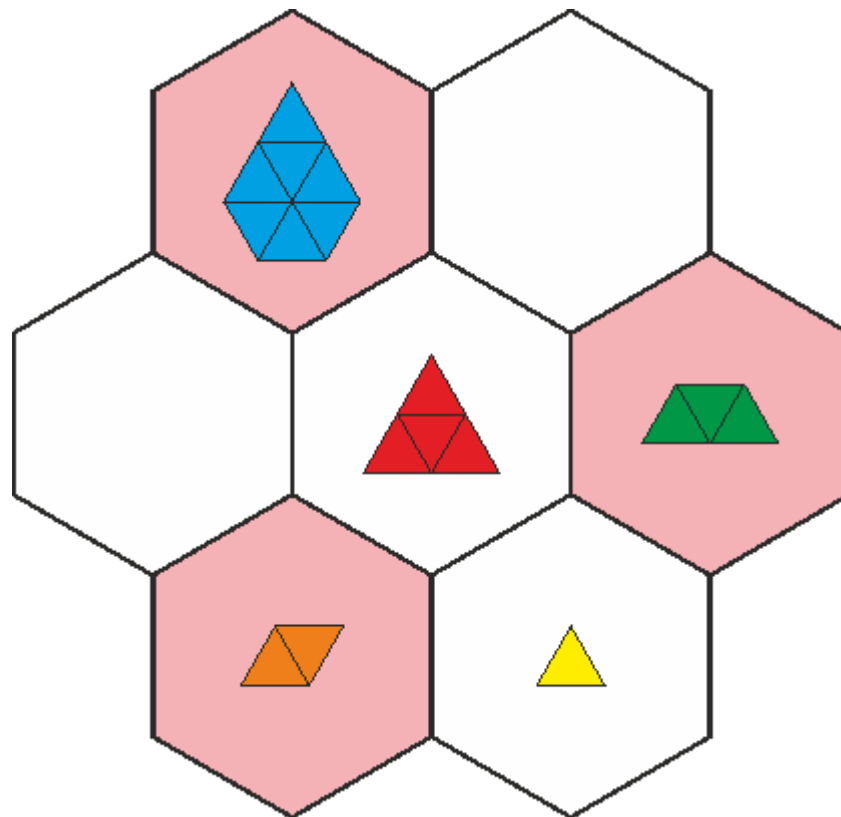
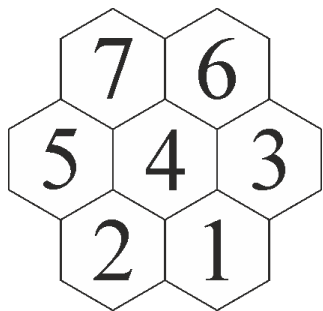
# HEXÀGON GEOMÀGIC



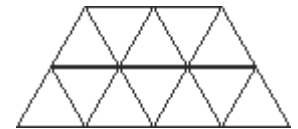
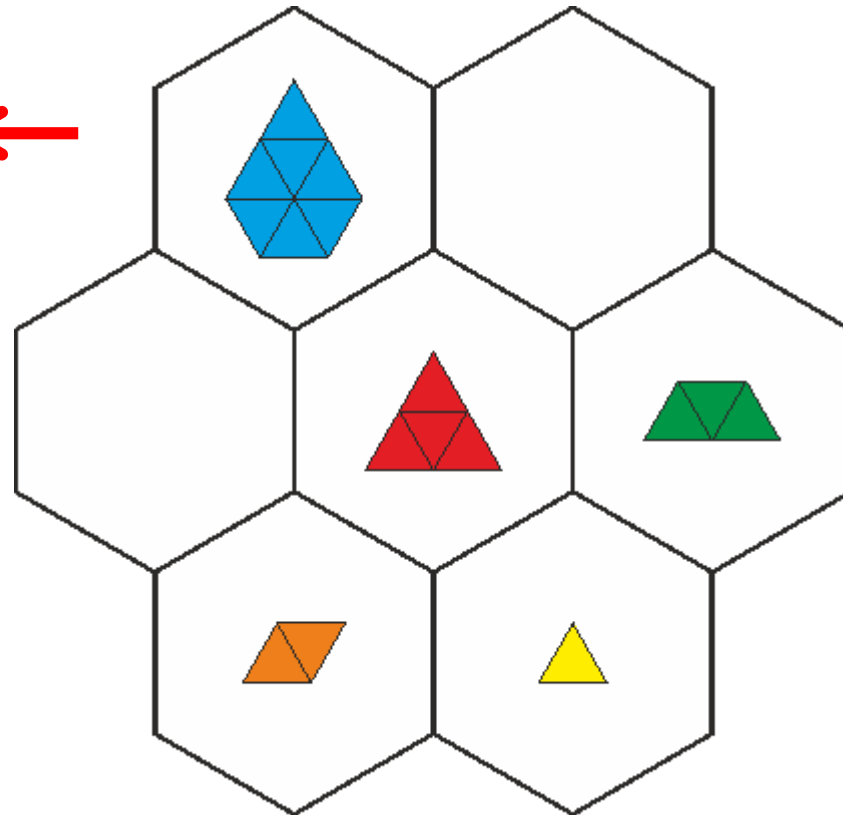
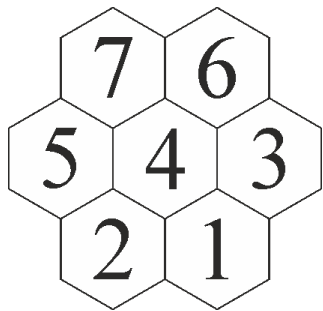
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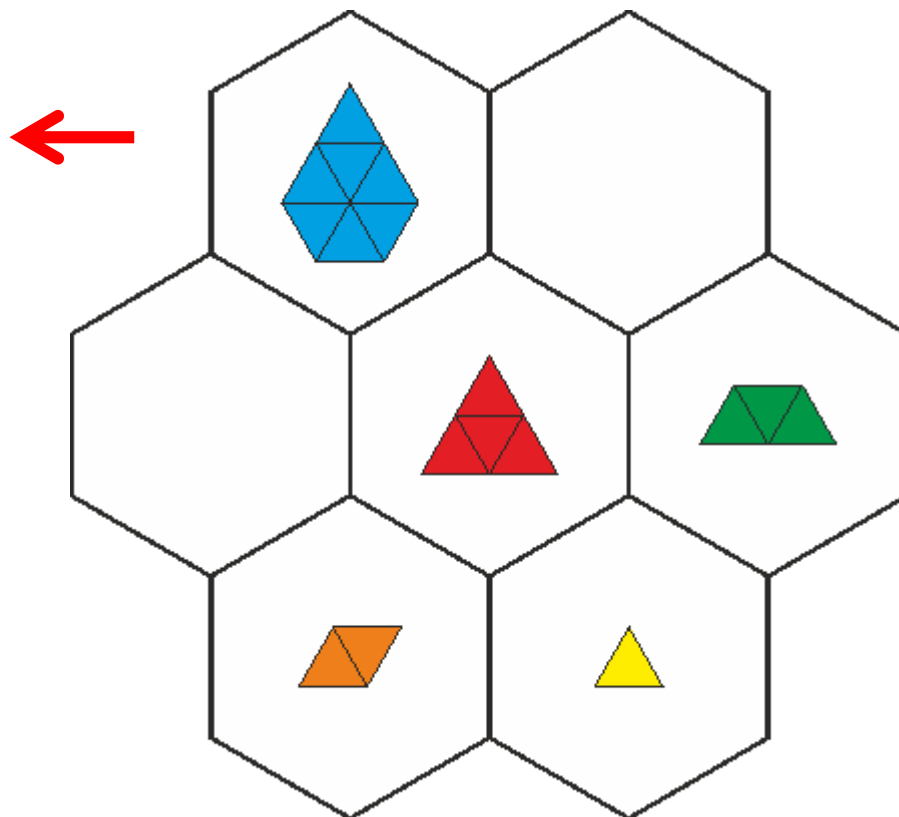
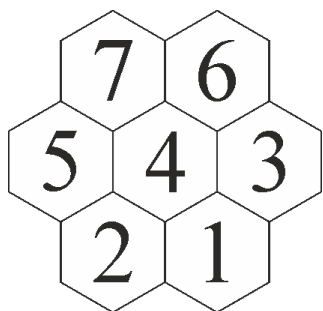
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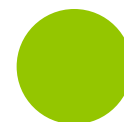
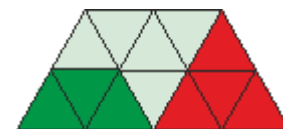
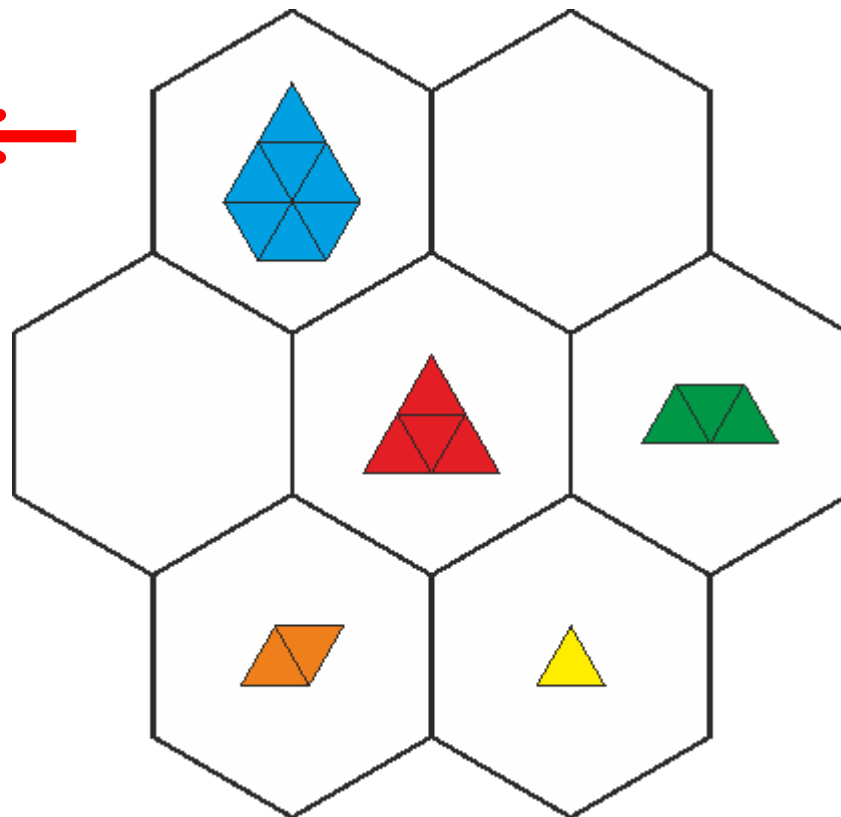
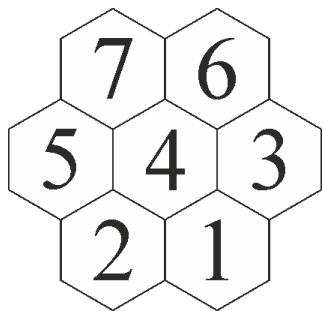
# HEXÀGON GEOMÀGIC



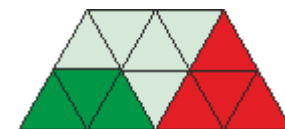
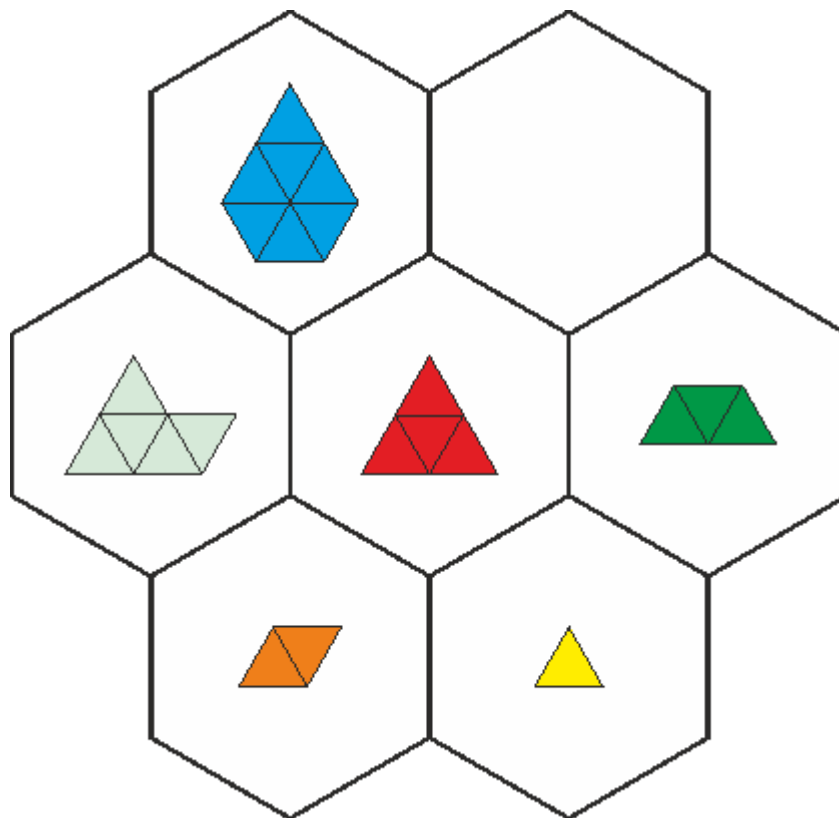
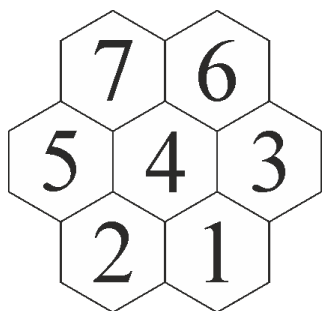
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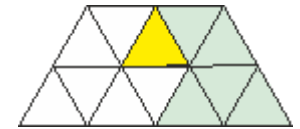
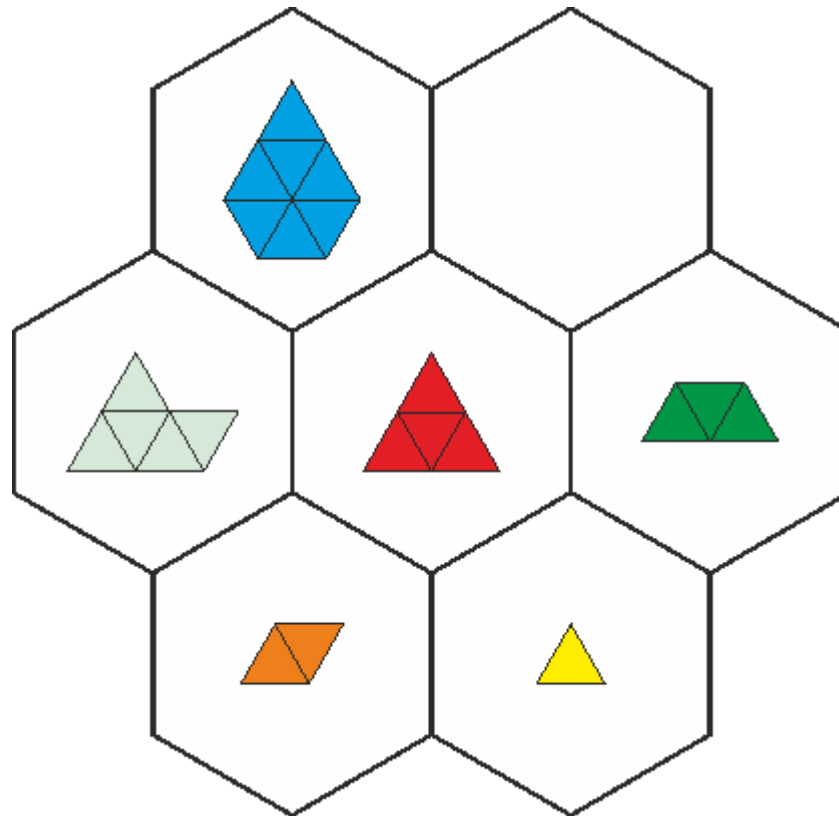
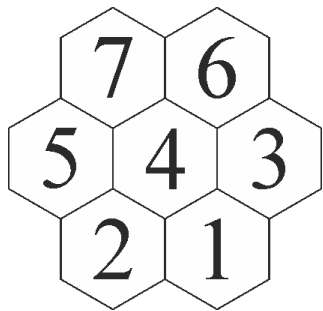
# HEXÀGON GEOMÀGIC



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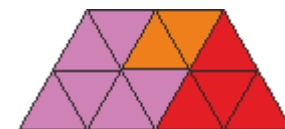
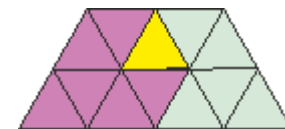
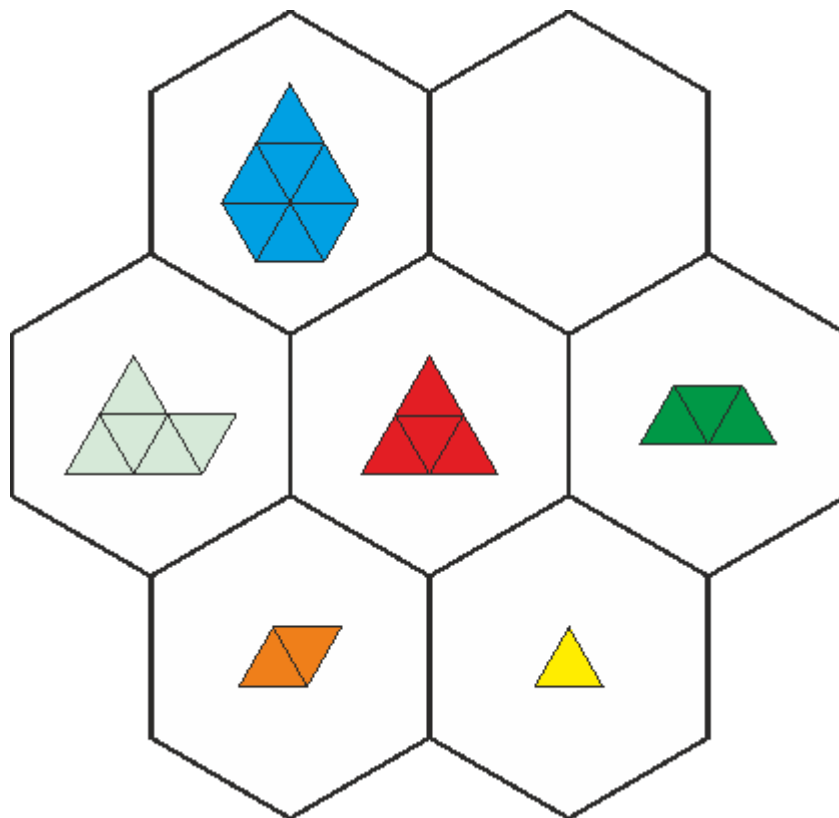
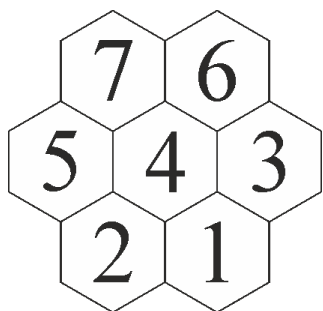


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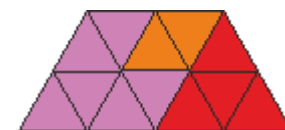
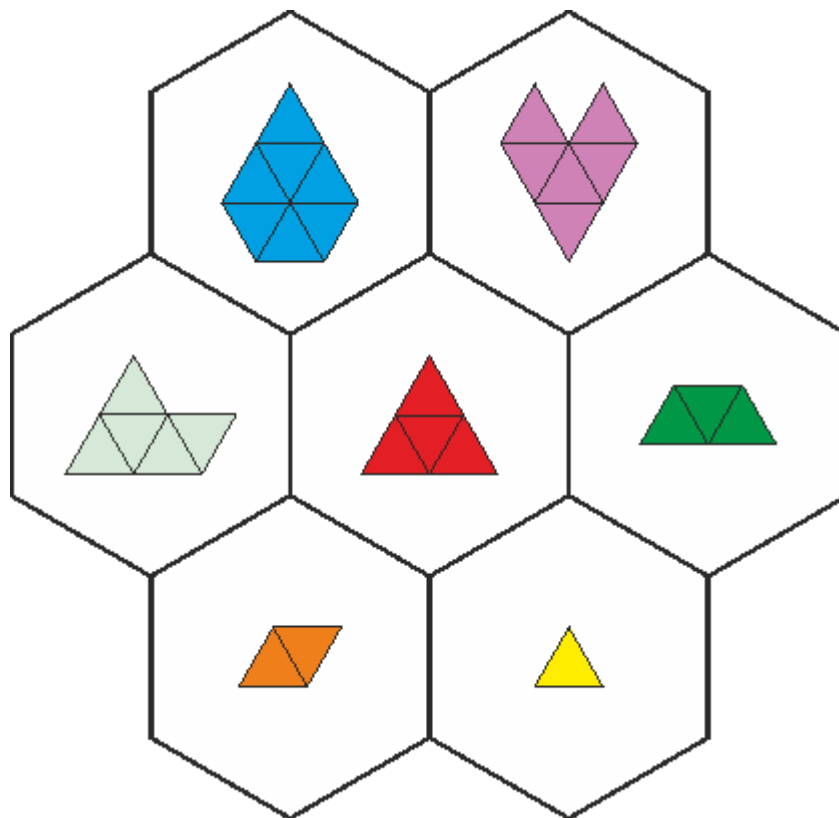
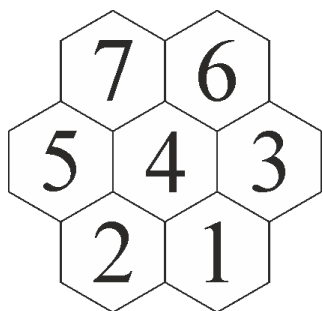




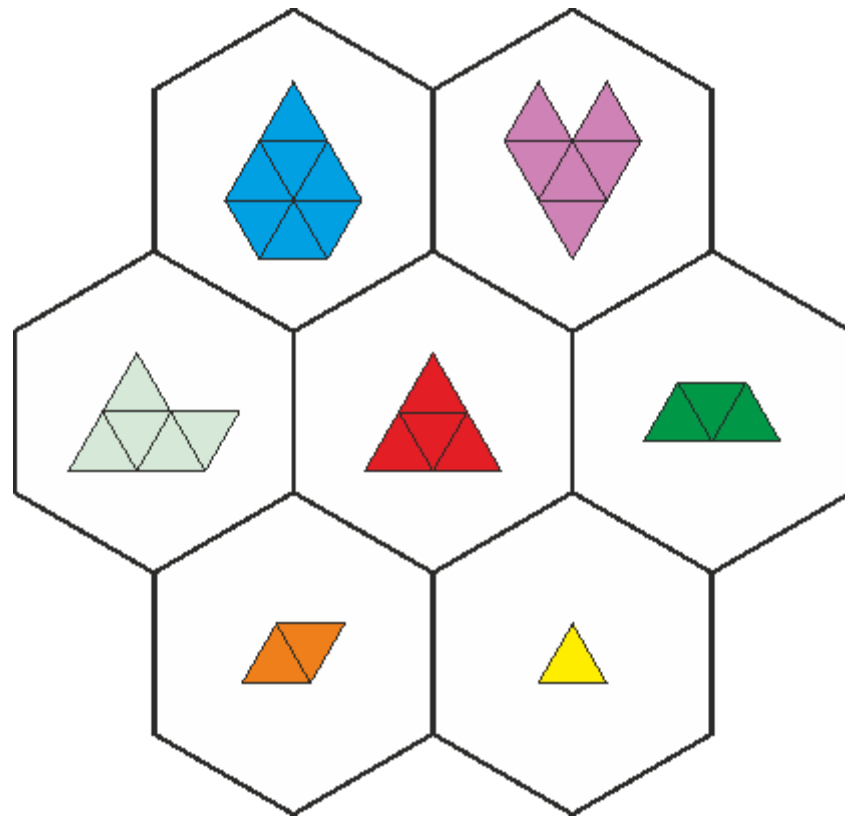
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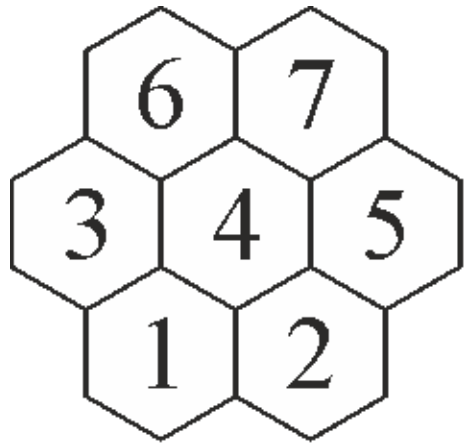
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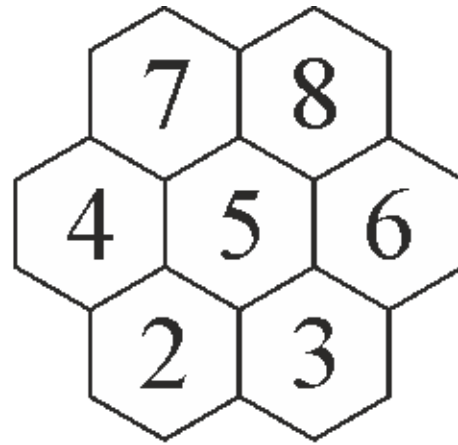
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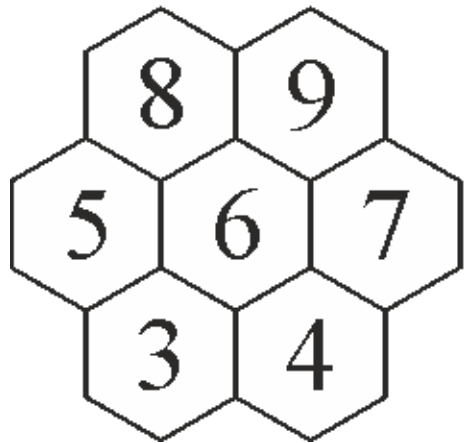
# HEXÀGONS MÀGICS



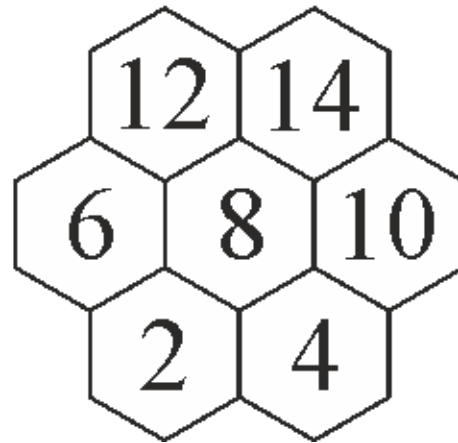
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15



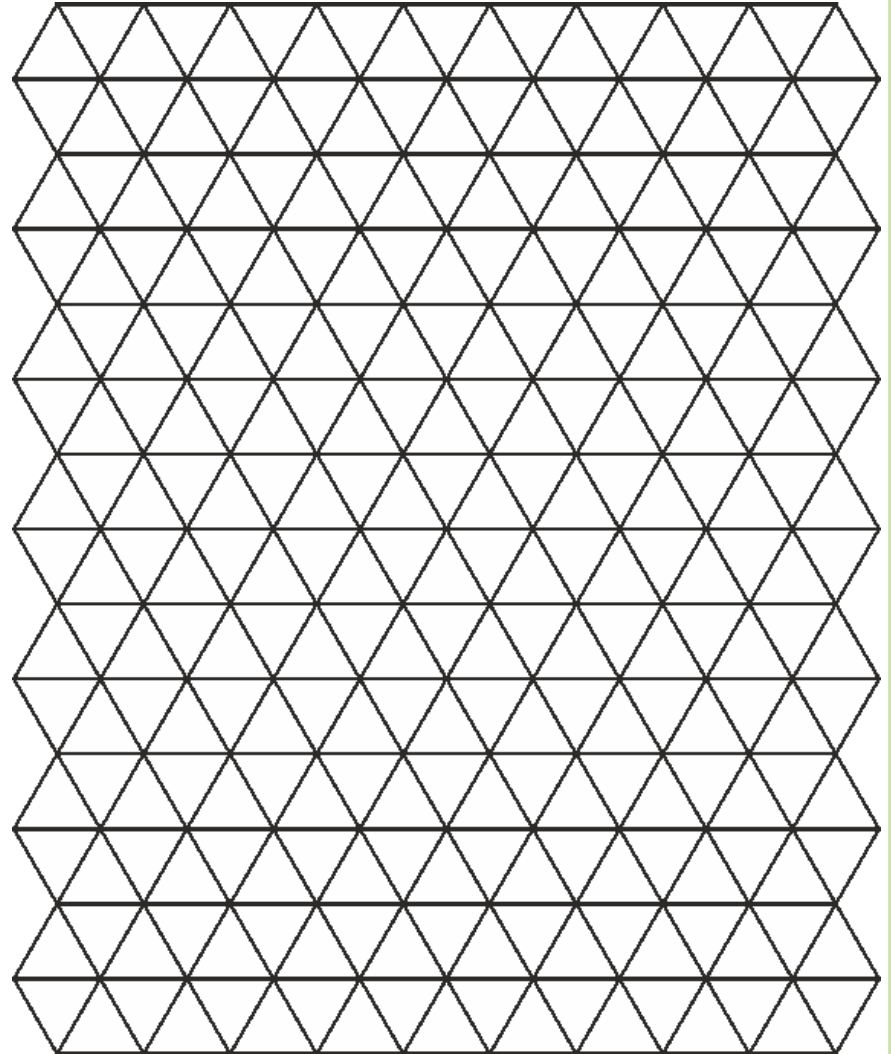
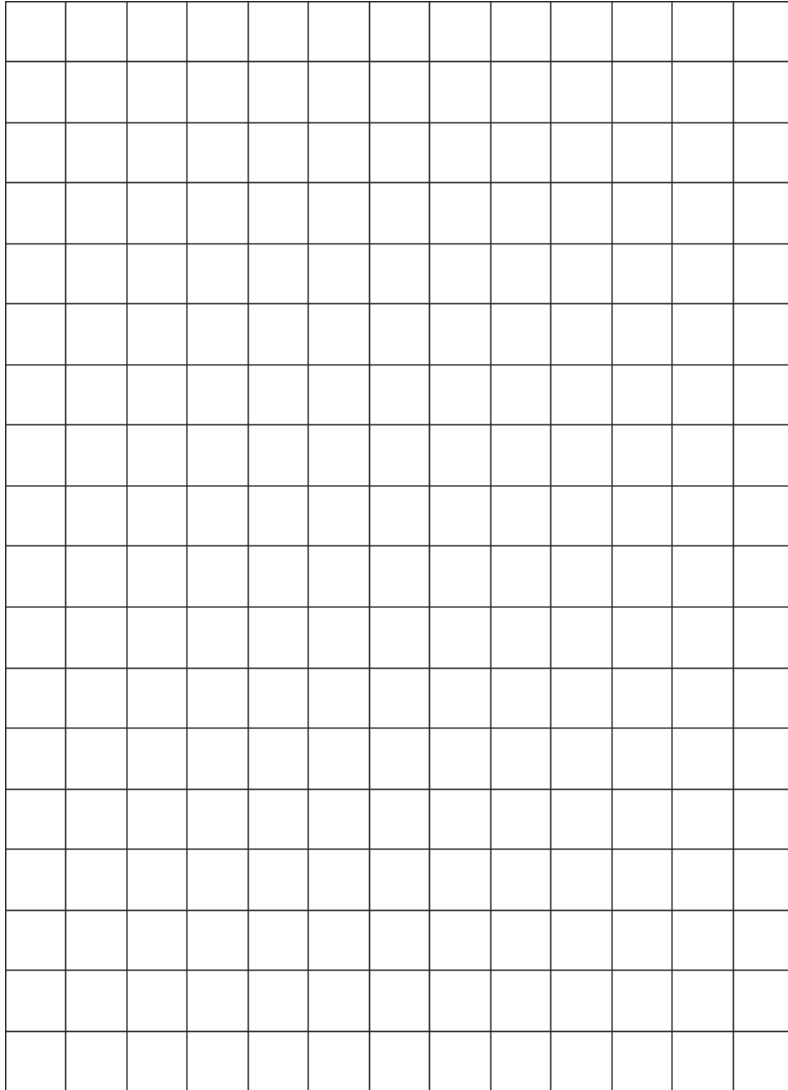
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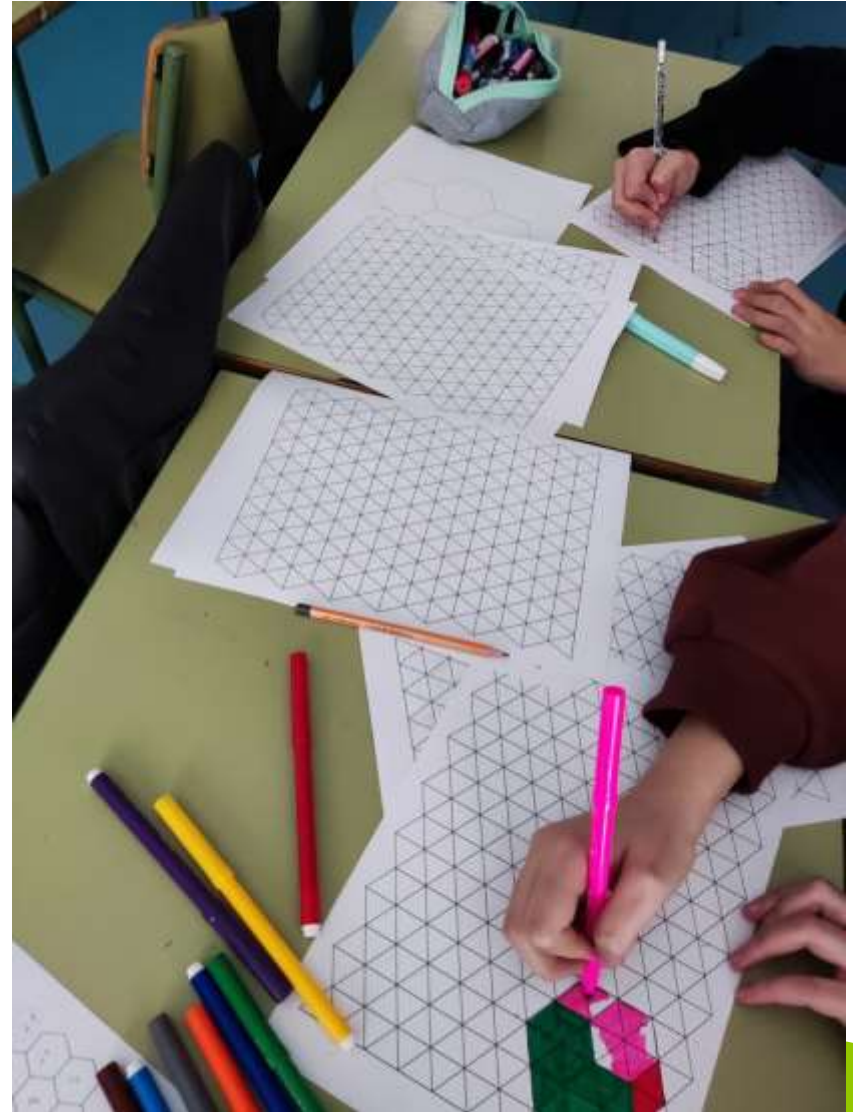
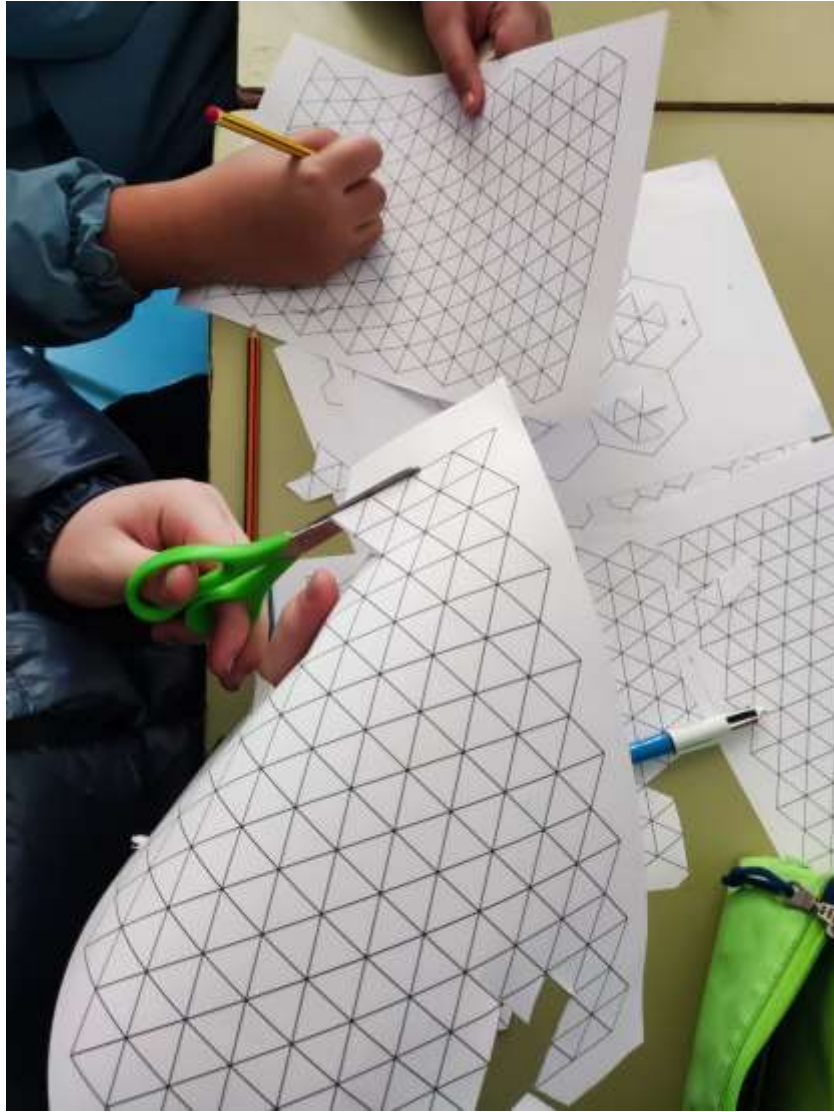


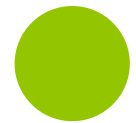
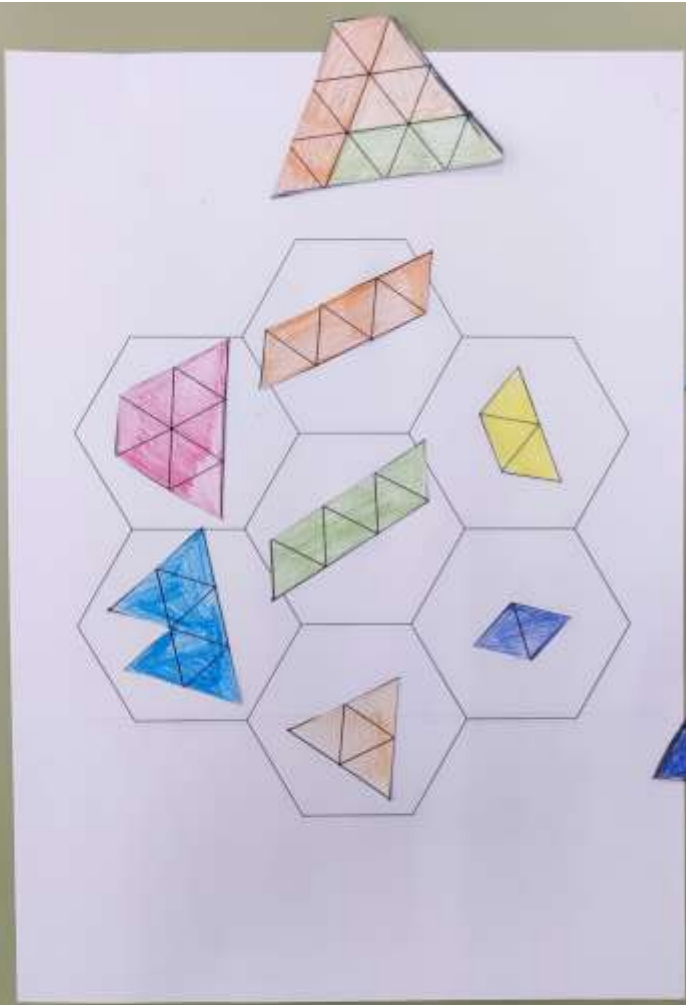
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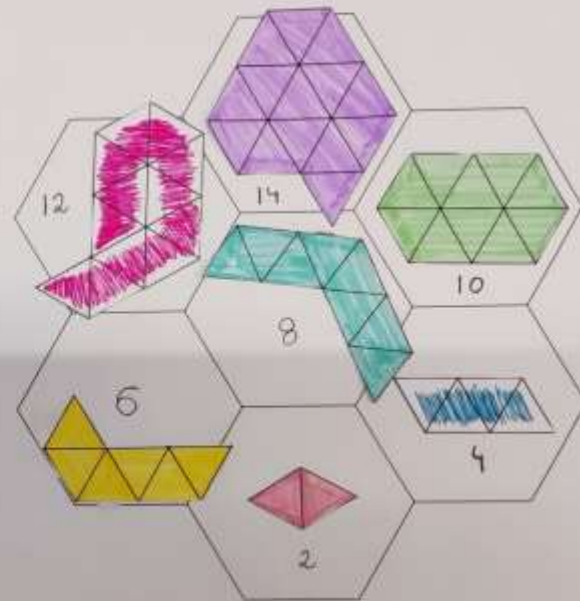
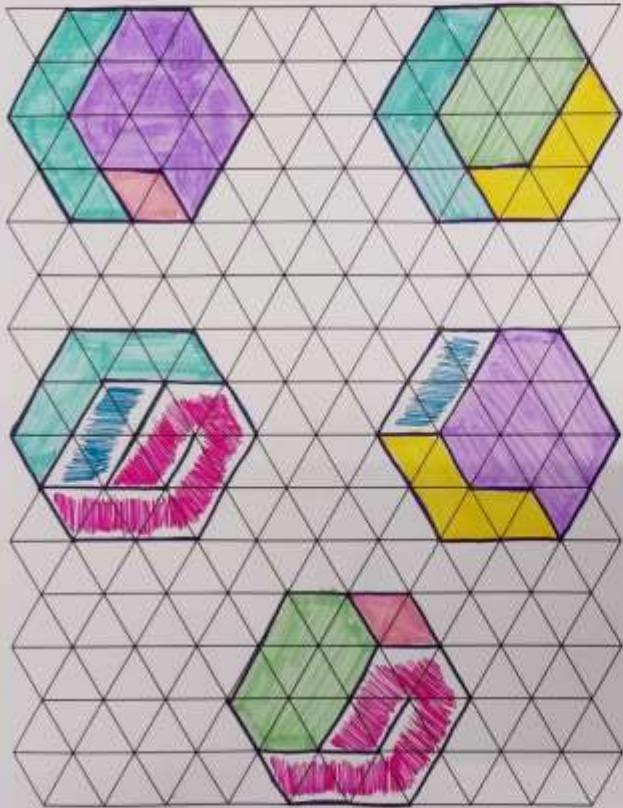


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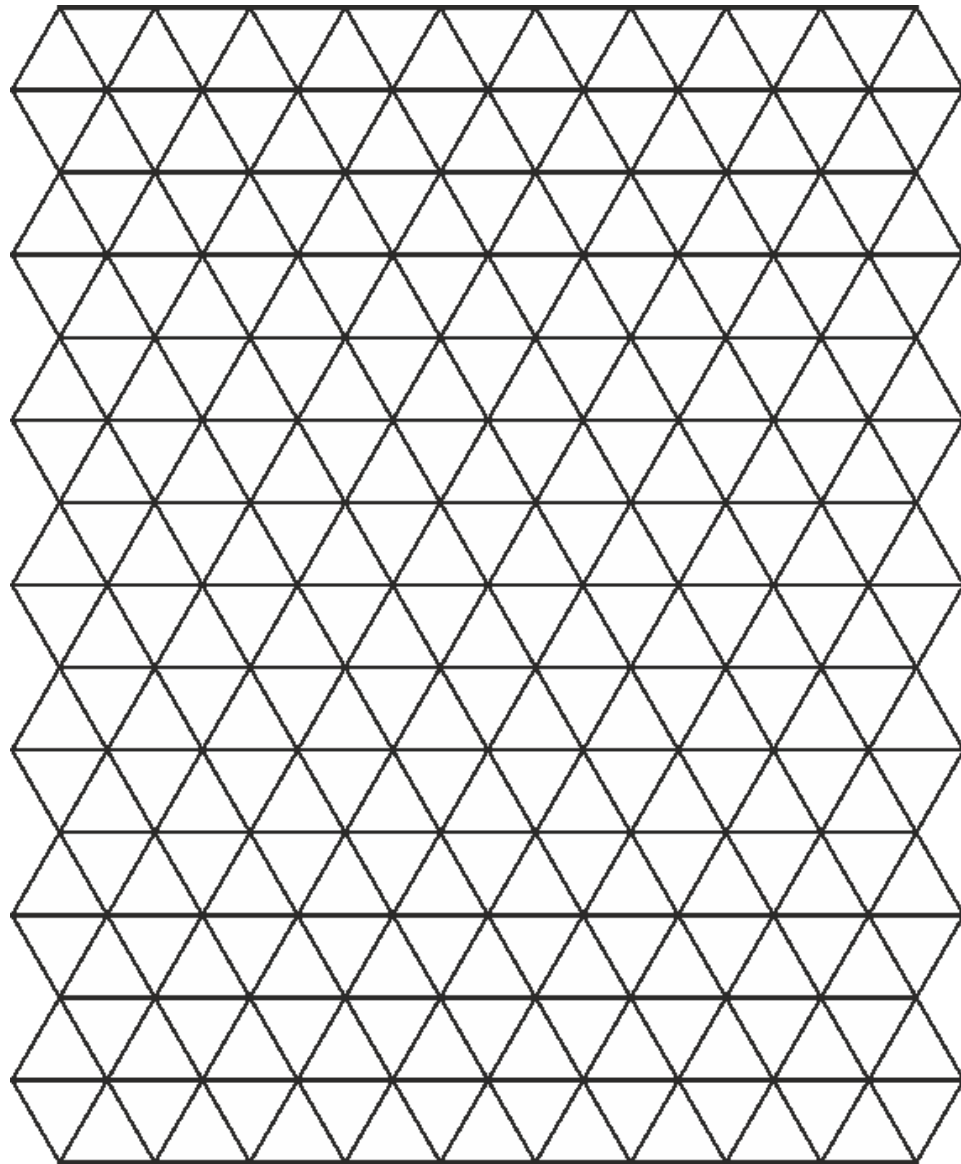


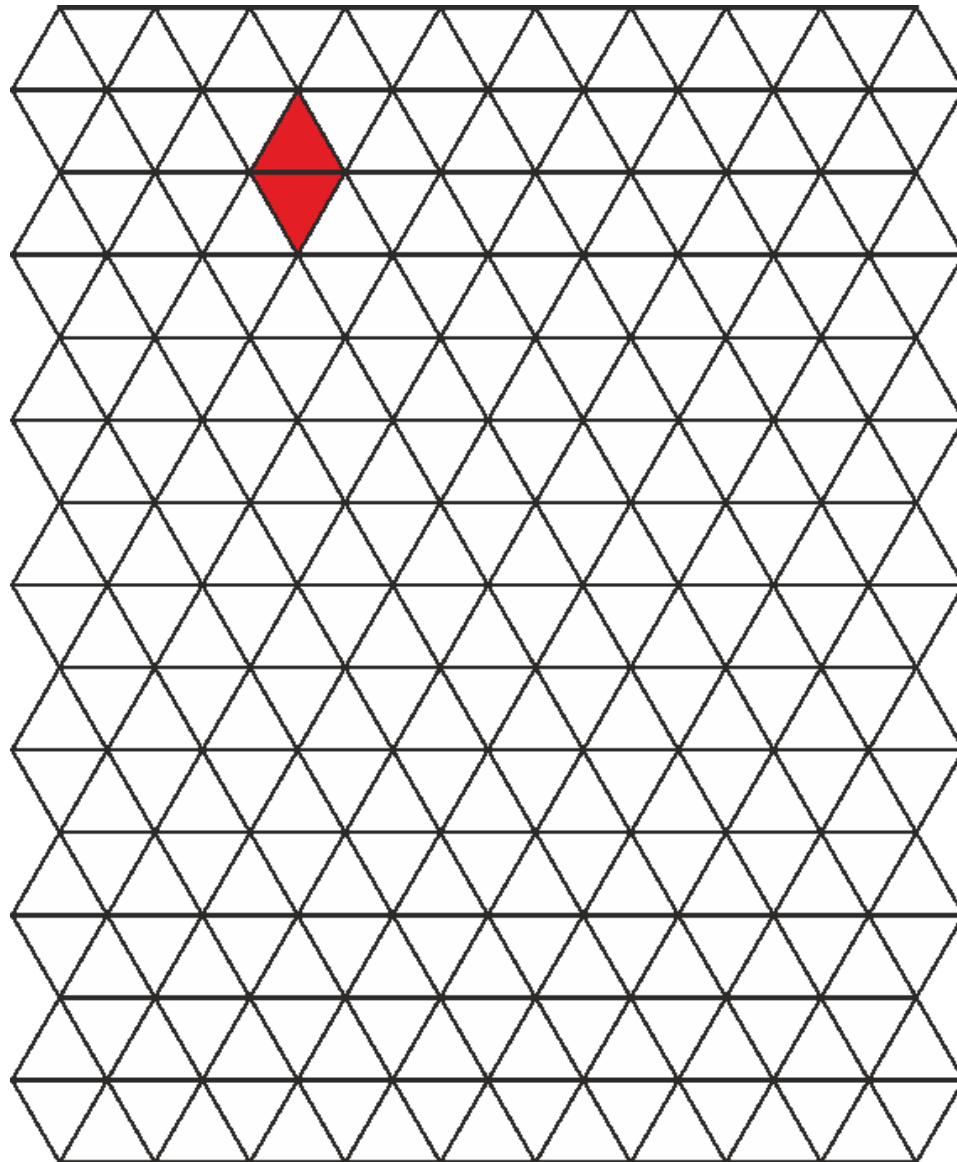


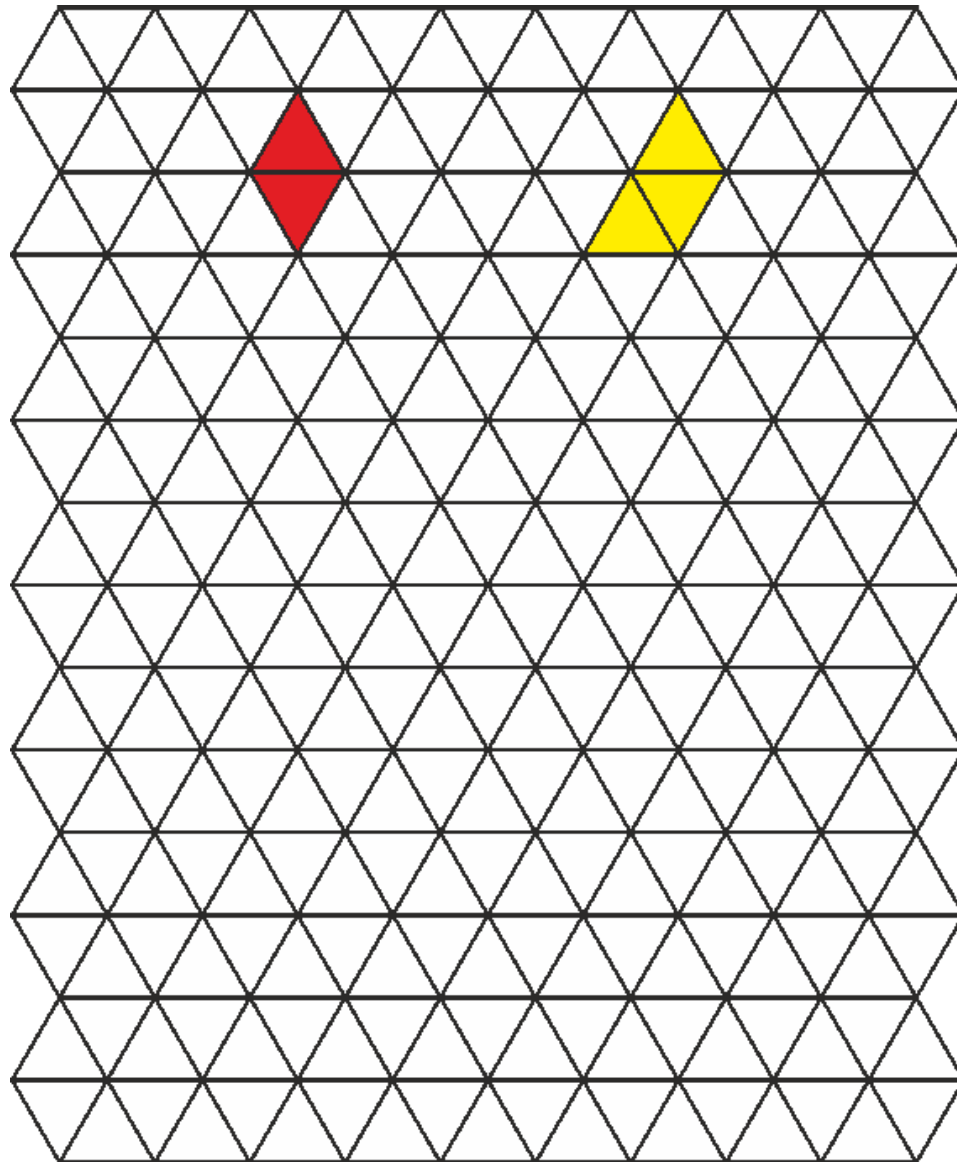


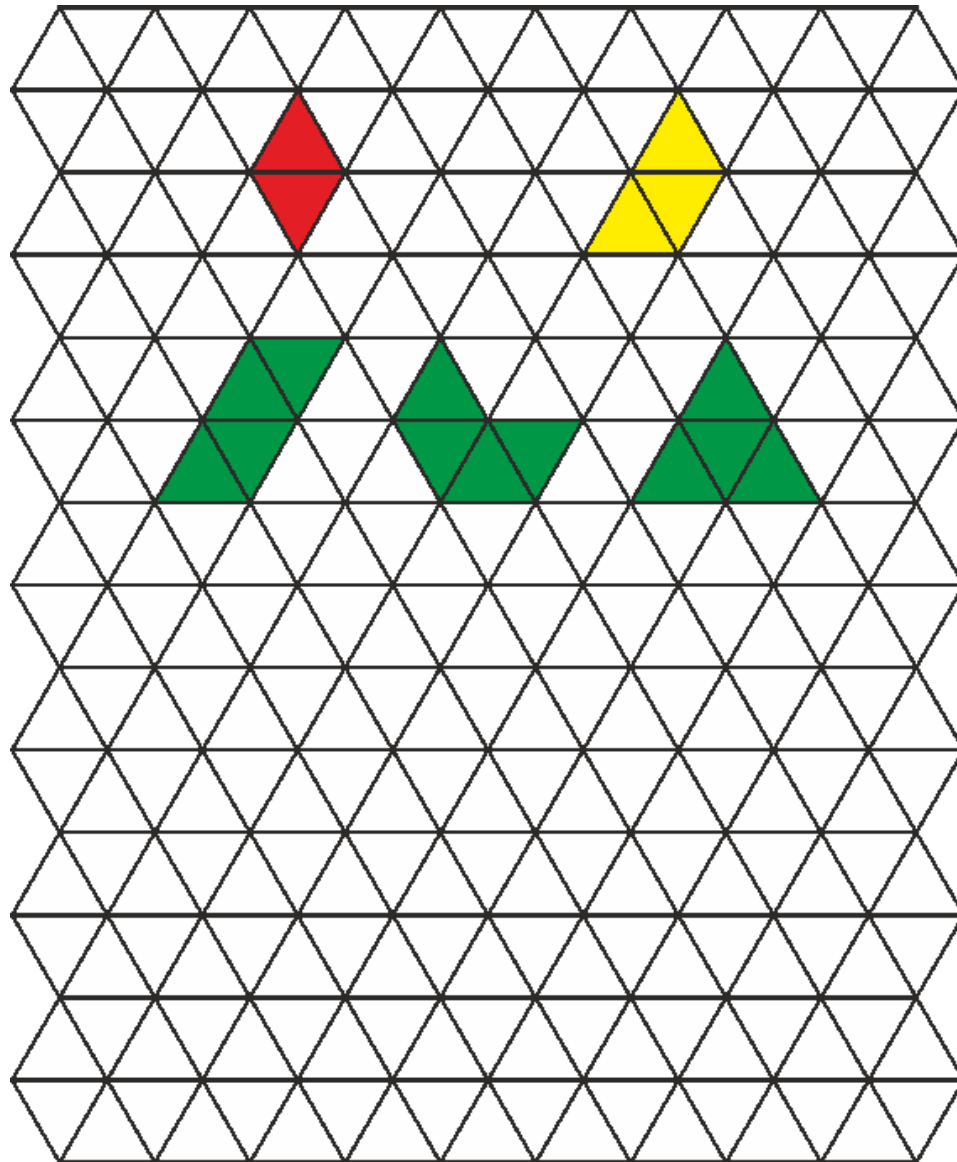


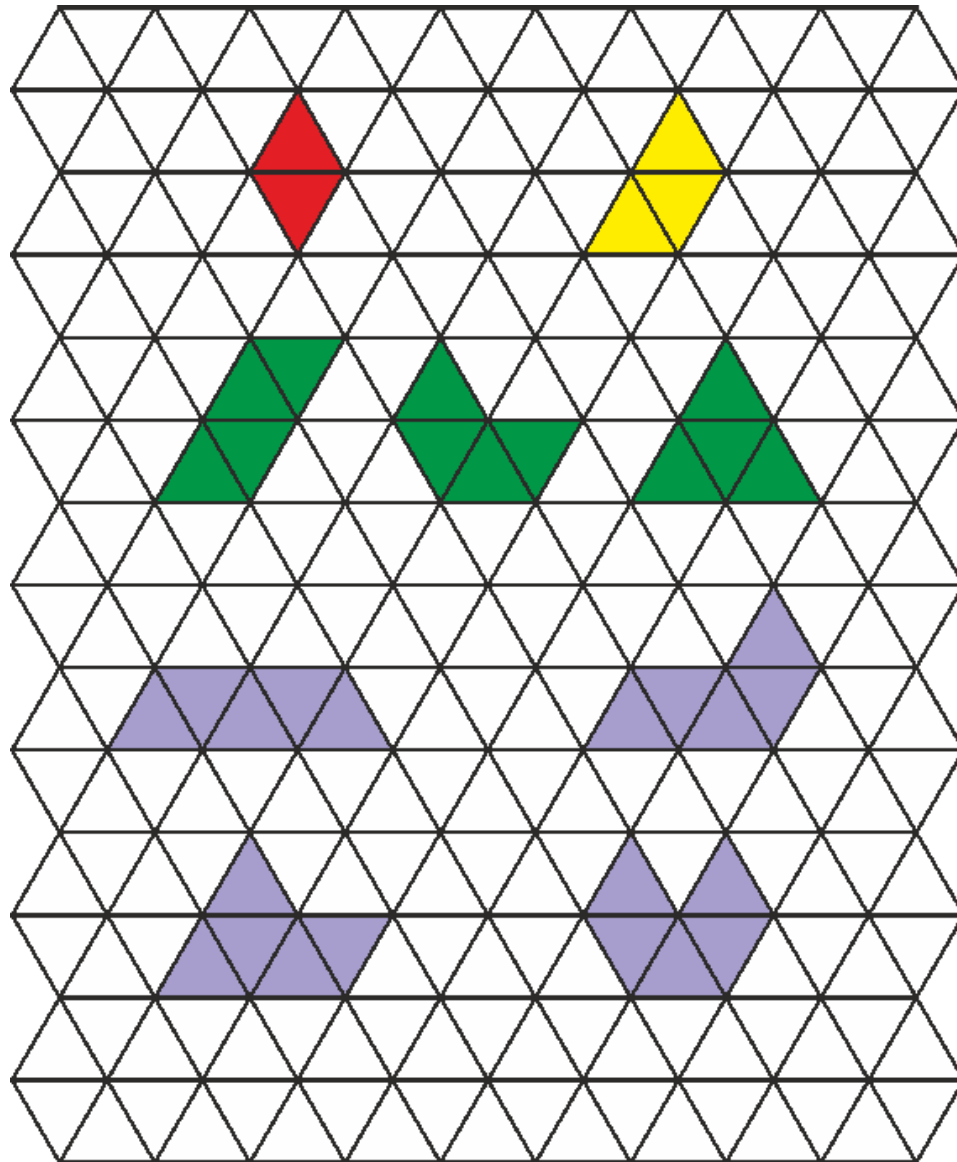


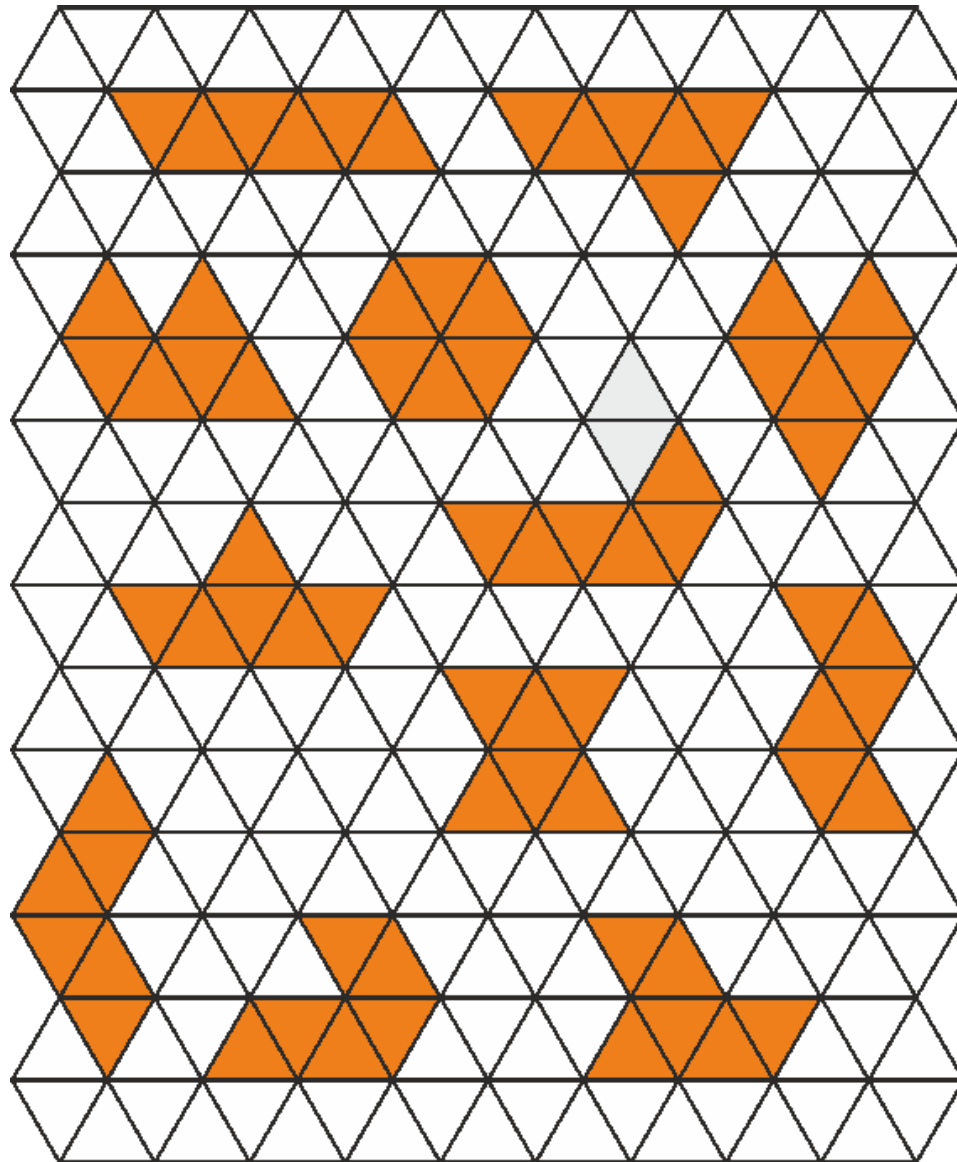














paral·lelogram



esfinx



rat penat



cor



iot



pal de golf



vaixell



hexàgon



pistola



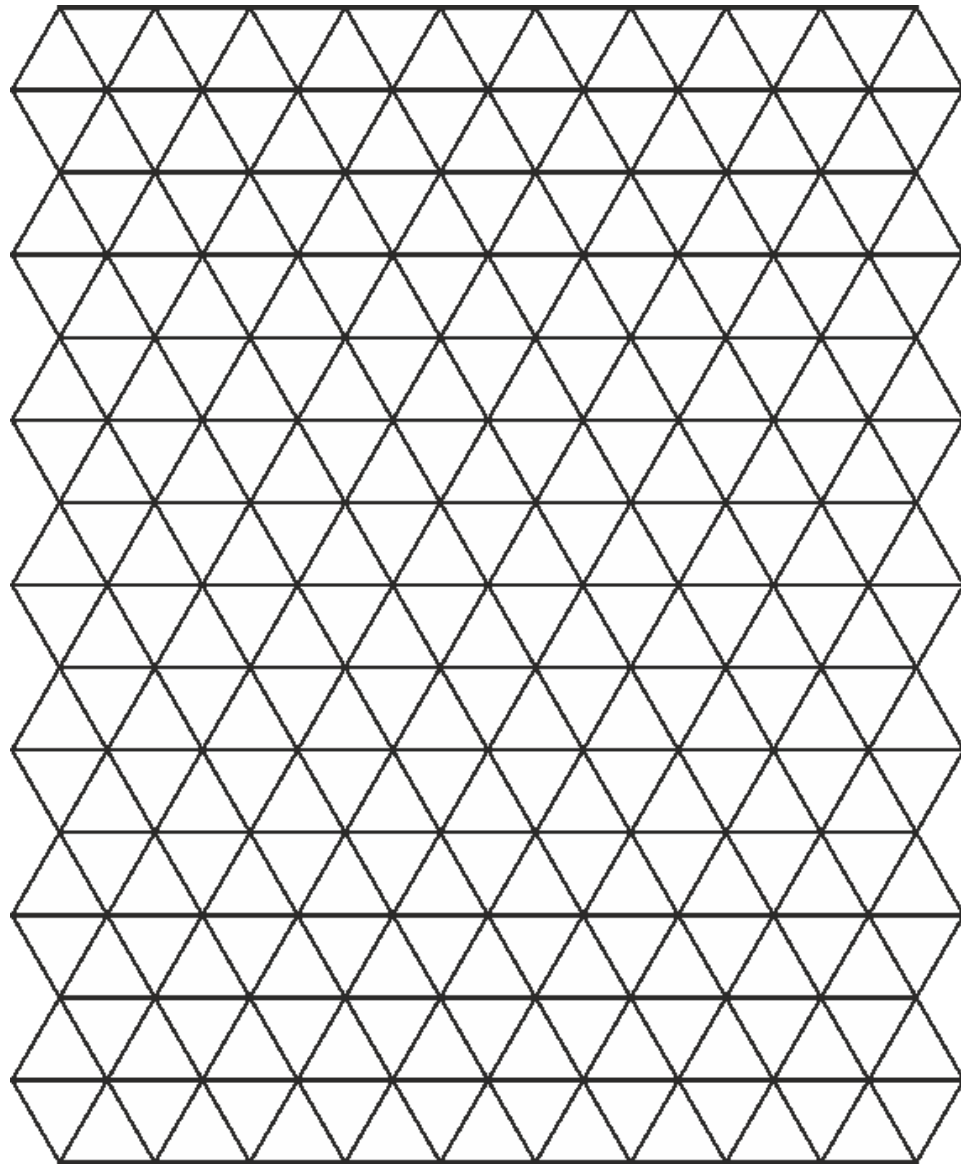
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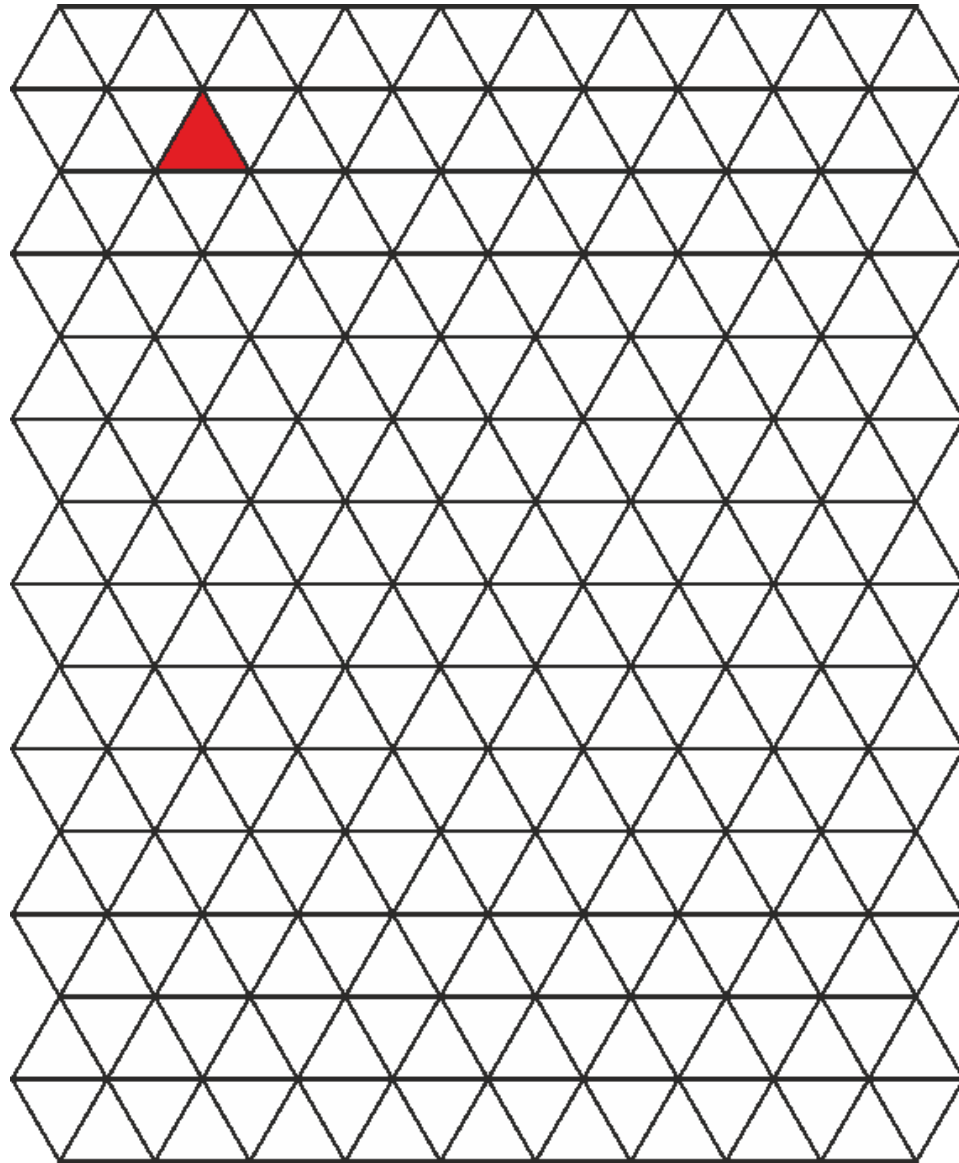
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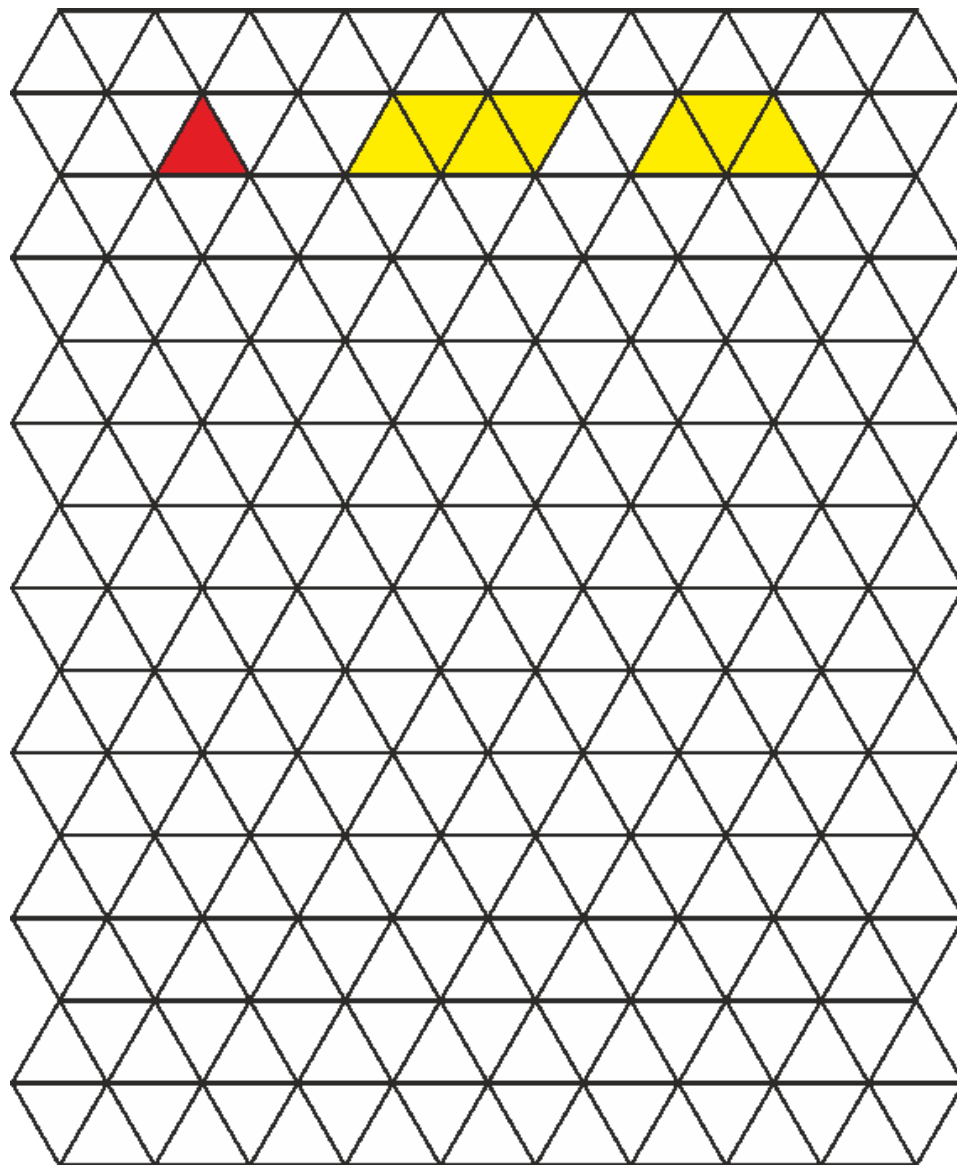


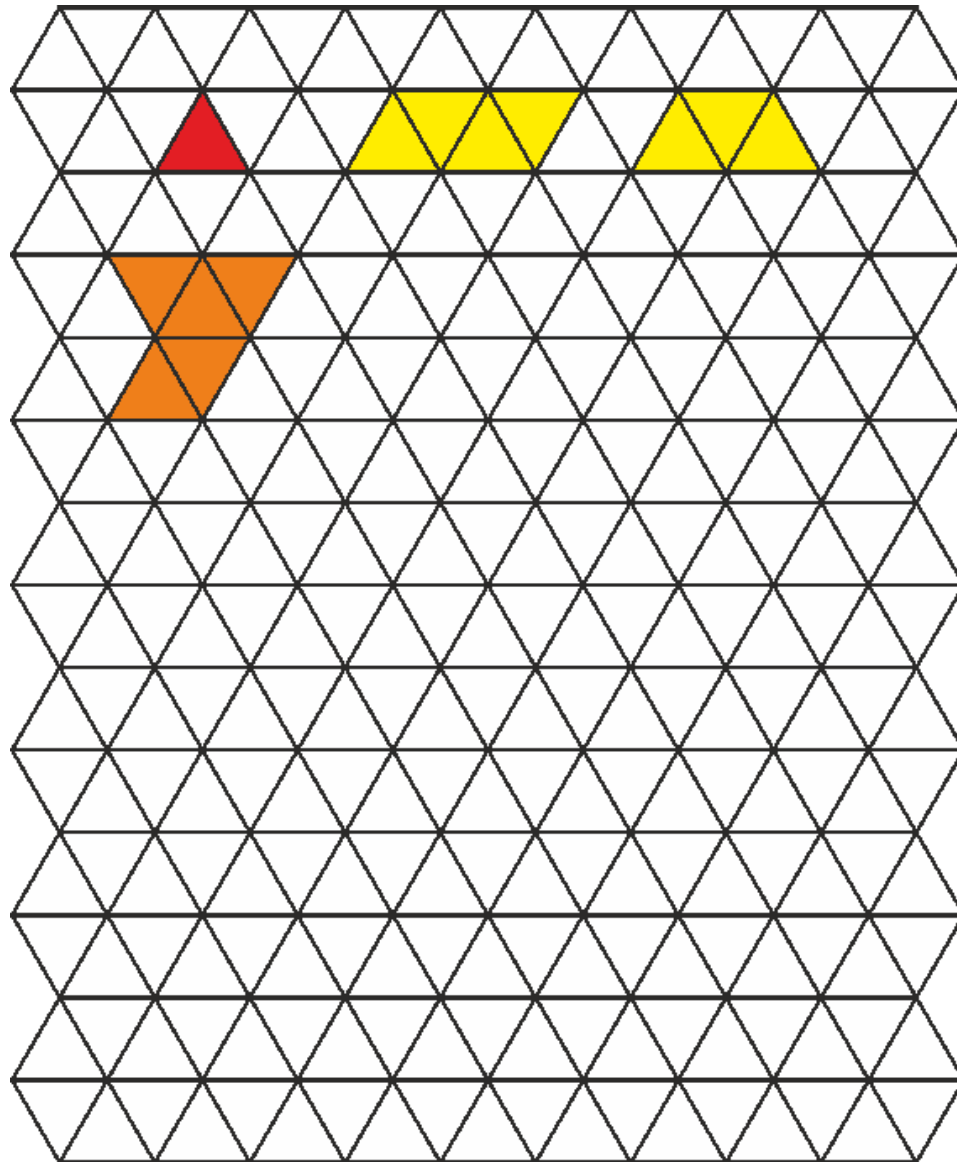
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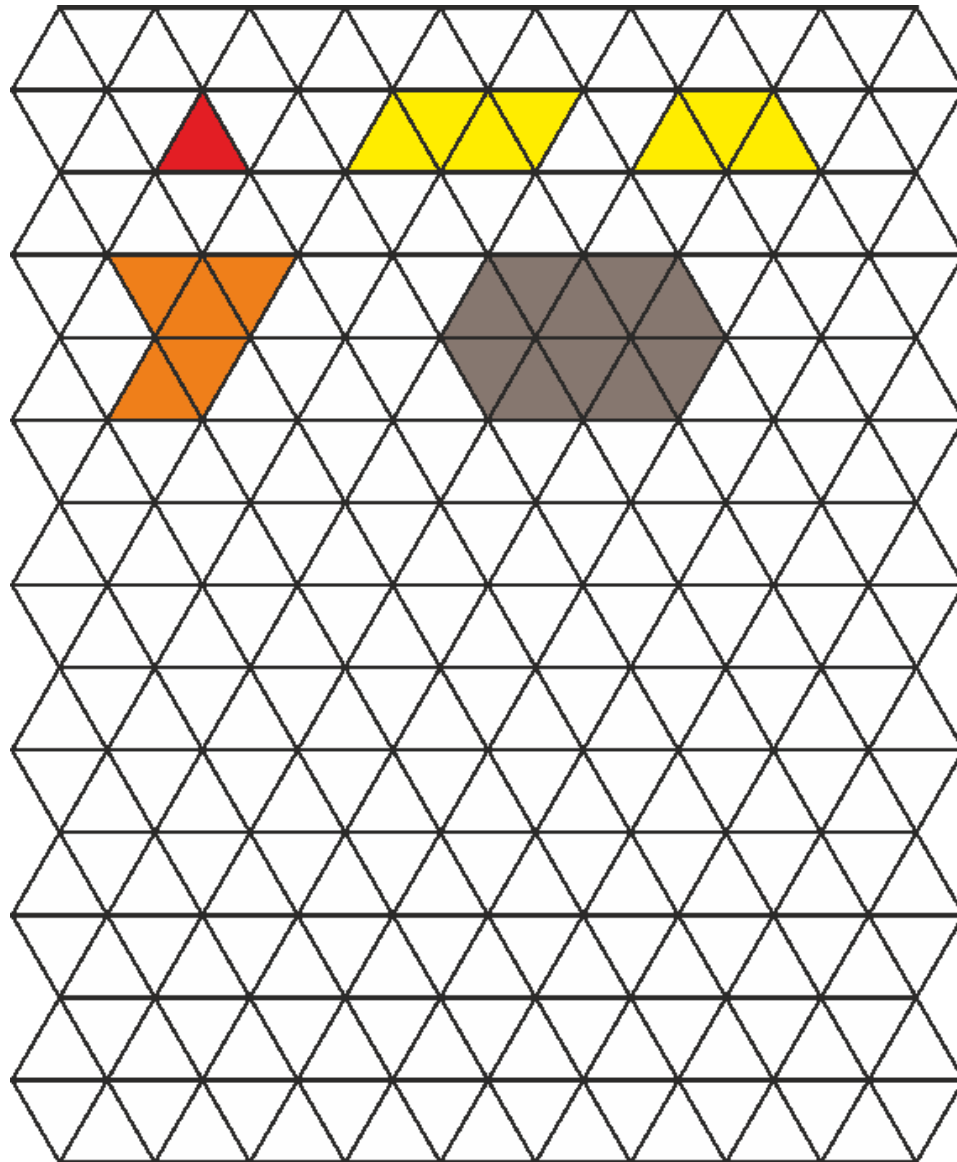


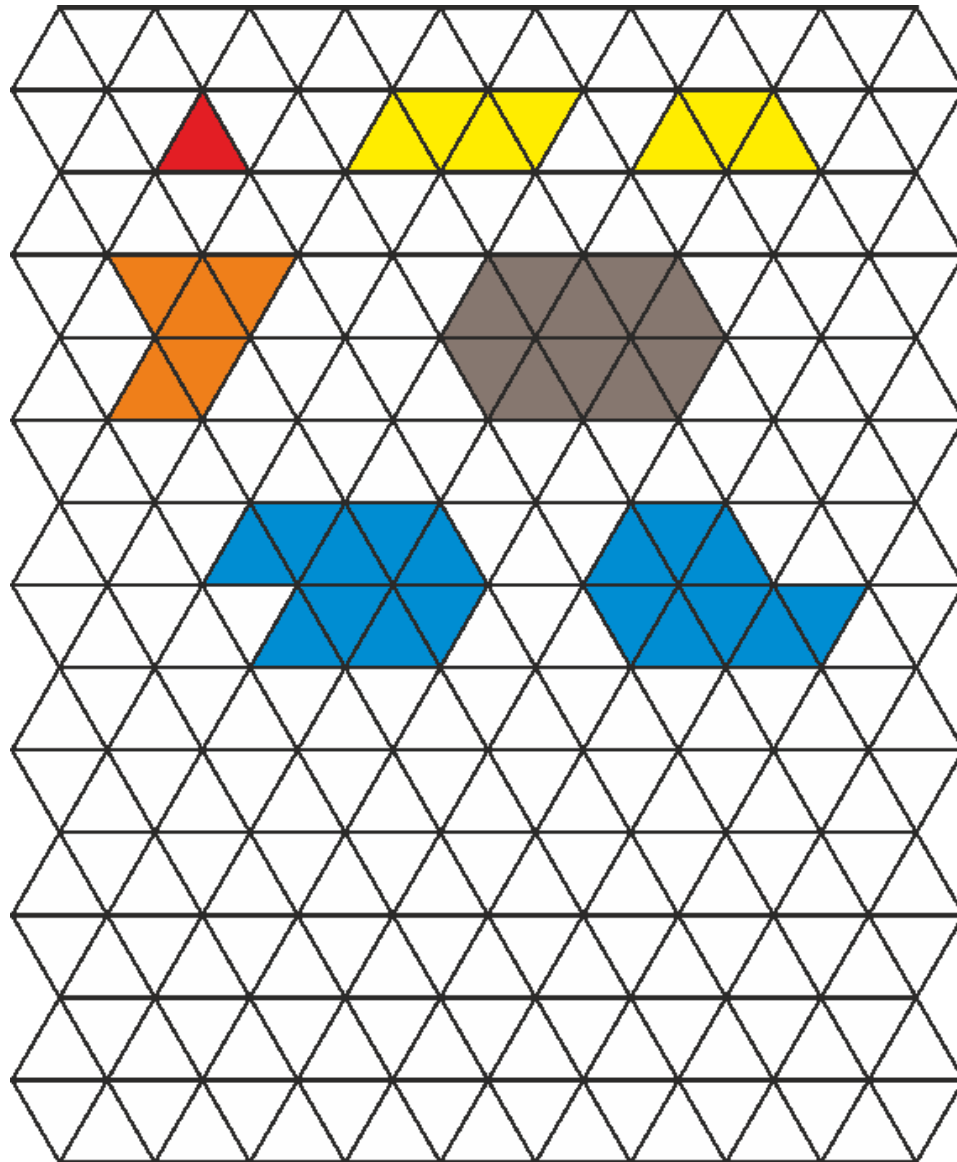


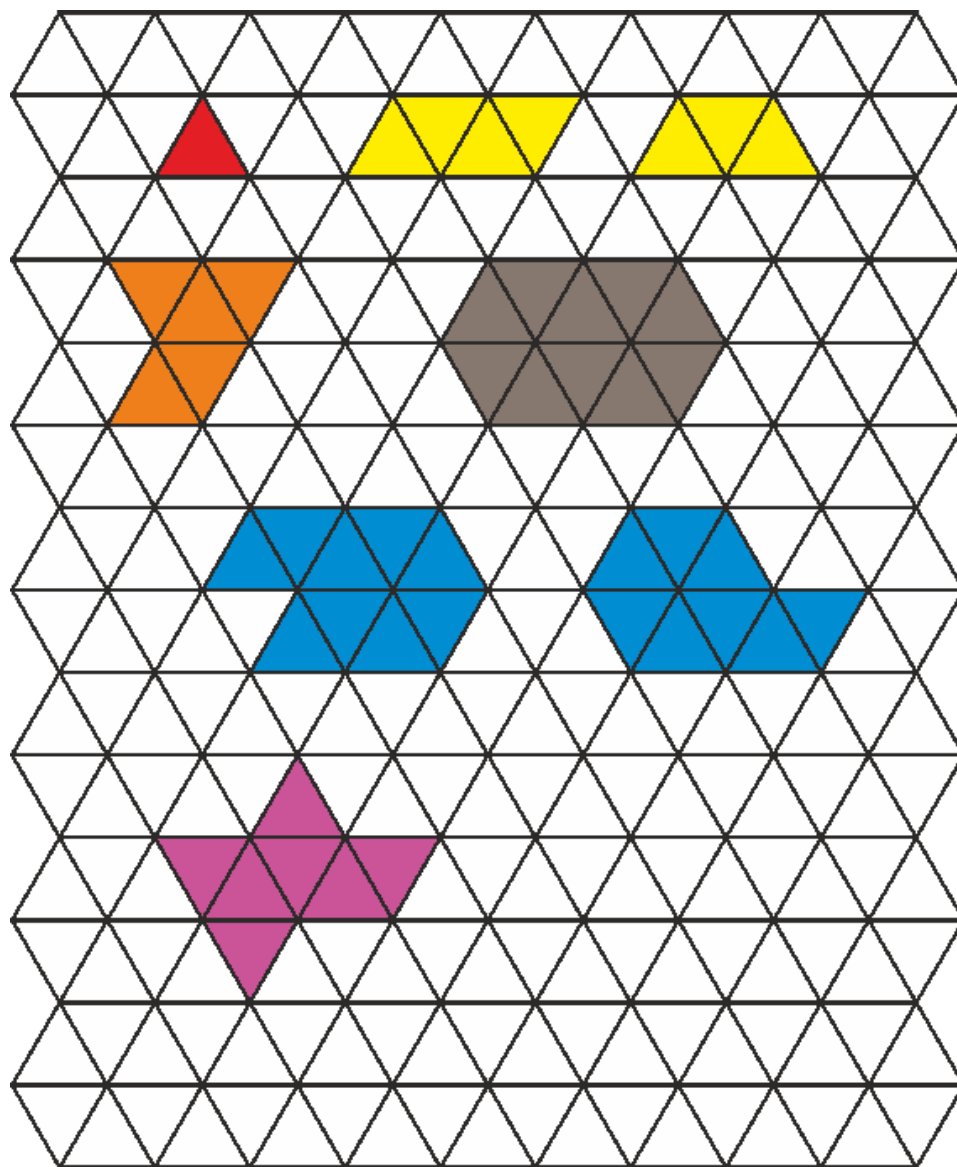


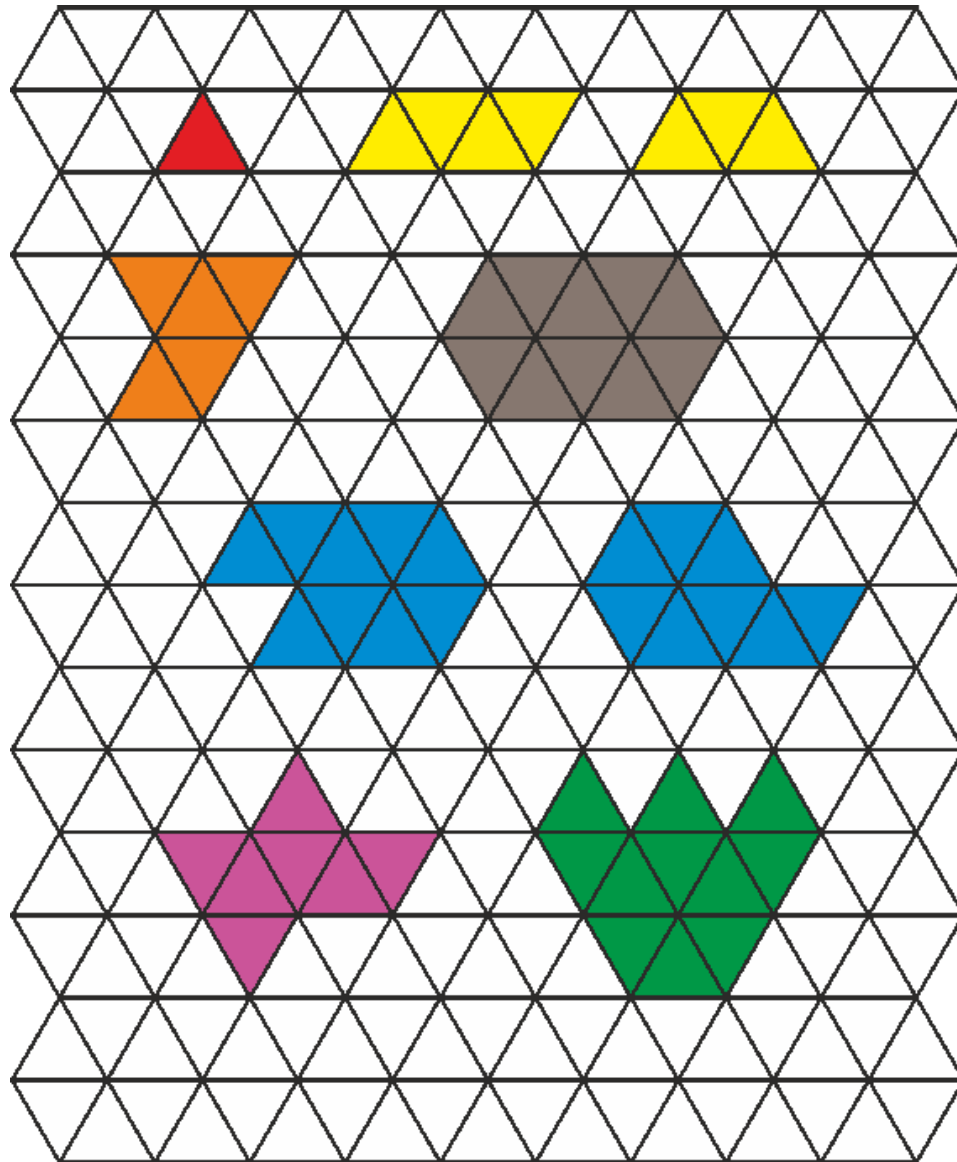










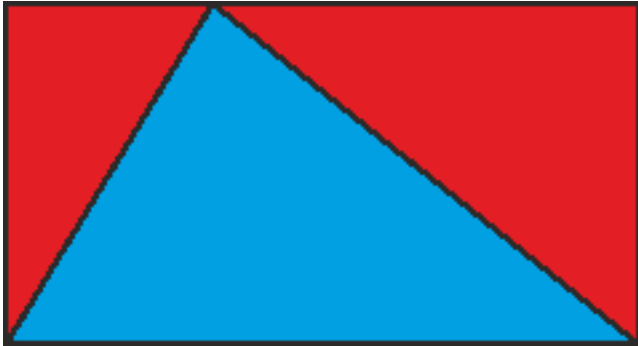


$$A (\text{ triangle } ) = 1/2 A (\text{ Rectangle } )$$

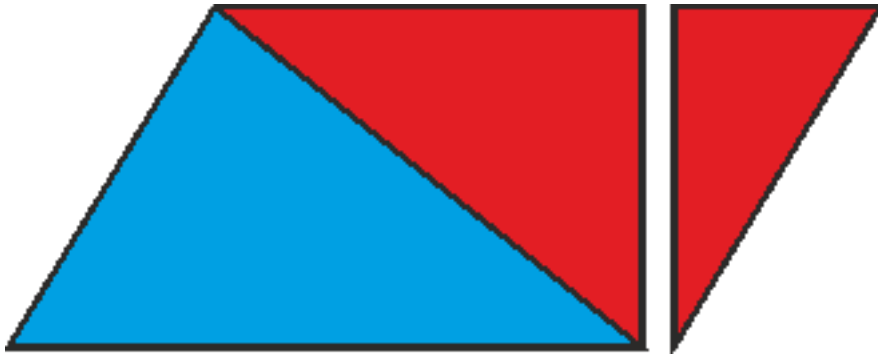




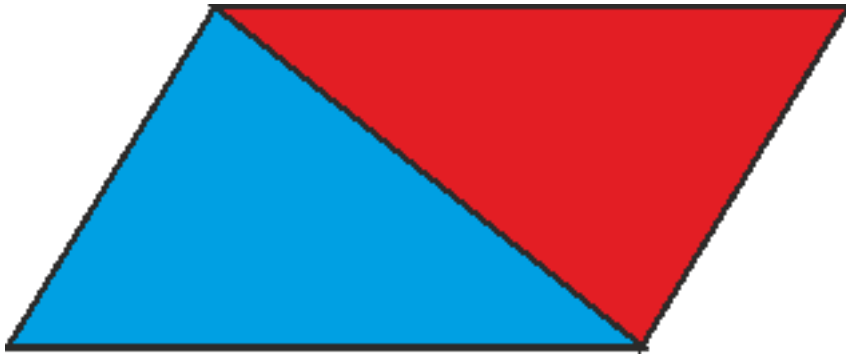
$$A (\text{ triangle } ) = 1/2 A (\text{ Rectangle } )$$



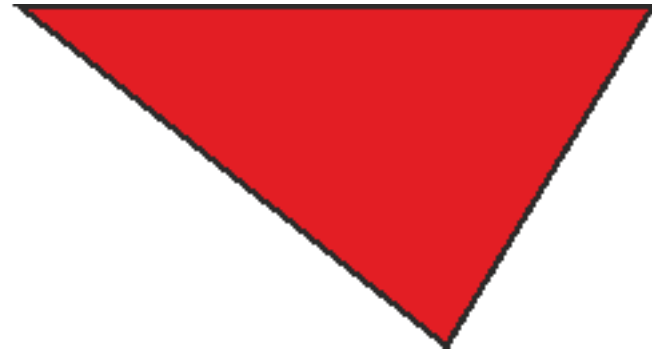
$$A (\text{ triangle } ) = 1/2 A (\text{ Rectangle } )$$



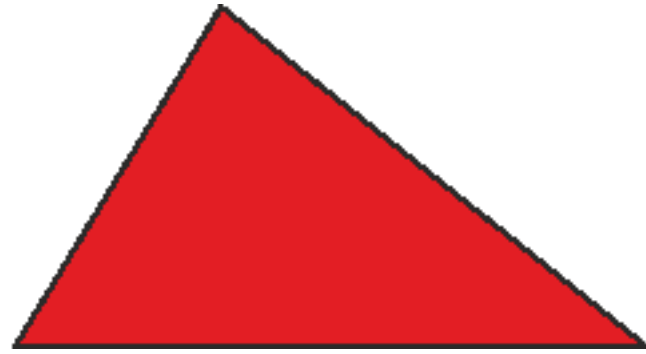
$$A (\text{ triangle } ) = 1/2 A (\text{ Rectangle } )$$



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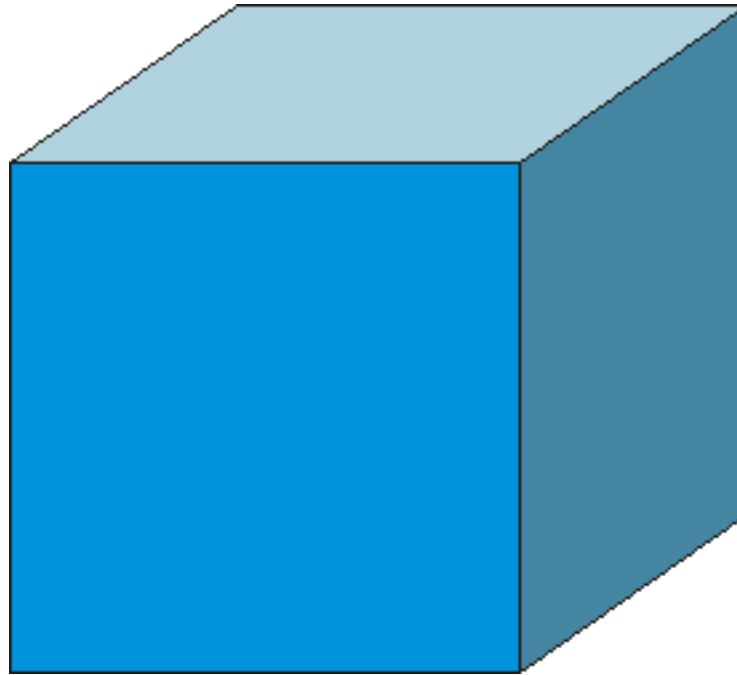



$$V (\text{ Piràmide } ) = 1/3 V (\text{ Prisma } )$$

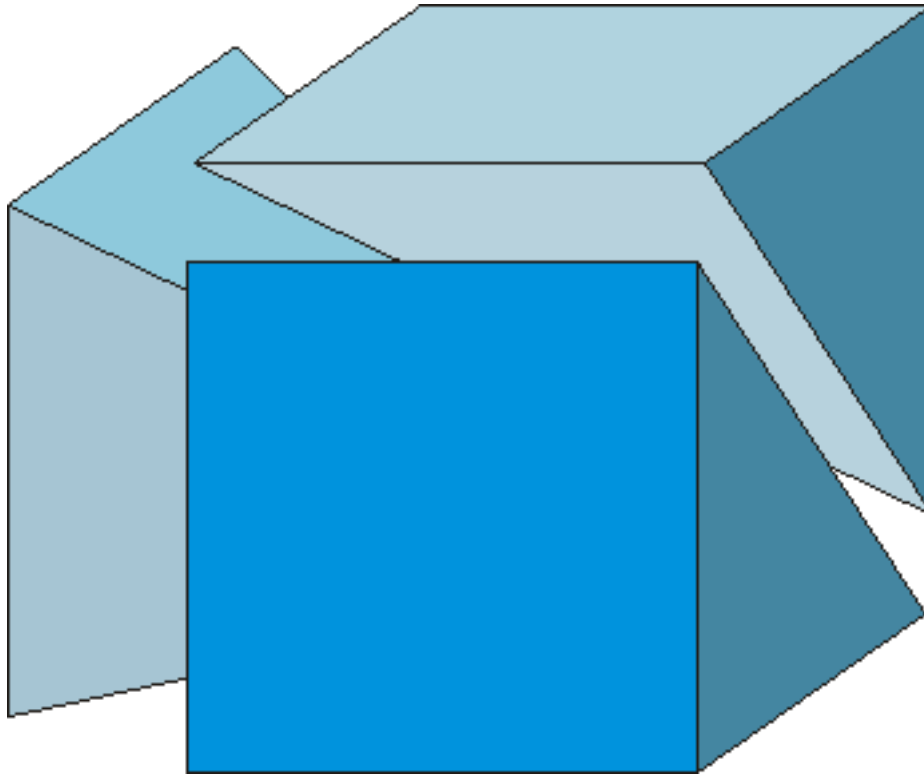
**Resposta alumne:**

$$V (\text{ Piràmide } ) = 1/2 V (\text{ Prisma } )$$

$$V (\text{Piràmide}) = 1/3 V (\text{Prisma})$$

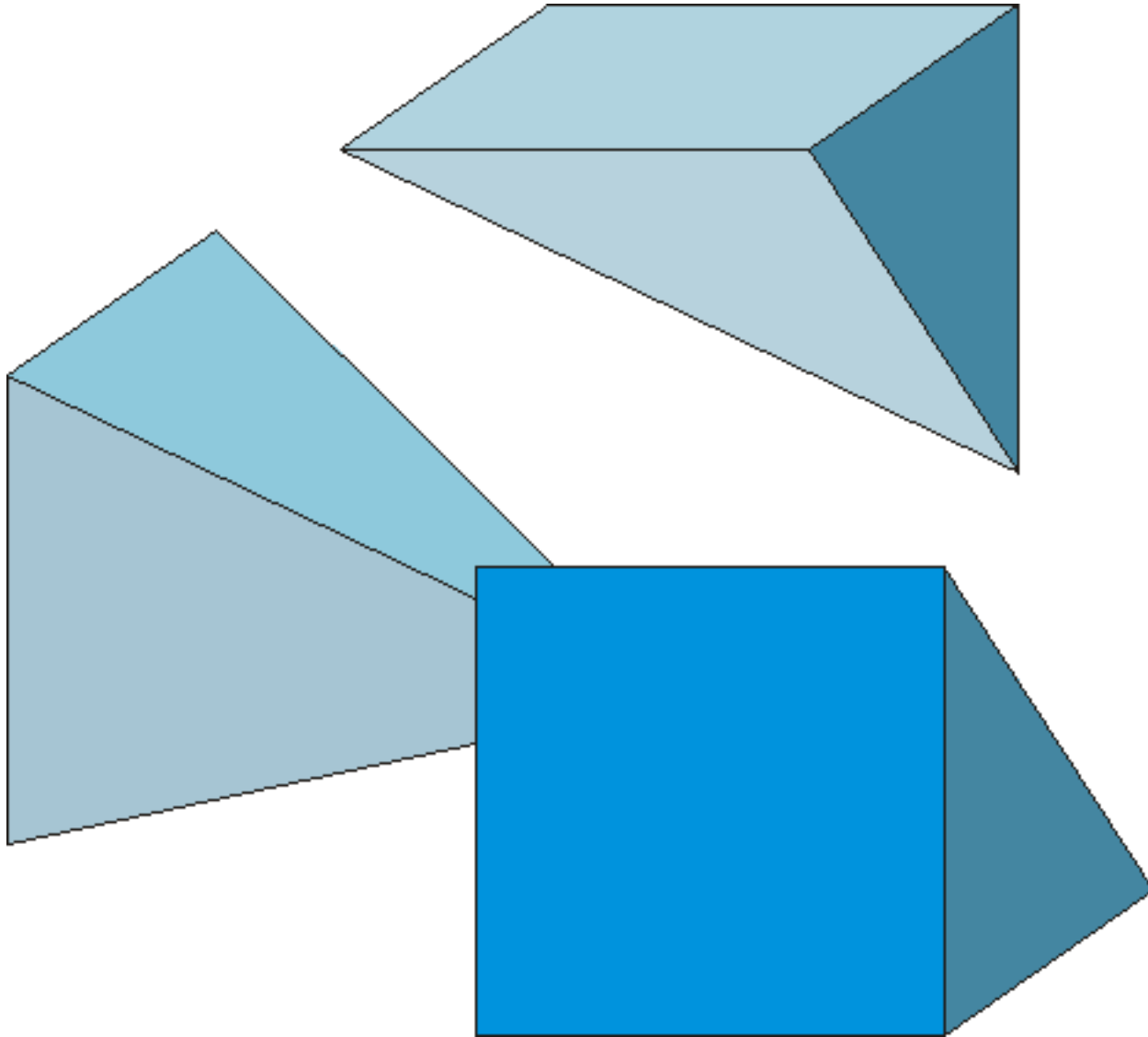


$$V (\text{Piràmide}) = 1/3 V (\text{Prisma})$$





$$V (\text{Piràmide}) = 1/3 V (\text{Prisma})$$

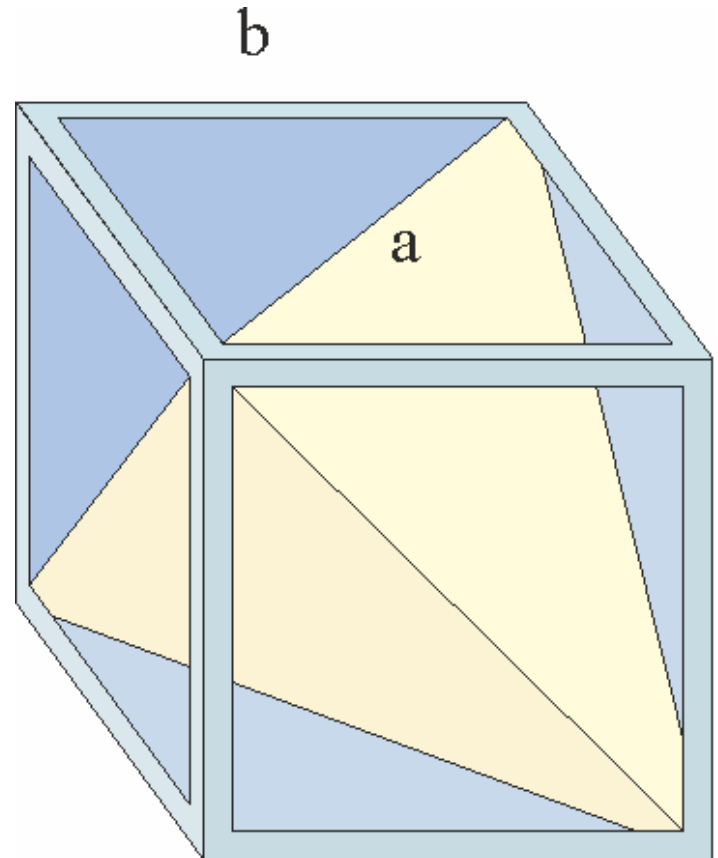


# Volum del tetraedre

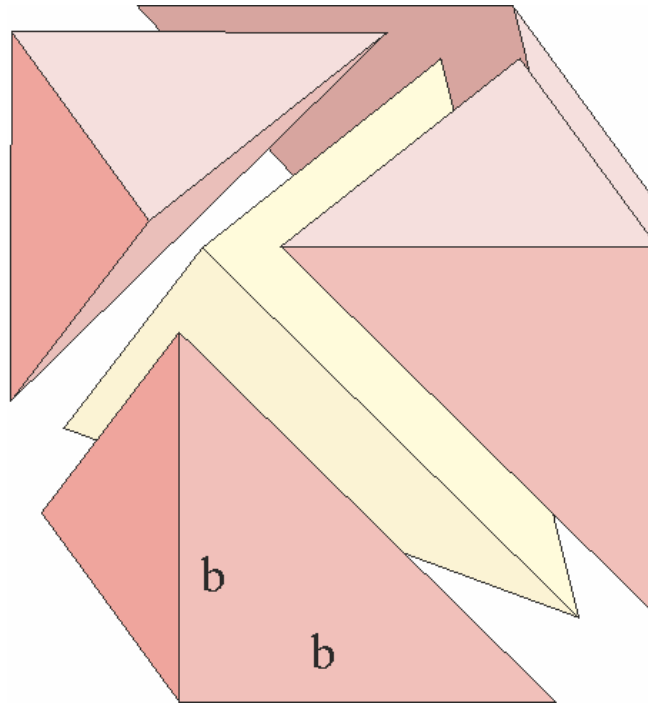
Aresta del tetraedre =  $a$

Aresta del cub =  $b$

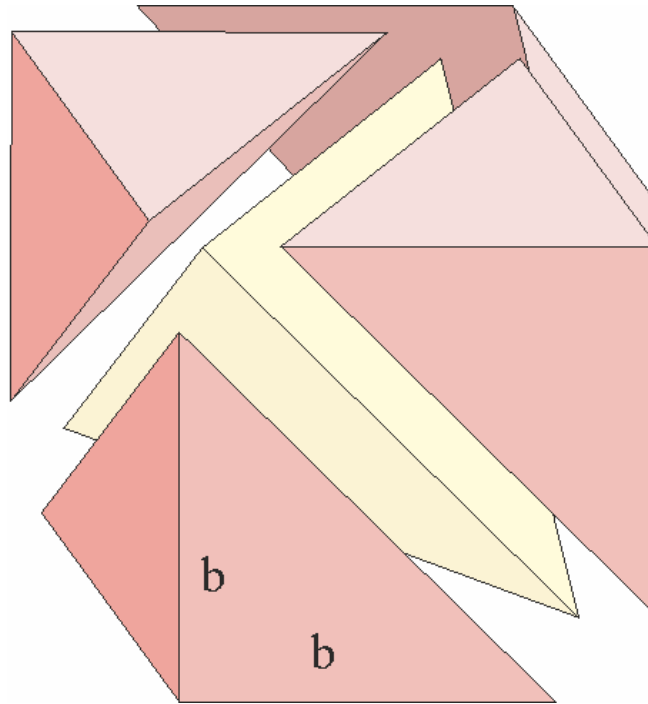
$$a/b = \sqrt{2}$$



# Volum del tetraedre

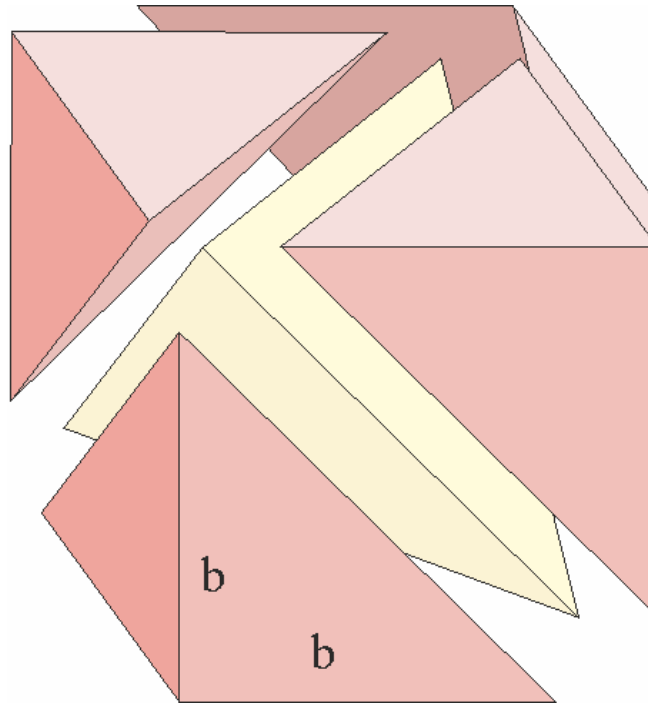


# Volum del tetraedre



$$V(\text{Cub}) = 4 V(\text{piràmide roja}) + V(\text{tetraedre})$$

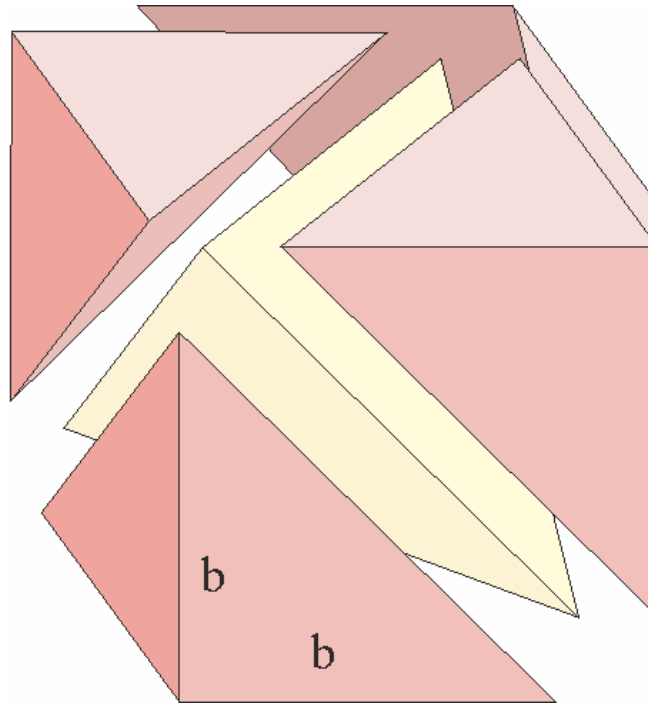
# Volum del tetraedre



$$V(\text{Cub}) = 4 V(\text{piràmide roja}) + V(\text{tetraedre})$$

$$V(\text{tetraedre}) = V(\text{Cub}) - 4 V(\text{piràmide roja})$$

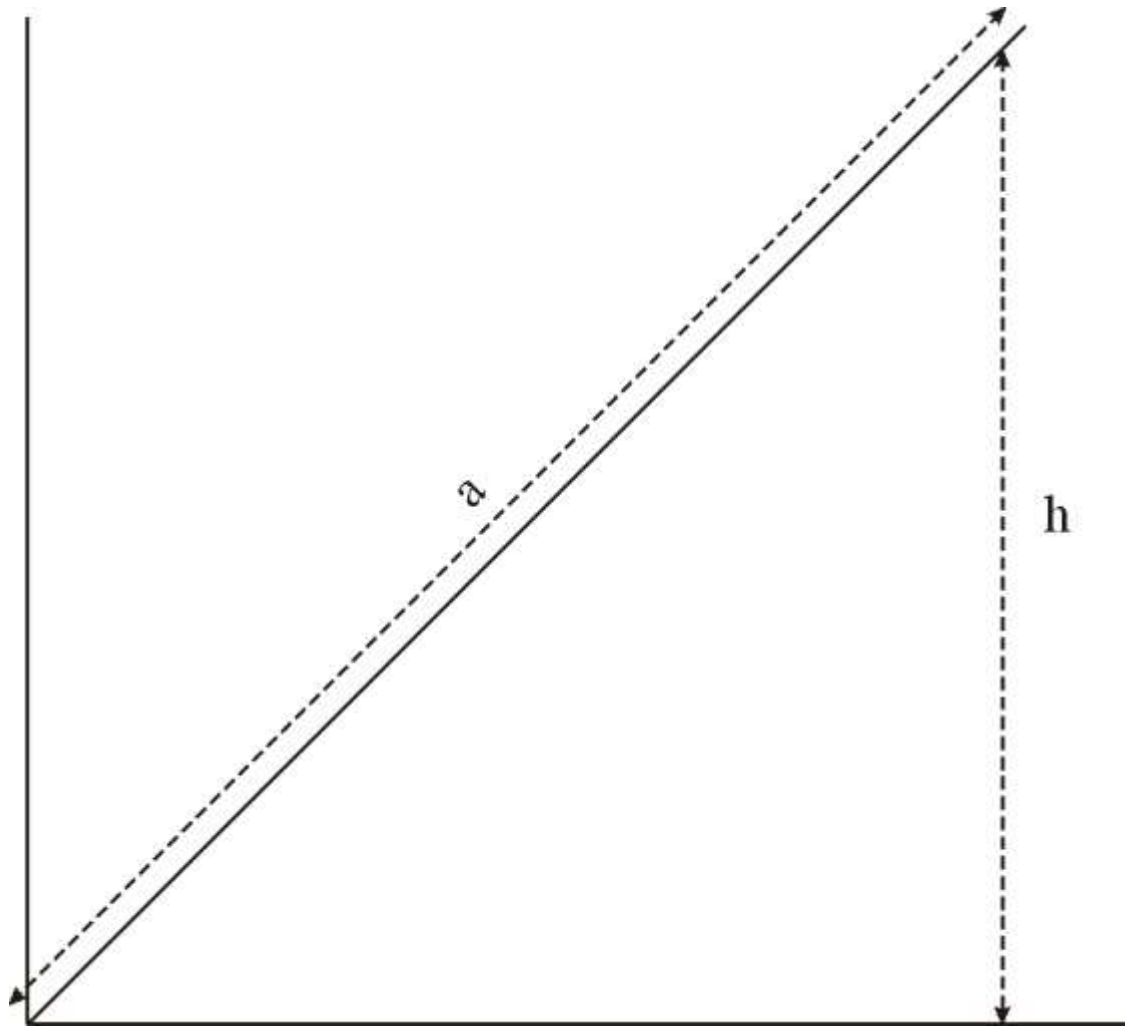
# Volum del tetraedre



$$V(\text{piràmide roja}) = \frac{Ab \cdot h}{3} = \frac{b^3}{6} = \frac{V(\text{cub})}{6}$$

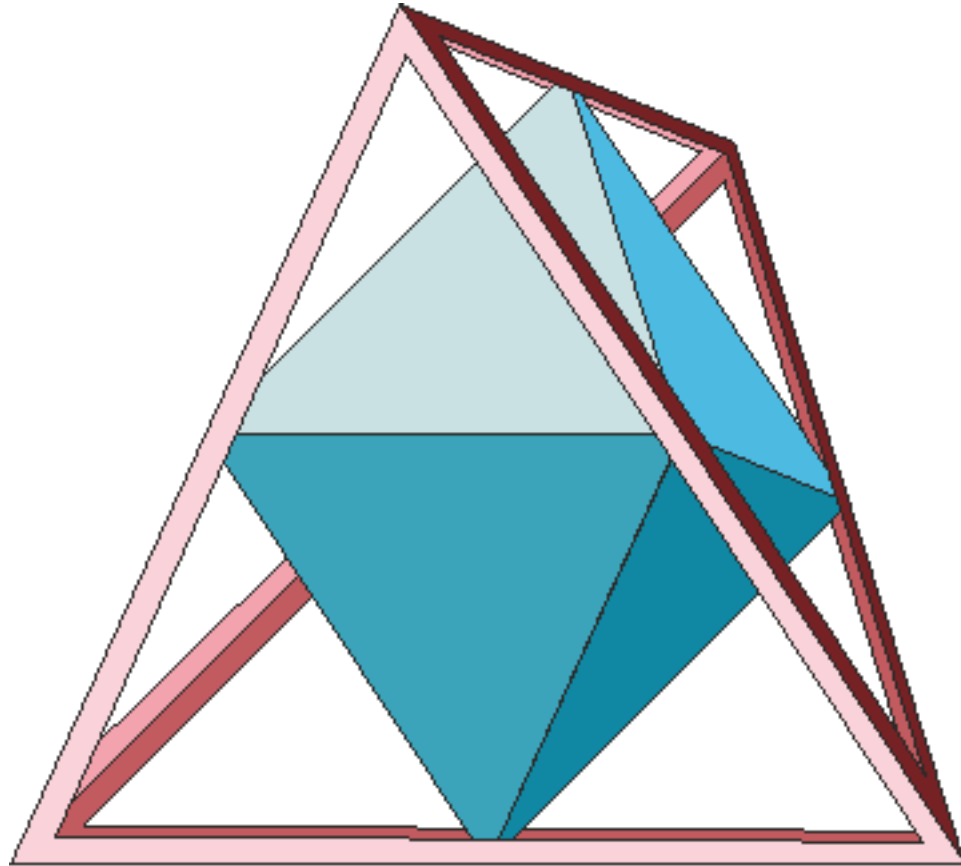
$$V(\text{tetraedre}) = \left(1 - \frac{4}{6}\right) V(\text{cub}) = \frac{b^3}{3} = \frac{a^3}{3 \cdot (\sqrt{2})^3} = \frac{\sqrt{2}}{12} \cdot a^3$$

# APROXIMACIÓ DEL VOLUM DEL TETRAEDRE



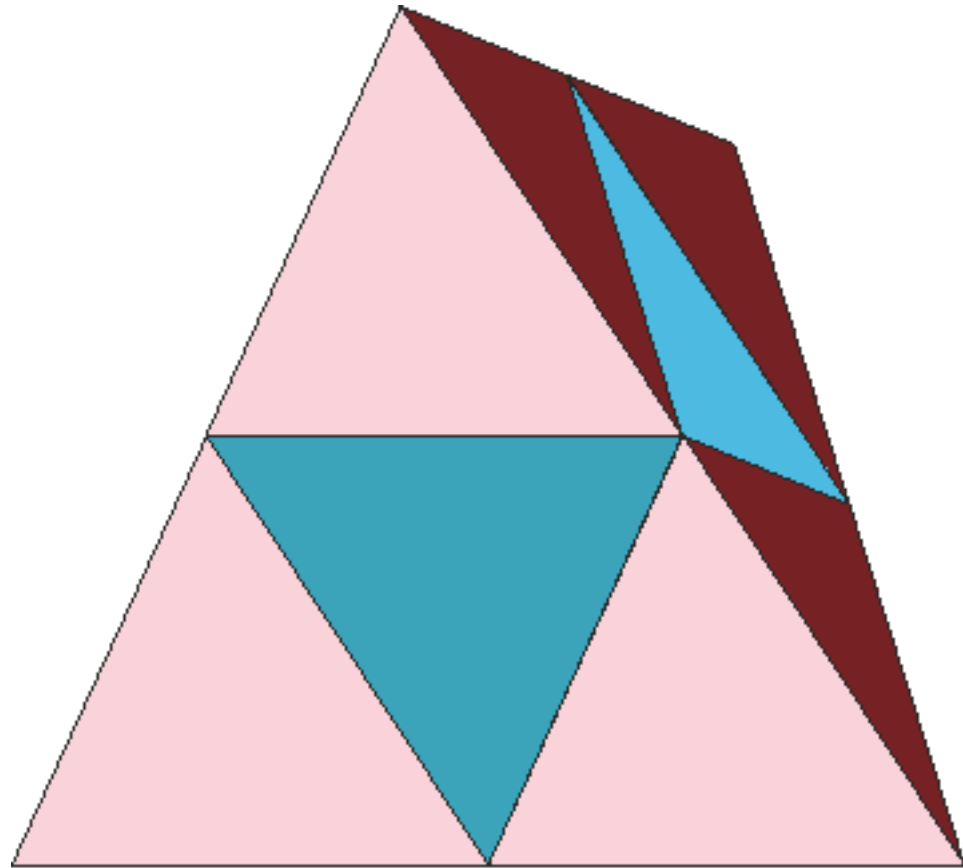
$$V(\text{tetraedre}) = \frac{h^3}{3}$$

# VOLUM DE L'OCTAEDRE

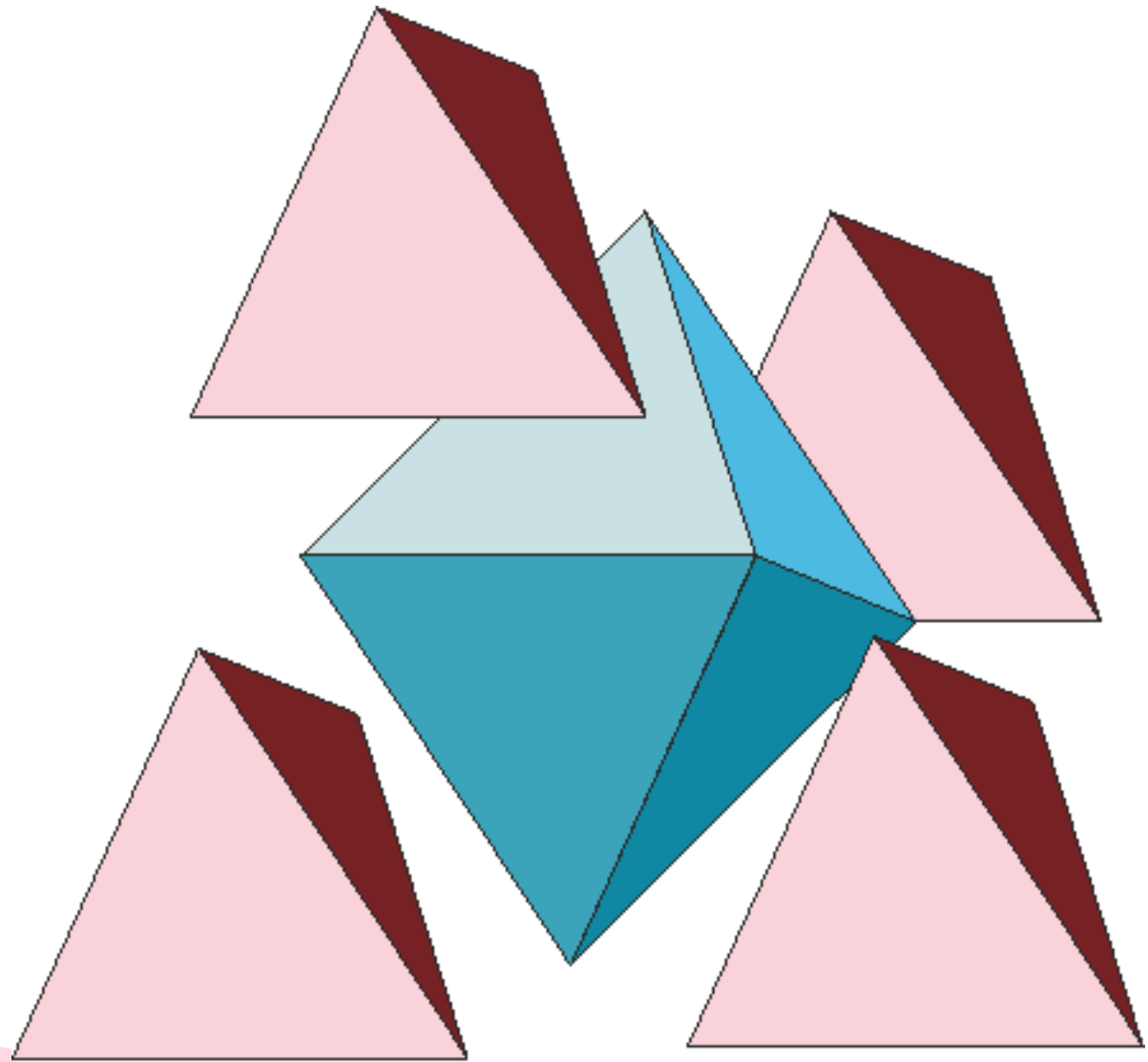




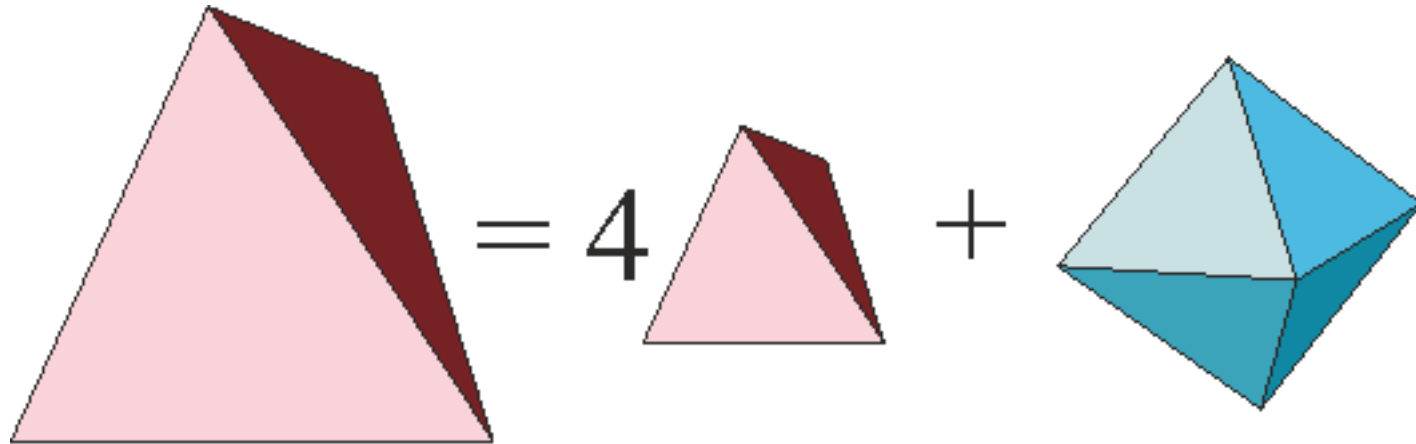
# VOLUM DE L'OCTAEDRE



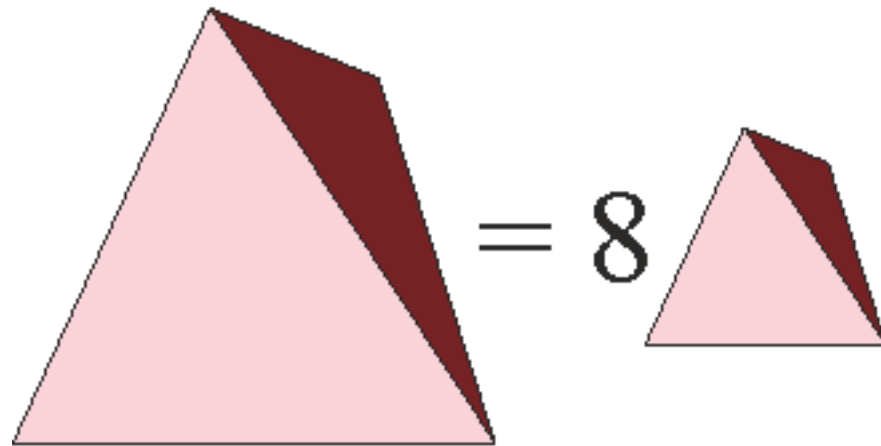
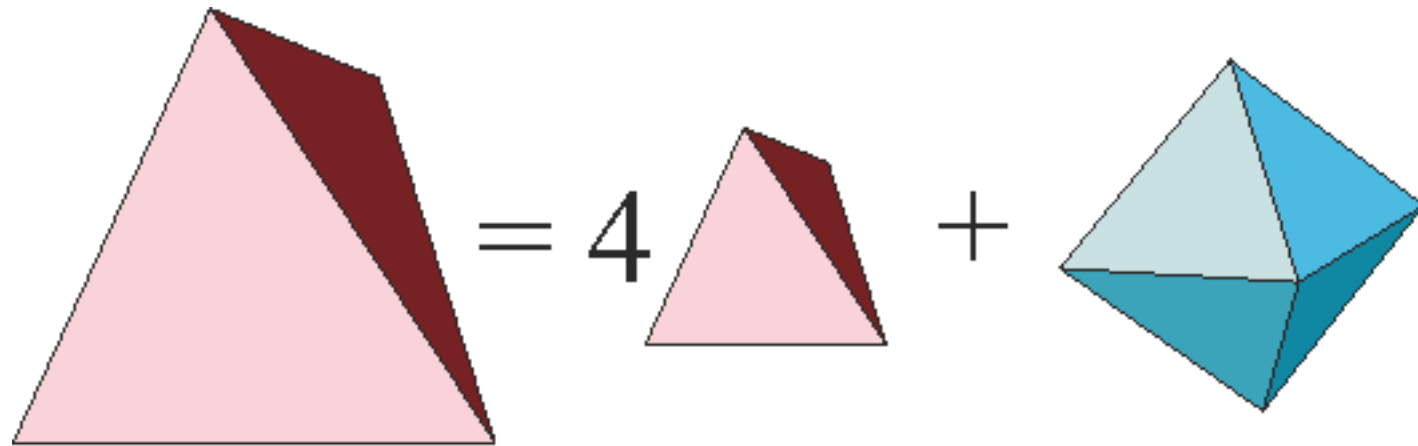
# VOLUM DE L'OCTAEDRE



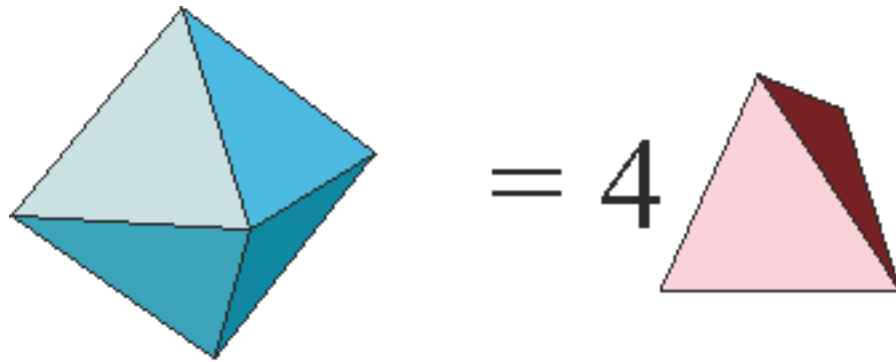
# VOLUM DE L'OCTAEDRE



# VOLUM DE L'OCTAEDRE

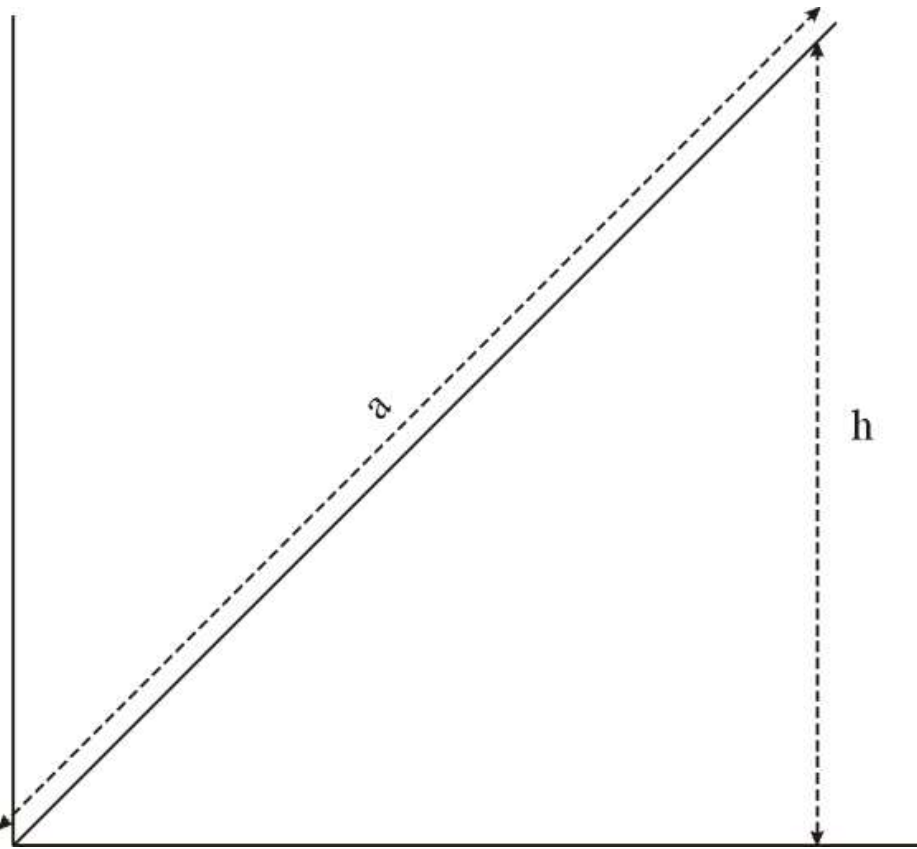


# VOLUM DE L'OCTAEDRE



$$V(\text{octaedre}) = 4V(\text{tetraedre}) = 4 \cdot \frac{\sqrt{2}}{12} \cdot a^3 = \frac{\sqrt{2}}{3} \cdot a^3$$

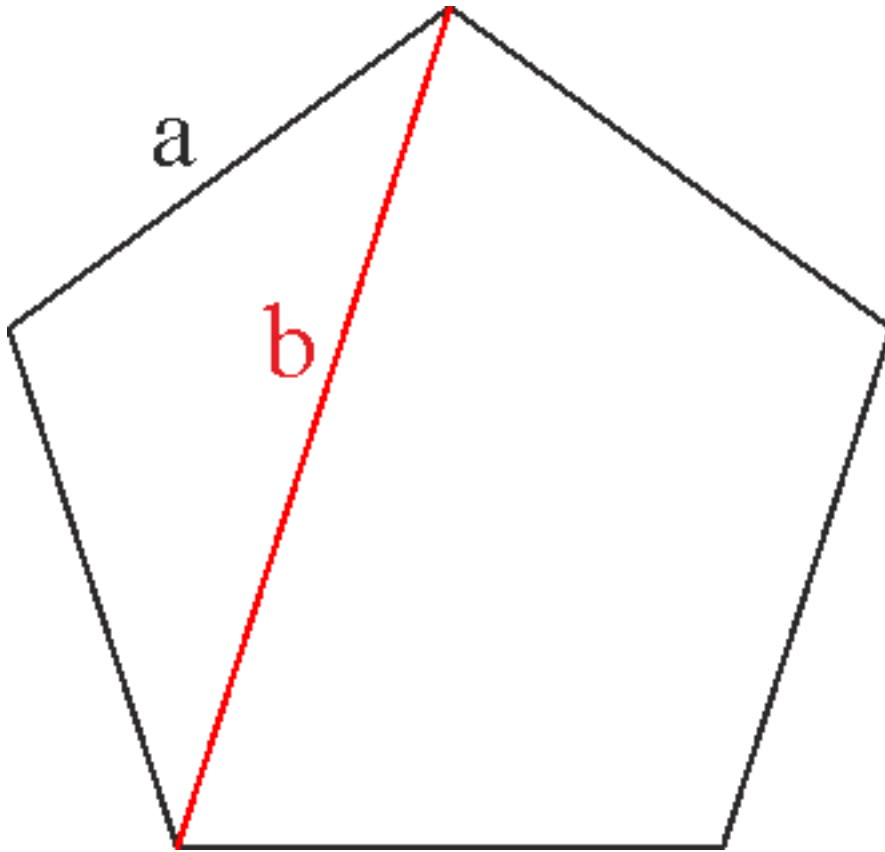
# APROXIMACIÓ DEL VOLUM DE L'OCTAEDRE



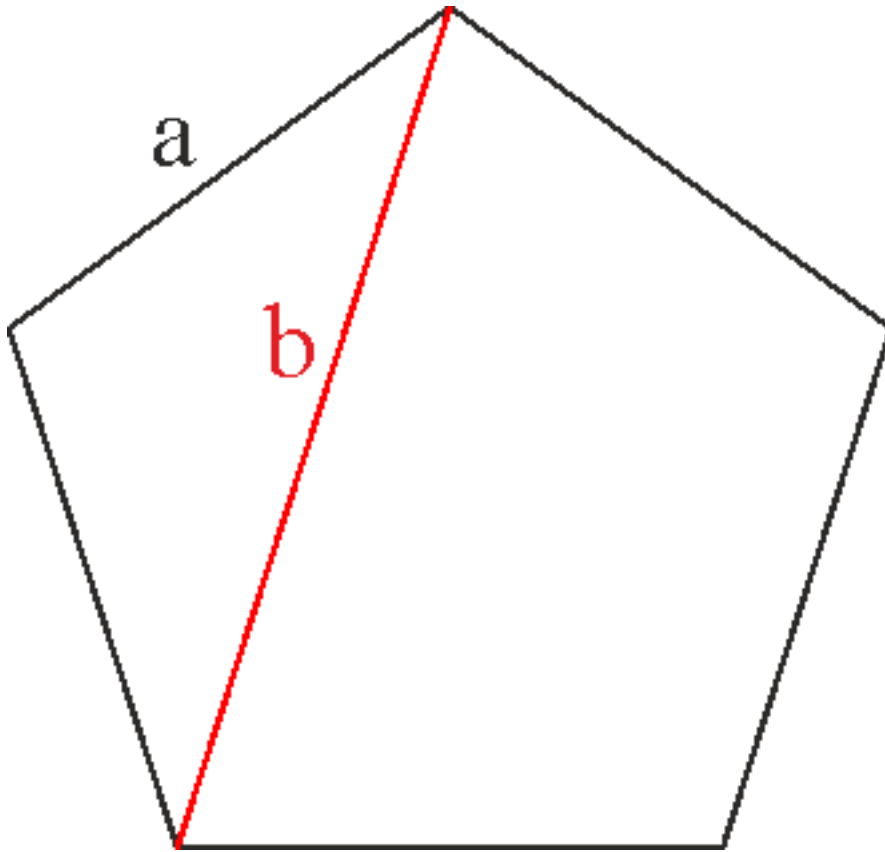
$$V(\text{tetraedre}) = \frac{h^3}{3}$$

$$V(\text{octaedre}) = \frac{4 \cdot h^3}{3}$$

# ARESTA I DIAGONAL D'UN PENTÀGON ESTAN EN PROPORCIÓ AURIA



# ARESTA I DIAGONAL D'UN PENTÀGON ESTAN EN PROPORCIÓ AURIA



$$\frac{b}{a} = \Phi = \frac{1 + \sqrt{5}}{2}$$



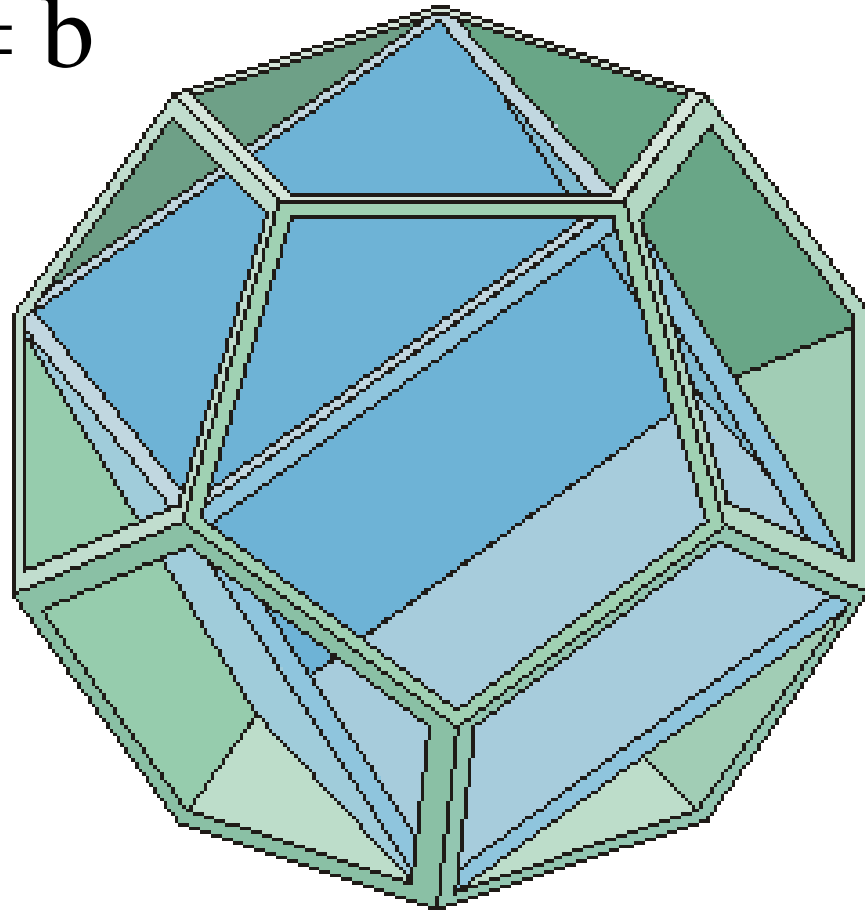


# VOLUM DEL DODECAEDRE

Aresta del dodecaedre =  $a$

Aresta del cub =  $b$

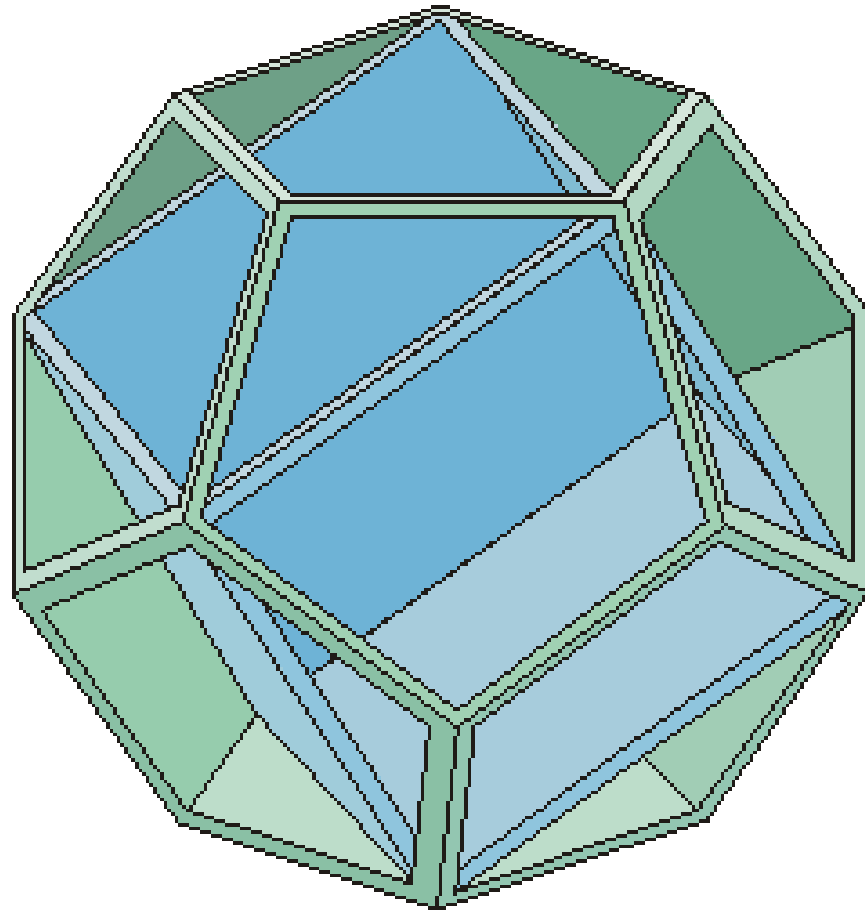
$$b/a = \Phi$$



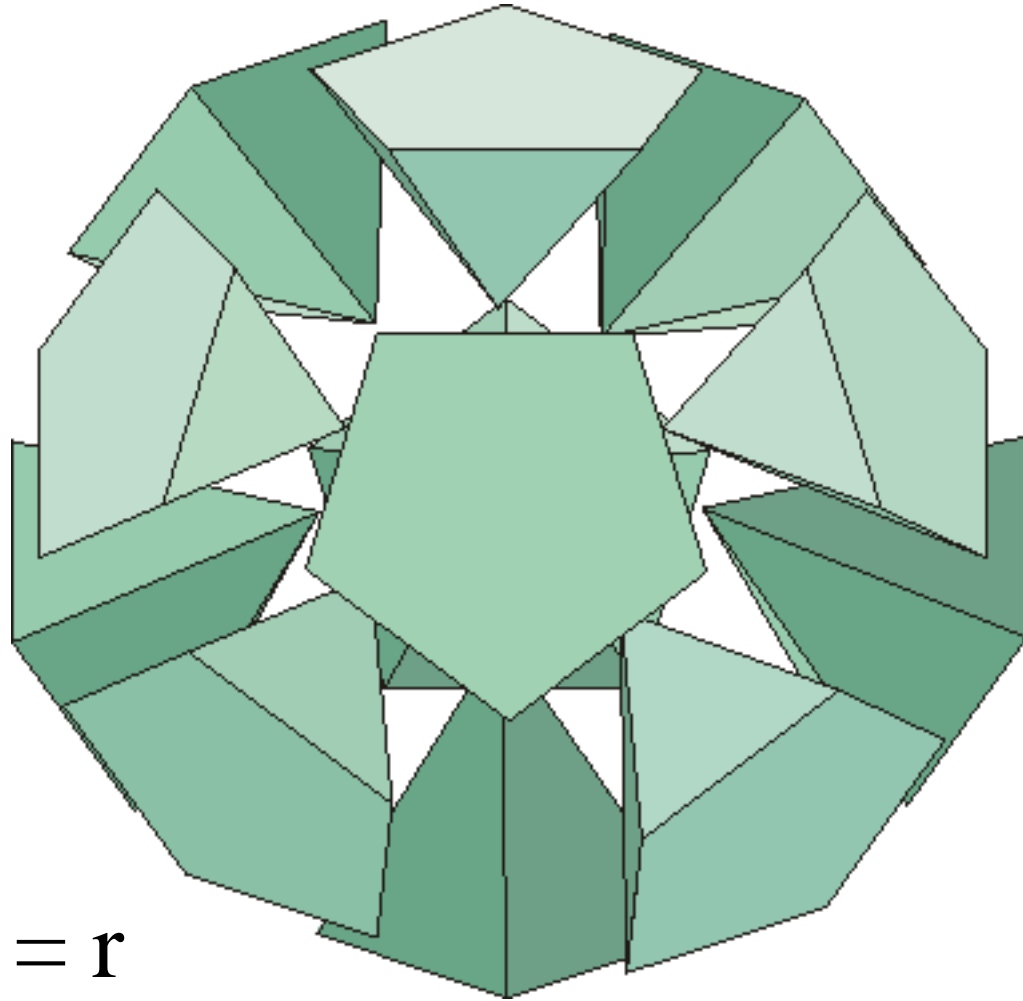
Radi dodecaedre = Radi cub = r

Radi cub =  $\frac{1}{2}$  diagonal del cub

$$\begin{aligned} r &= \frac{1}{2}d = \frac{\sqrt{3}}{2}b = \\ &= \frac{\sqrt{3}}{2} \cdot \frac{1+\sqrt{5}}{2}a = \\ &= \frac{\sqrt{3} + \sqrt{15}}{4}a \end{aligned}$$



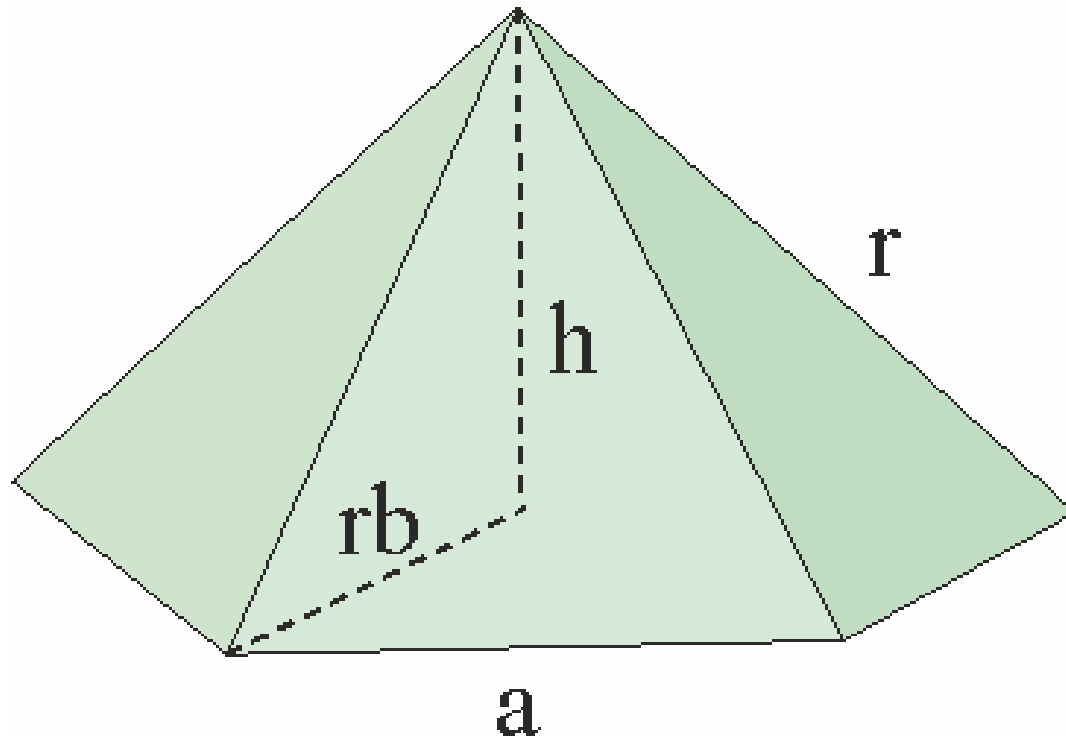
$$V (\text{dodecaedre}) = 12 \cdot V (\text{Piramide})$$

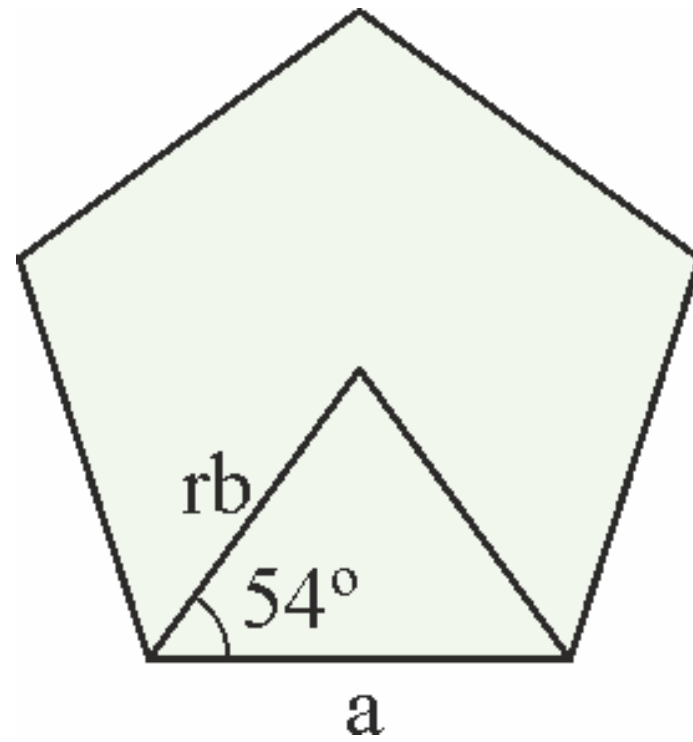


Aresta lateral =  $r$

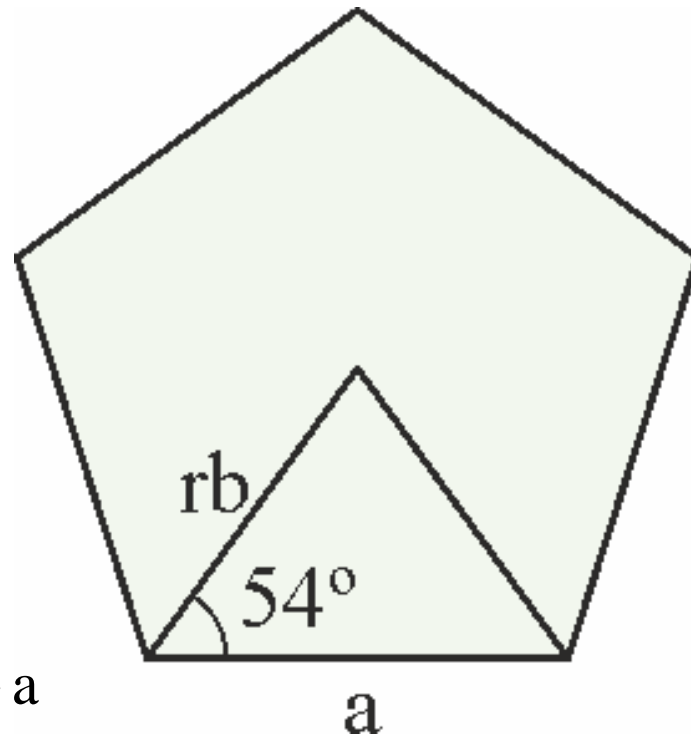


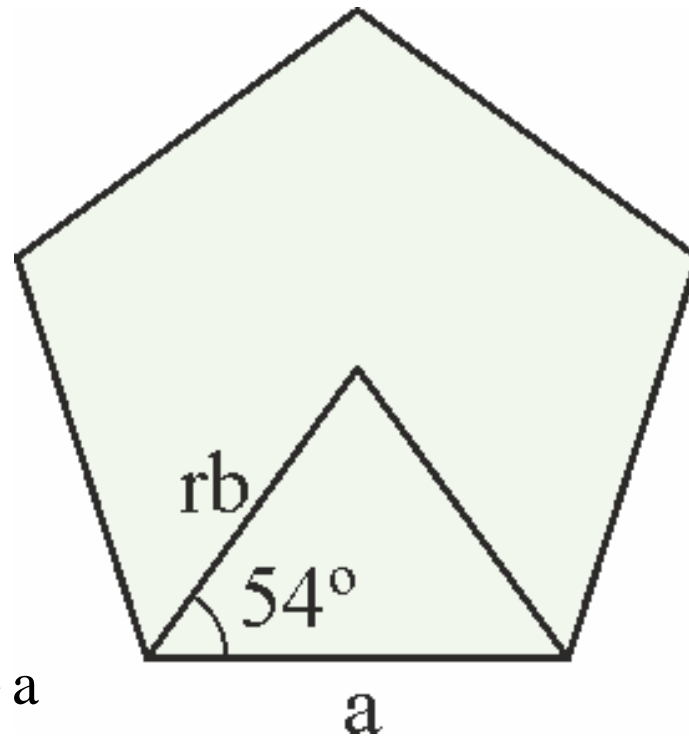
# Volum de la piràmide





$$rb = \frac{a}{2 \cos(54)} = \frac{\sqrt{10 \cdot \sqrt{5} + 50}}{10} \cdot a$$

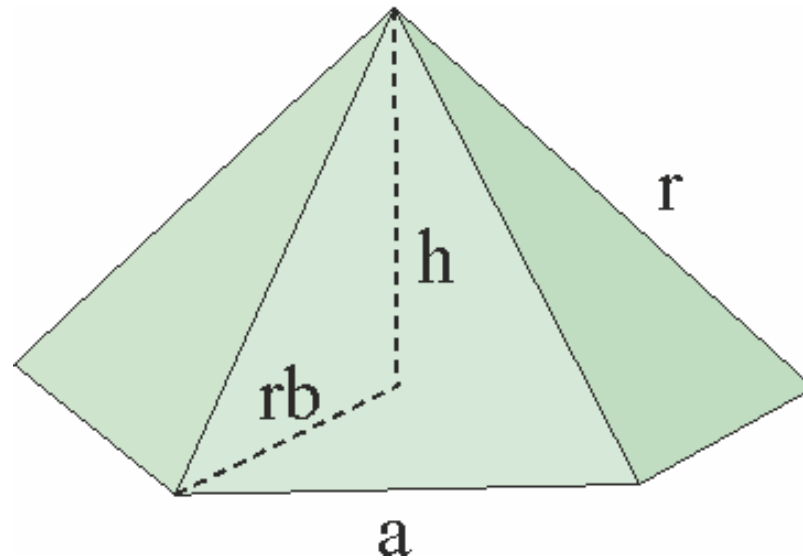




$$rb = \frac{a}{2 \cos(54)} = \frac{\sqrt{10 \cdot \sqrt{5} + 50}}{10} \cdot a$$

$$Ab = 5 \cdot \frac{a \cdot rb \cdot \sin(54)}{2} = \left( \frac{5 \cdot \sqrt{2 \cdot \sqrt{5} + 10}}{16} + \frac{\sqrt{10 \cdot \sqrt{5} + 50}}{16} \right) \cdot a^2$$



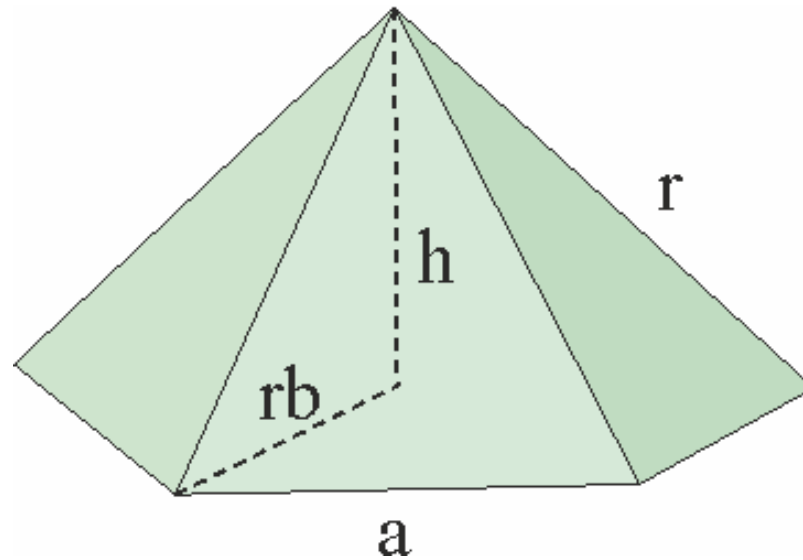


$$rb = \frac{a}{2 \cos(54)} = \frac{\sqrt{10 \cdot \sqrt{5} + 50}}{10} \cdot a$$

$$Ab = 5 \cdot \frac{a \cdot rb \cdot \sin(54)}{2} = \left( \frac{5 \cdot \sqrt{2 \cdot \sqrt{5} + 10}}{16} + \frac{\sqrt{10 \cdot \sqrt{5} + 50}}{16} \right) \cdot a^2$$







$$rb = \frac{a}{2 \cos(54)} = \frac{\sqrt{10 \cdot \sqrt{5} + 50}}{10} \cdot a$$

$$Ab = 5 \cdot \frac{a \cdot rb \cdot \sin(54)}{2} = \left( \frac{5 \cdot \sqrt{2 \cdot \sqrt{5} + 10}}{16} + \frac{\sqrt{10 \cdot \sqrt{5} + 50}}{16} \right) \cdot a^2$$

$$h = \sqrt{r^2 - (rb)^2} = \frac{\sqrt{110 \cdot \sqrt{5} + 250}}{20} \cdot a$$



$$rb = \frac{a}{2 \cos(54)} = \frac{\sqrt{10 \cdot \sqrt{5} + 50}}{10} \cdot a$$

$$Ab = 5 \cdot \frac{a \cdot rb \cdot \sin(54)}{2} = \left( \frac{5 \cdot \sqrt{2 \cdot \sqrt{5} + 10}}{16} + \frac{\sqrt{10 \cdot \sqrt{5} + 50}}{16} \right) \cdot a^2$$

$$h = \sqrt{r^2 - (rb)^2} = \frac{\sqrt{110 \cdot \sqrt{5} + 250}}{20} \cdot a$$



$$rb = \frac{a}{2 \cos(54)} = \frac{\sqrt{10 \cdot \sqrt{5} + 50}}{10} \cdot a$$

$$Ab = 5 \cdot \frac{a \cdot rb \cdot \sin(54)}{2} = \left( \frac{5 \cdot \sqrt{2 \cdot \sqrt{5} + 10}}{16} + \frac{\sqrt{10 \cdot \sqrt{5} + 50}}{16} \right) \cdot a^2$$

$$h = \sqrt{r^2 - (rb)^2} = \frac{\sqrt{110 \cdot \sqrt{5} + 250}}{20} \cdot a$$

$$V(P) = \frac{Ab \cdot h}{3}$$



$$rb = \frac{a}{2 \cos(54)} = \frac{\sqrt{10 \cdot \sqrt{5} + 50}}{10} \cdot a$$

$$Ab = 5 \cdot \frac{a \cdot rb \cdot \sin(54)}{2} = \left( \frac{5 \cdot \sqrt{2 \cdot \sqrt{5} + 10}}{16} + \frac{\sqrt{10 \cdot \sqrt{5} + 50}}{16} \right) \cdot a^2$$

$$h = \sqrt{r^2 - (rb)^2} = \frac{\sqrt{110 \cdot \sqrt{5} + 250}}{20} \cdot a$$

$$V(P) = \frac{Ab \cdot h}{3}$$

$$V(\text{dodeca}) = 12 \cdot V(P) = 4 \cdot Ab \cdot h$$

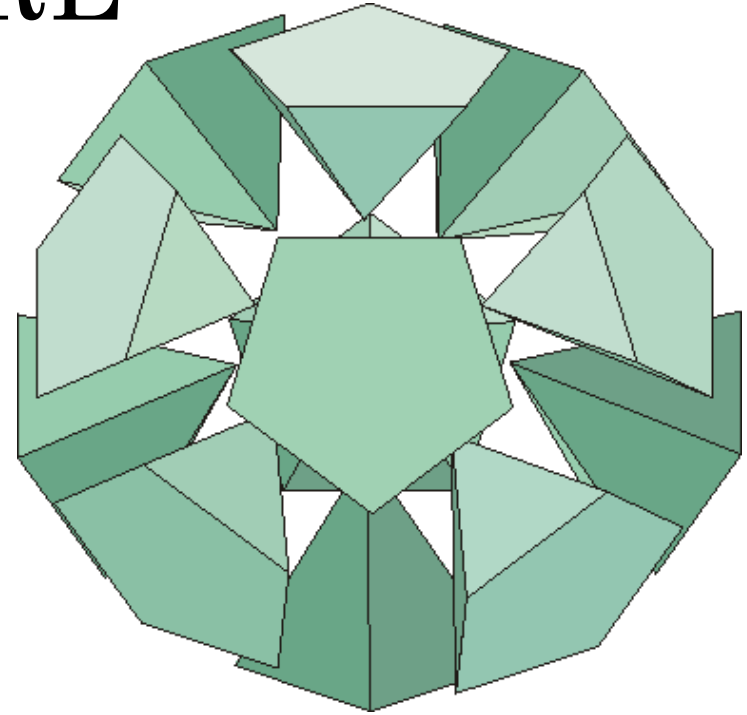


## VOLUM DEL DODECAEDRE

$$V = 4 \cdot Ab \cdot h = \left( \frac{7\sqrt{5}}{4} + \frac{15}{4} \right) \cdot a^3$$



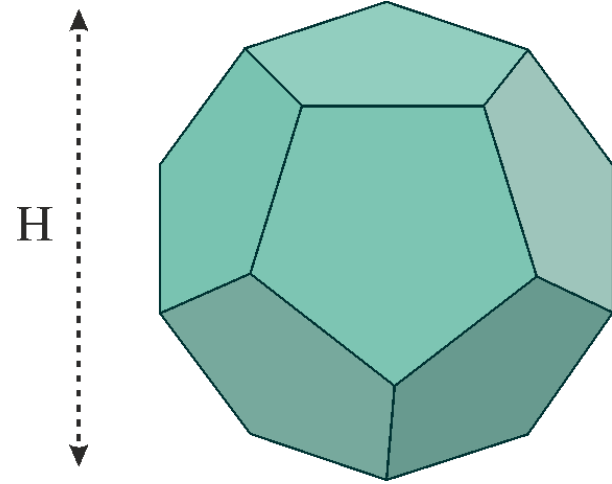
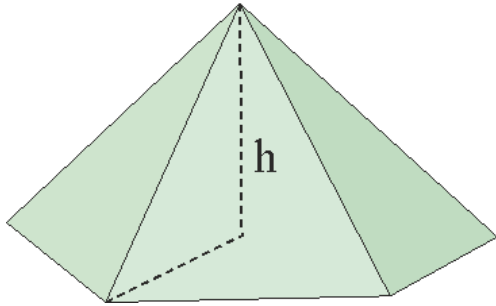
# APROXIMACIÓ DEL VOLUM DEL DODECAEDRE



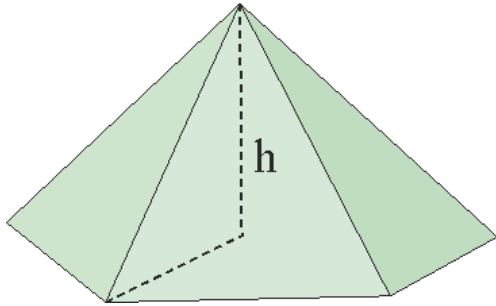
$$V (\text{dodecaedre}) = 12 \cdot V (\text{Piràmide}) = 12 \cdot \frac{A_B \cdot h}{3}$$



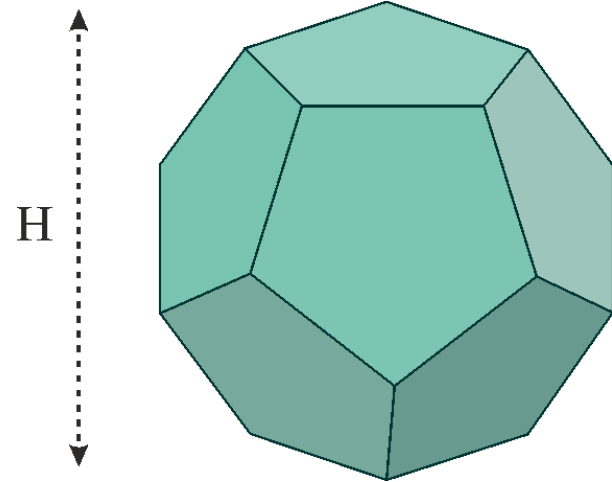
# APROXIMACIÓ DEL VOLUM DEL DODECAEDRE



# APROXIMACIÓ DEL VOLUM DEL DODECAEDRE

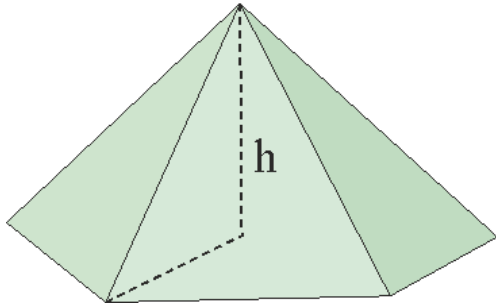


$$h = \frac{H}{2}$$



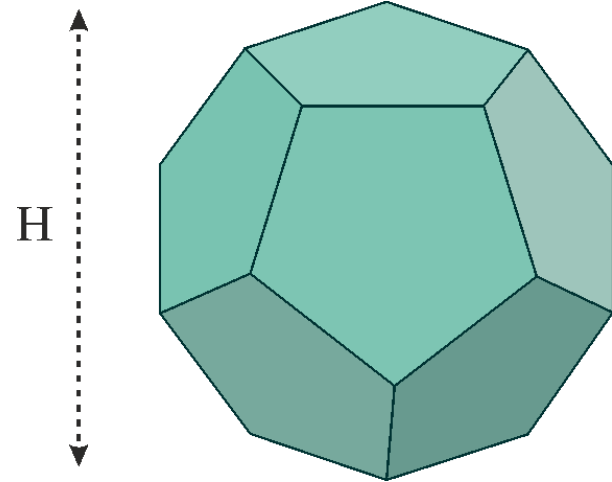


# APROXIMACIÓ DEL VOLUM DEL DODECAEDRE

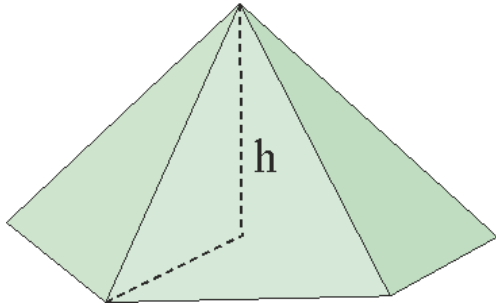


$$h = \frac{H}{2}$$

$$V_{\text{piramide}} = \frac{A_B H}{6}$$



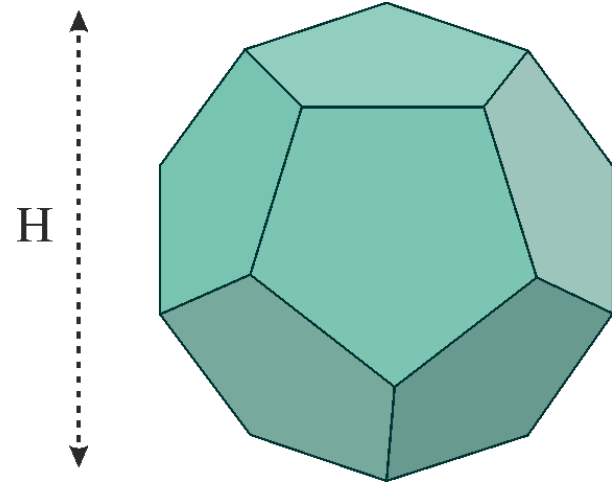
# APROXIMACIÓ DEL VOLUM DEL DODECAEDRE



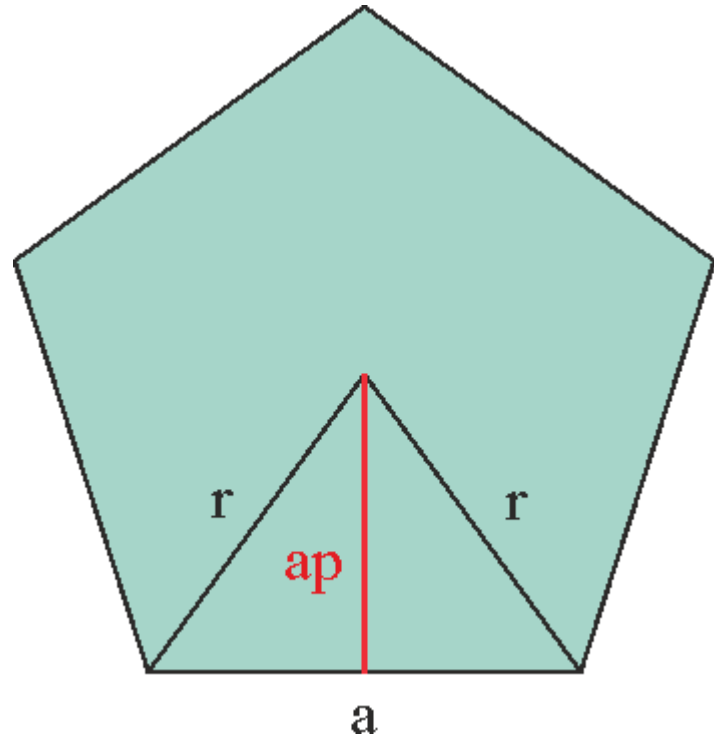
$$h = \frac{H}{2}$$

$$V_{\text{piramide}} = \frac{A_B H}{6}$$

$$V_{\text{dodecaedre}} = 2 \cdot A_B H$$

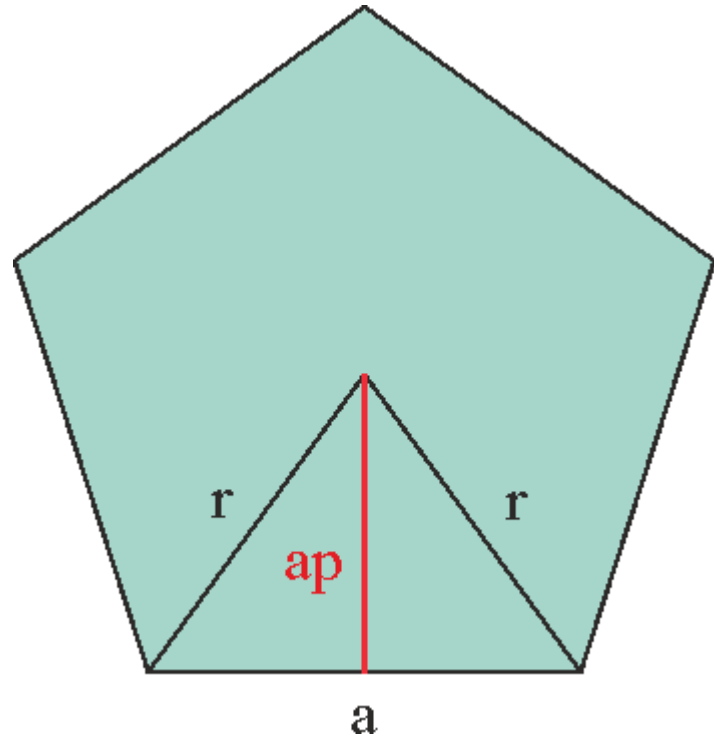


# APROXIMACIÓ DEL VOLUM DEL DODECAEDRE



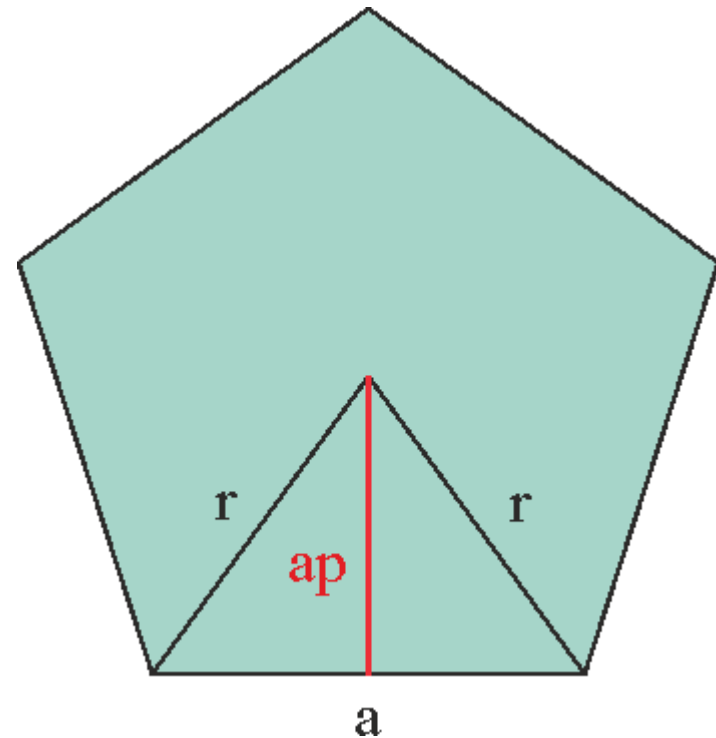
# APROXIMACIÓ DEL VOLUM DEL DODECAEDRE

$$\frac{a}{ap} = k$$



# APROXIMACIÓ DEL VOLUM DEL DODECAEDRE

| costat | apotema | c/ap |
|--------|---------|------|
| 3      | 2,1     | 1,43 |
| 4      | 2,8     | 1,43 |
| 5      | 3,4     | 1,47 |
| 6      | 4,2     | 1,43 |
| 7      | 4,8     | 1,46 |
| 8      | 5,5     | 1,45 |
| 9      | 6,2     | 1,45 |
| 10     | 6,9     | 1,45 |
| 11     | 7,6     | 1,45 |
| 12     | 8,3     | 1,45 |
| 13     | 8,9     | 1,46 |
| 14     | 9,6     | 1,46 |
| 15     | 10,3    | 1,46 |



Mitjana  $c/ap = 1,45$

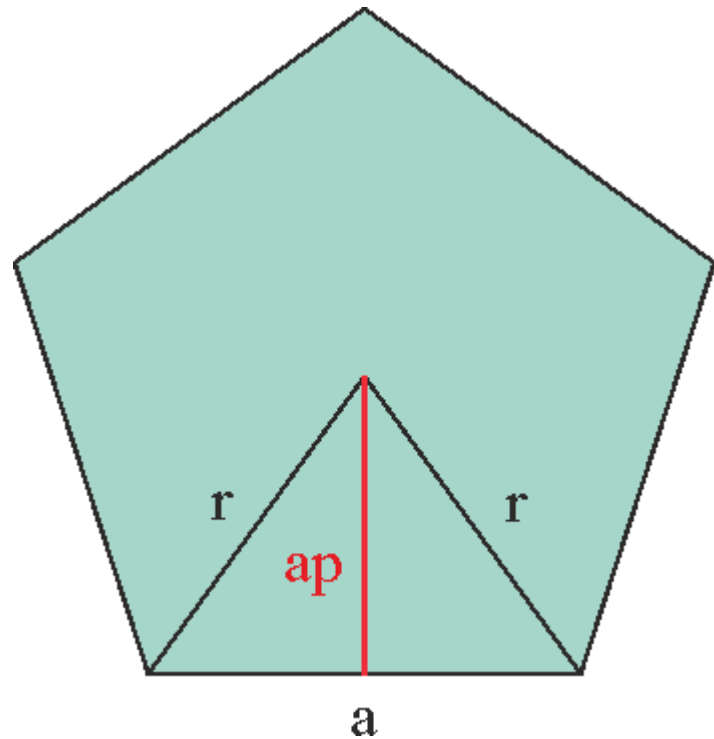


# APROXIMACIÓ DEL VOLUM DEL DODECAEDRE

$$\frac{a}{ap} = 1,45$$

$$ap = \frac{a}{1,45}$$

En realitat  $ap = \frac{a}{1,45309}$



Mitjana  $c/ap = 1,45$



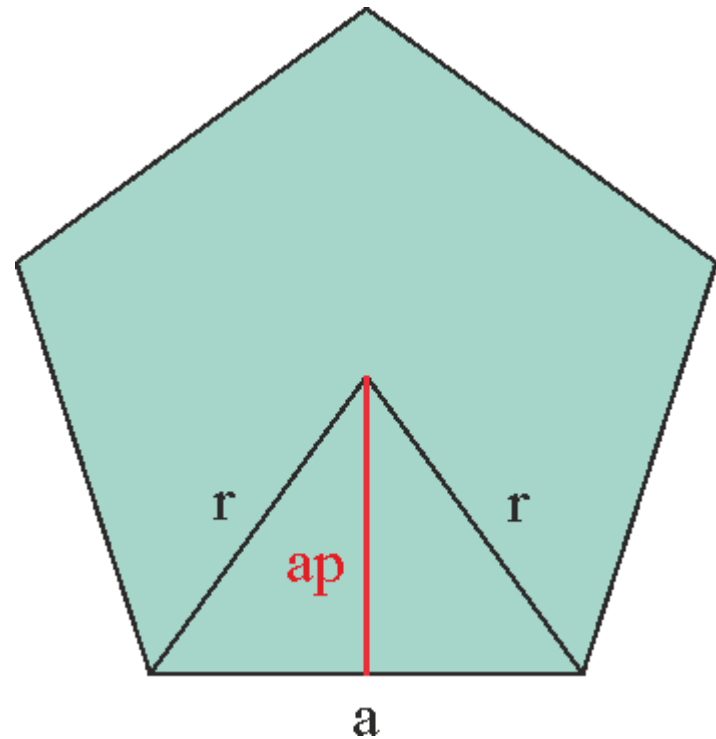
# APROXIMACIÓ DEL VOLUM DEL DODECAEDRE

$$\frac{a}{ap} = 1,45$$

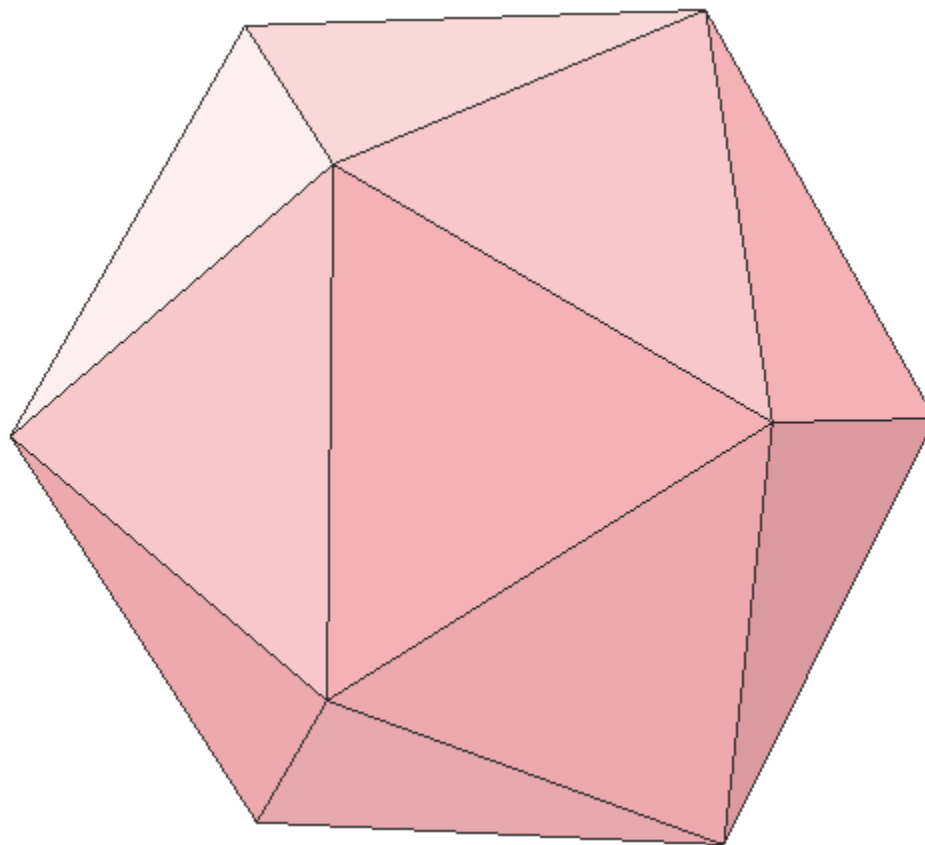
$$ap = \frac{a}{1,45}$$

En realitat  $ap = \frac{a}{1,45309}$

$$A_B = \frac{\text{Per} \cdot ap}{2} = \frac{5a \cdot \frac{a}{1,45}}{2} = 1,72a^2$$

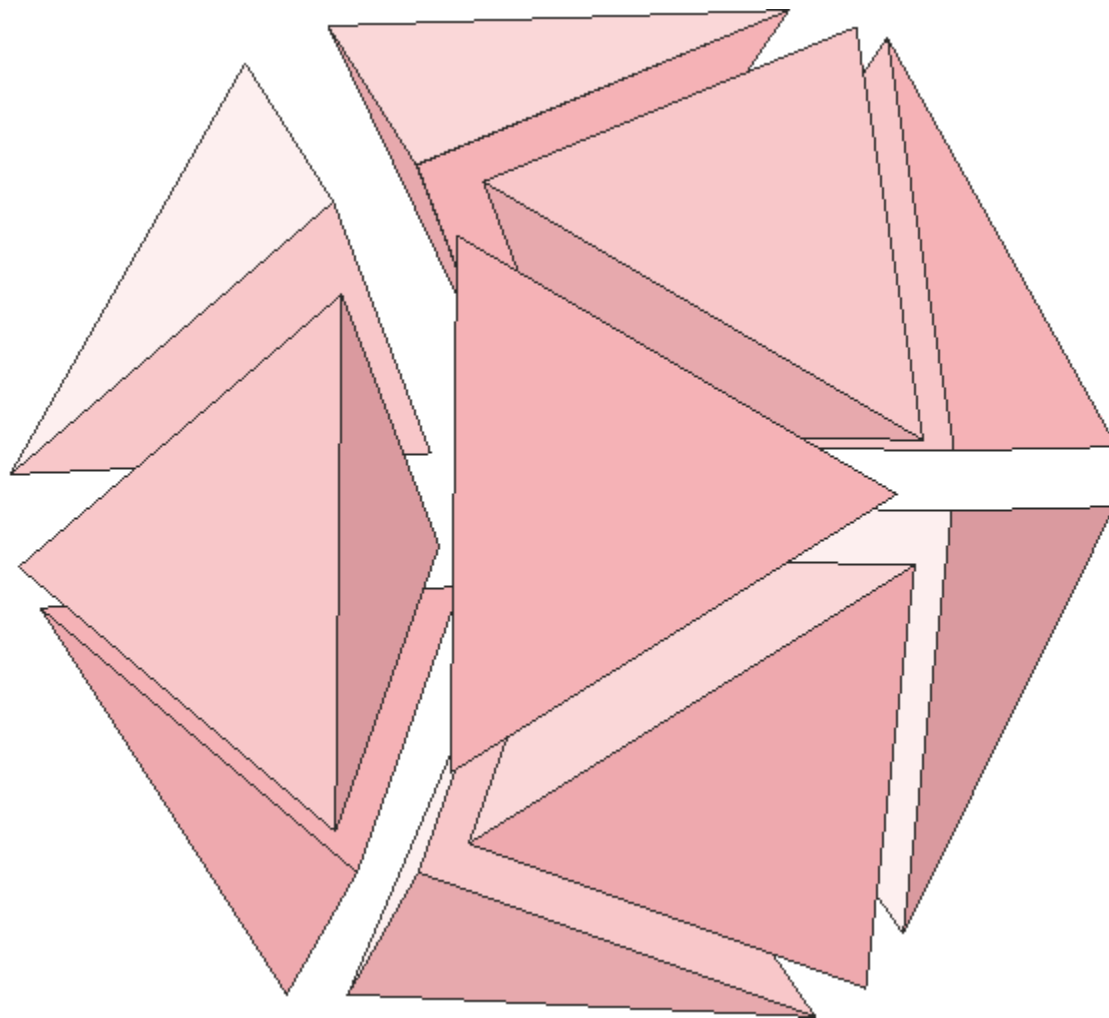


# VOLUM DE L'ICOSAEDRE



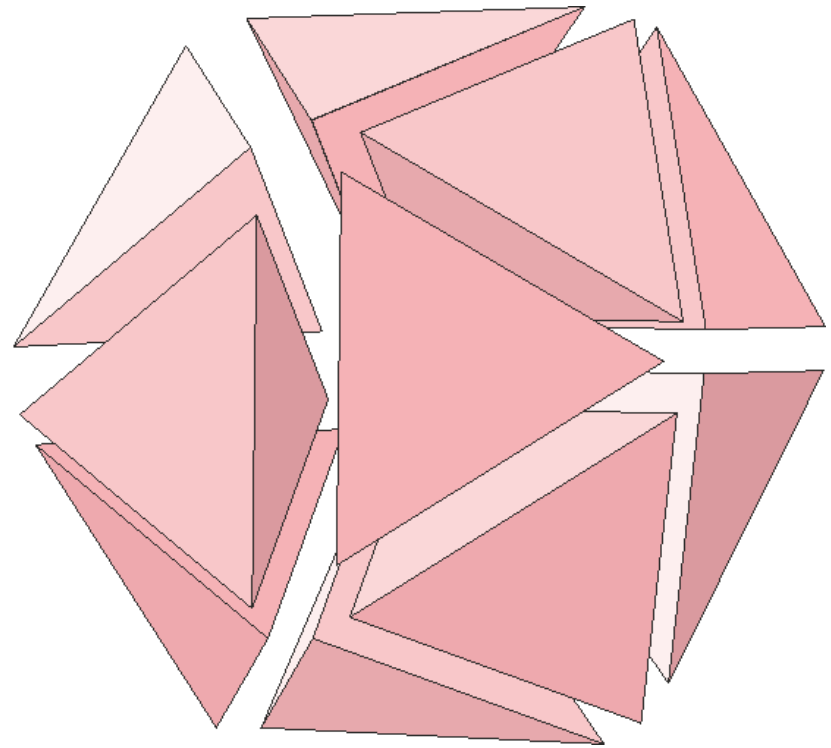


# VOLUM DE L'ICOSAEDRE

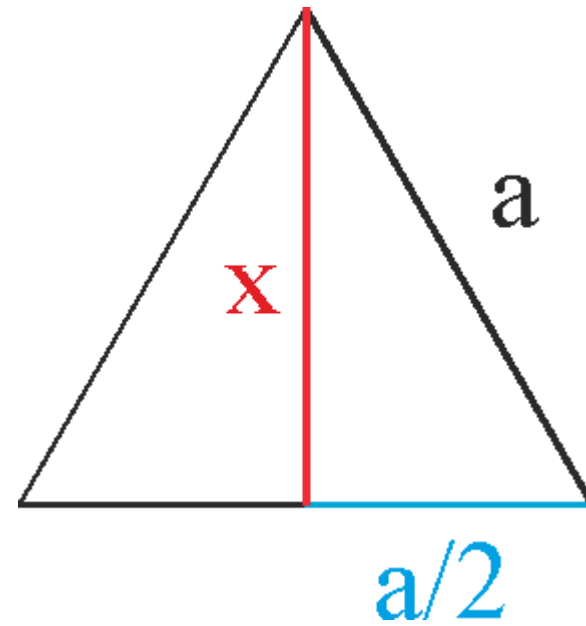


# VOLUM DE L'ICOSAEDRE

$$V (\text{icosaedre}) = 20 \cdot V (\text{Piràmide}) = 20 \cdot \frac{A_B \cdot h}{3}$$

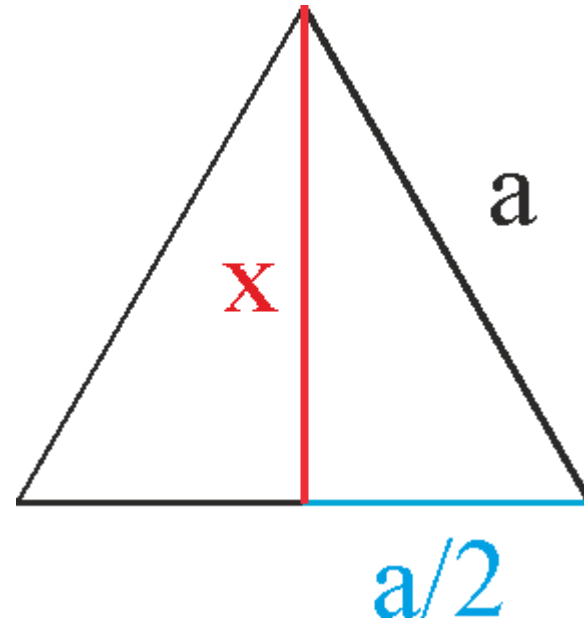


# VOLUM DE L'ICOSAEDRE



# VOLUM DE L'ICOSAEDRE

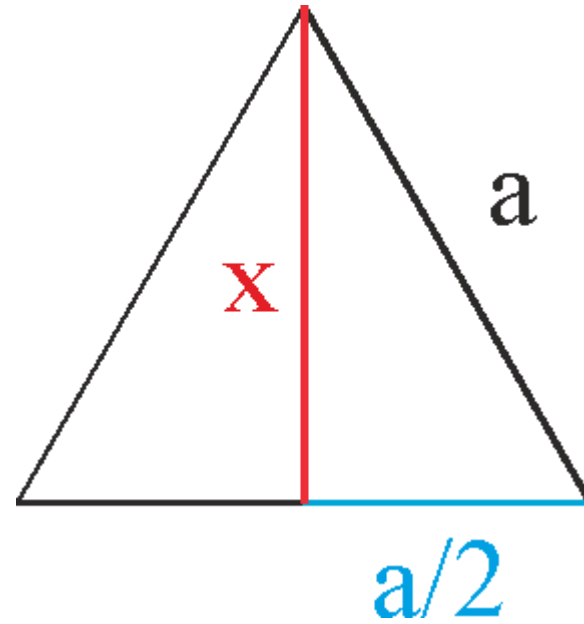
$$x^2 = a^2 - \left(\frac{a}{2}\right)^2$$



# VOLUM DE L'ICOSAEDRE

$$x^2 = a^2 - \left(\frac{a}{2}\right)^2$$

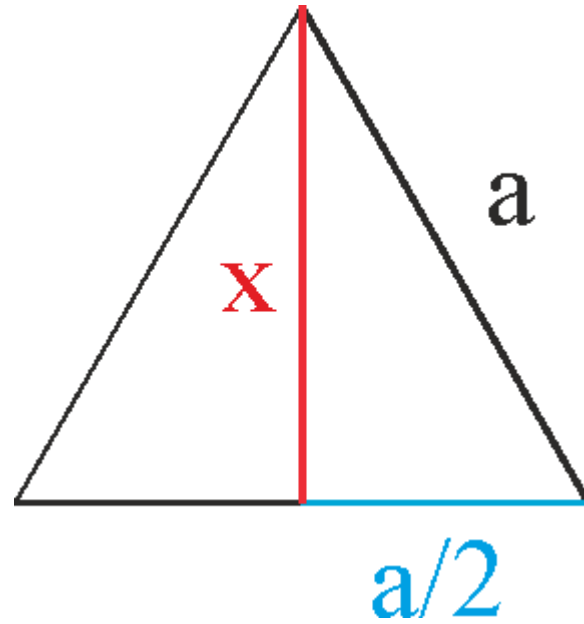
$$x = \frac{\sqrt{3}}{2}a$$



# VOLUM DE L'ICOSAEDRE

$$x^2 = a^2 - \left(\frac{a}{2}\right)^2$$

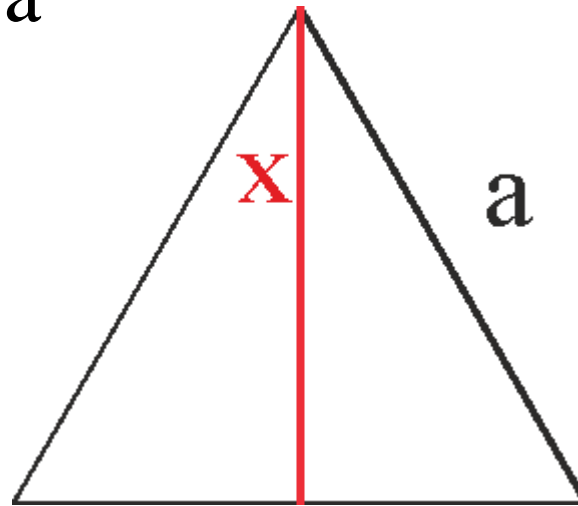
$$x = \frac{\sqrt{3}}{2} a$$



$$A_B = \frac{a \cdot \left(\frac{\sqrt{3}}{2} a\right)}{2} = \frac{\sqrt{3}}{4} \cdot a^2$$

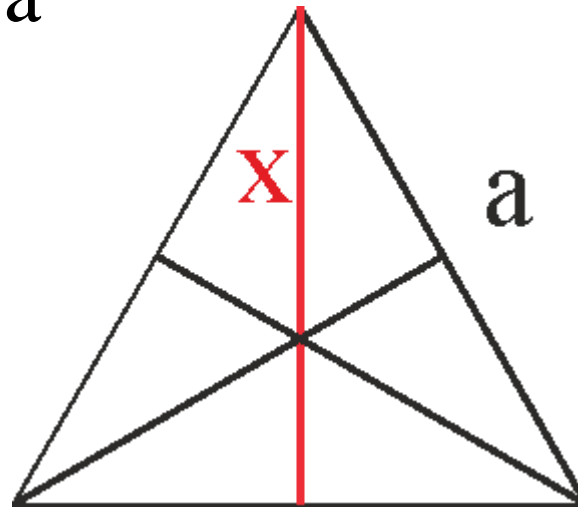
# VOLUM DE L'ICOSAEDRE

$$x = \frac{\sqrt{3}}{2}a$$



# VOLUM DE L'ICOSAEDRE

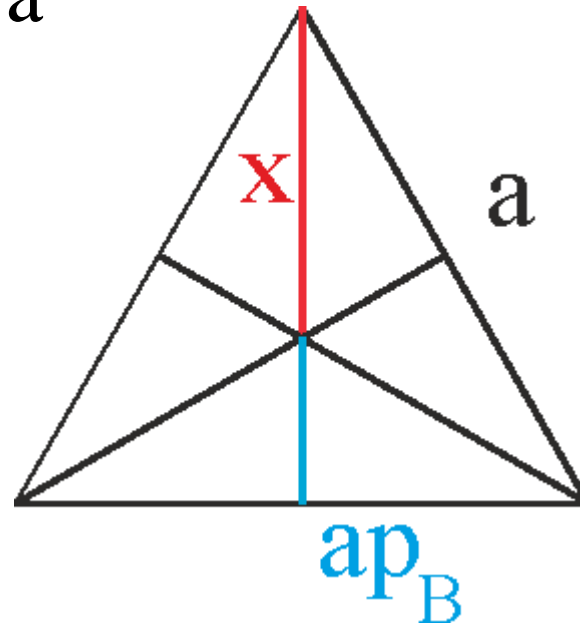
$$x = \frac{\sqrt{3}}{2}a$$





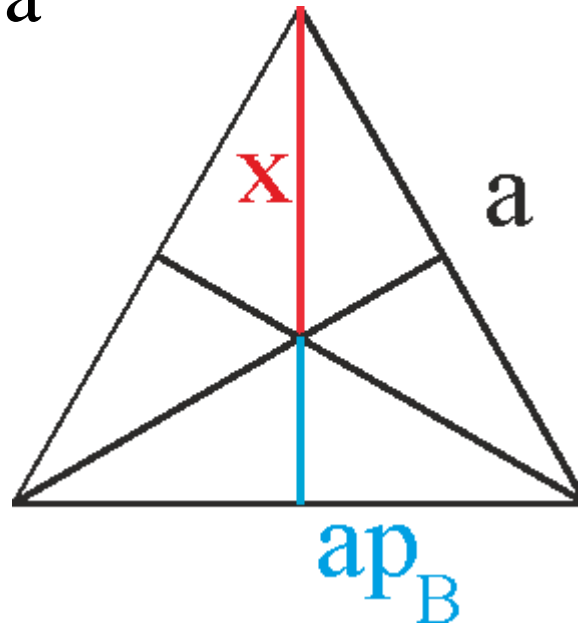
# VOLUM DE L'ICOSAEDRE

$$x = \frac{\sqrt{3}}{2}a$$



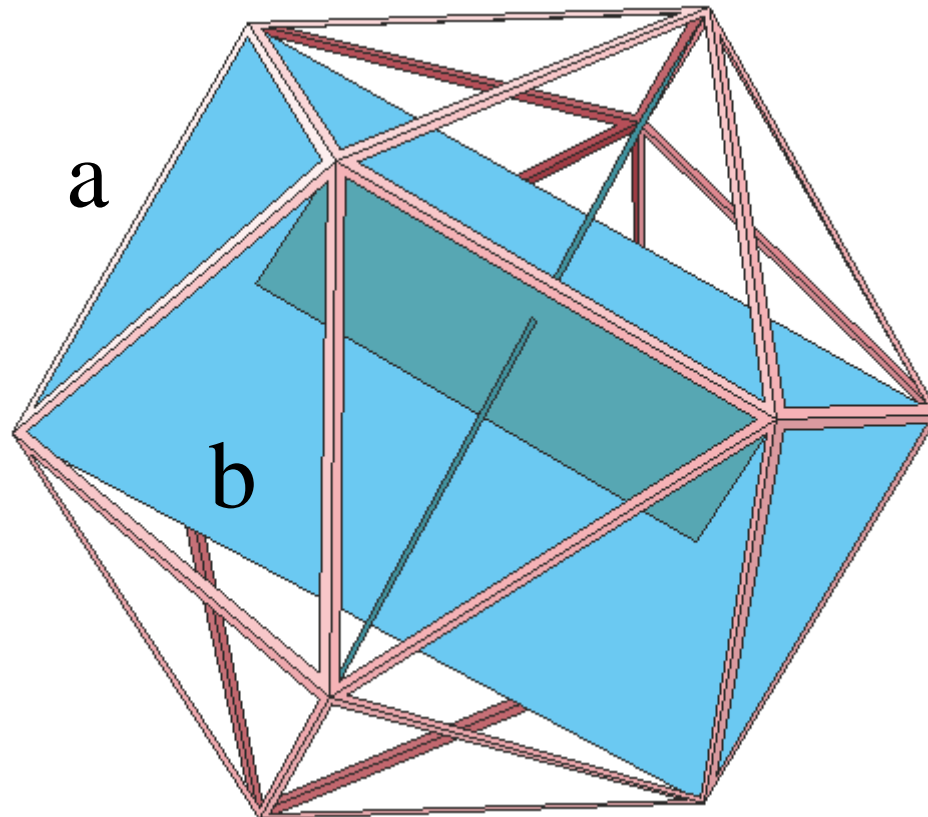
# VOLUM DE L'ICOSAEDRE

$$x = \frac{\sqrt{3}}{2} a$$

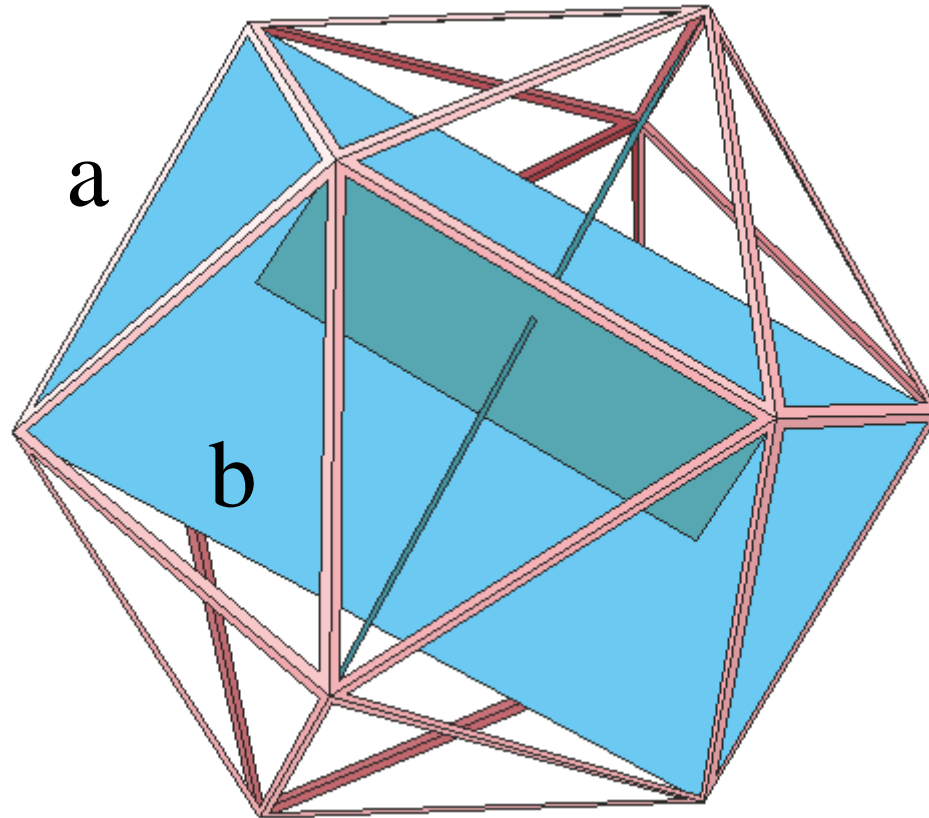


$$ap_B = \frac{x}{3} = \frac{\sqrt{3}}{6} a$$

# VOLUM DE L'ICOSAEDRE

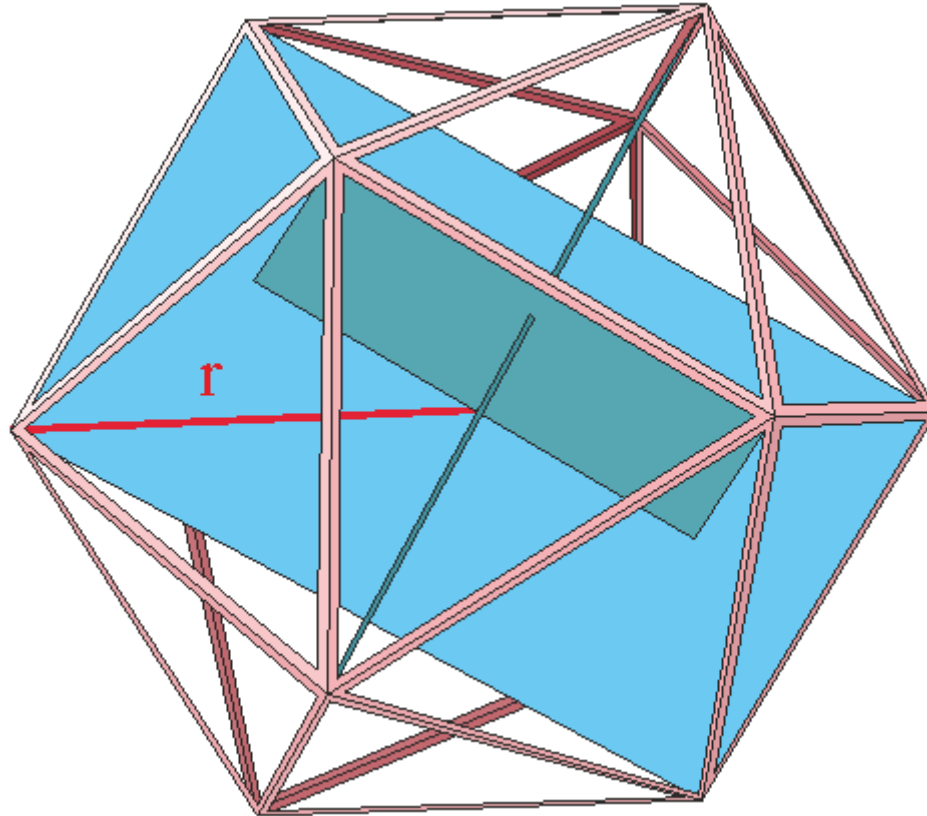


# VOLUM DE L'ICOSAEDRE



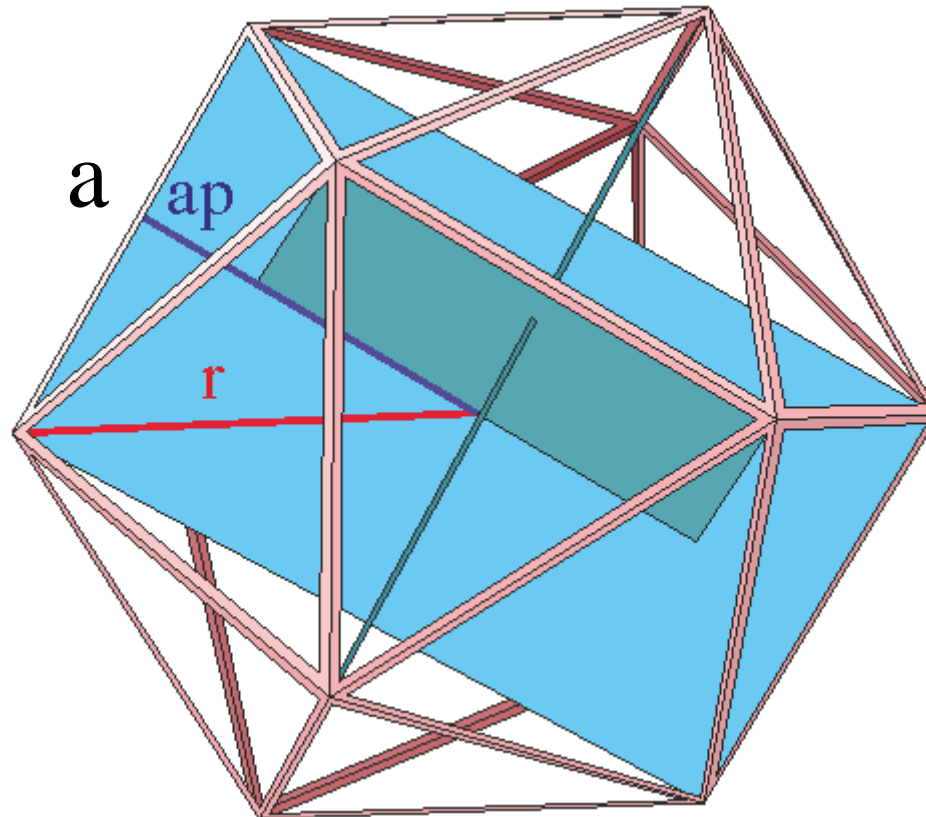
$$\frac{b}{a} = \Phi$$

# VOLUM DE L'ICOSAEDRE



$$\frac{b}{a} = \Phi$$

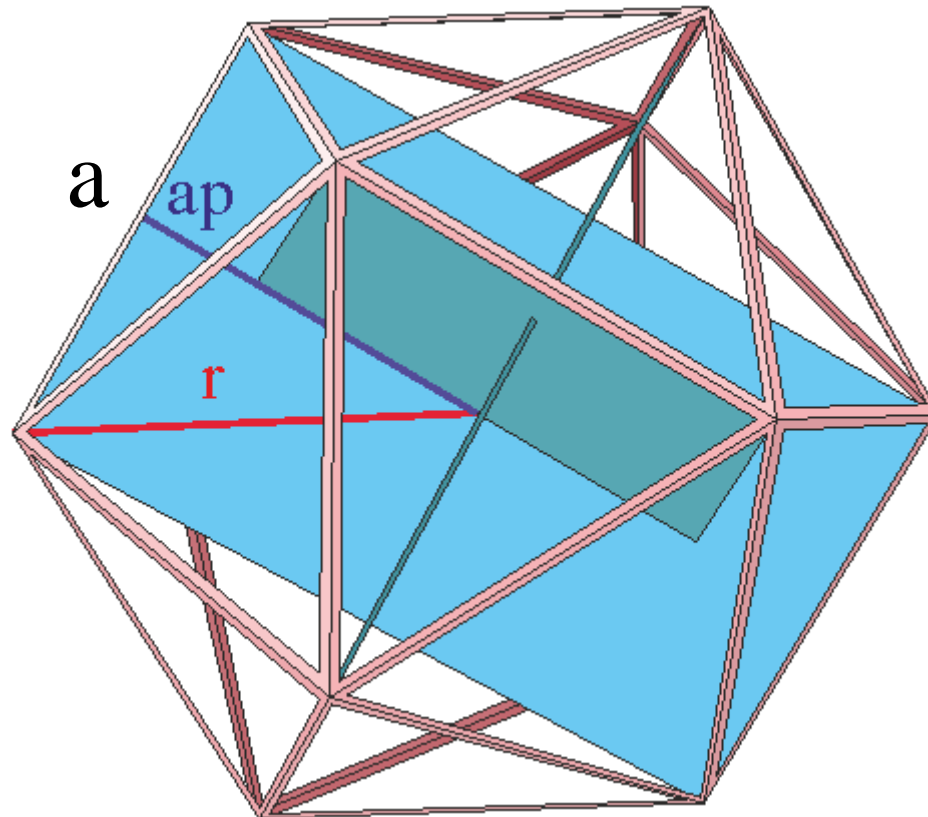
# VOLUM DE L'ICOSAEDRE



$$\frac{b}{a} = \Phi$$

$$\frac{ap}{a} = \frac{\Phi}{2}$$

# VOLUM DE L'ICOSAEDRE

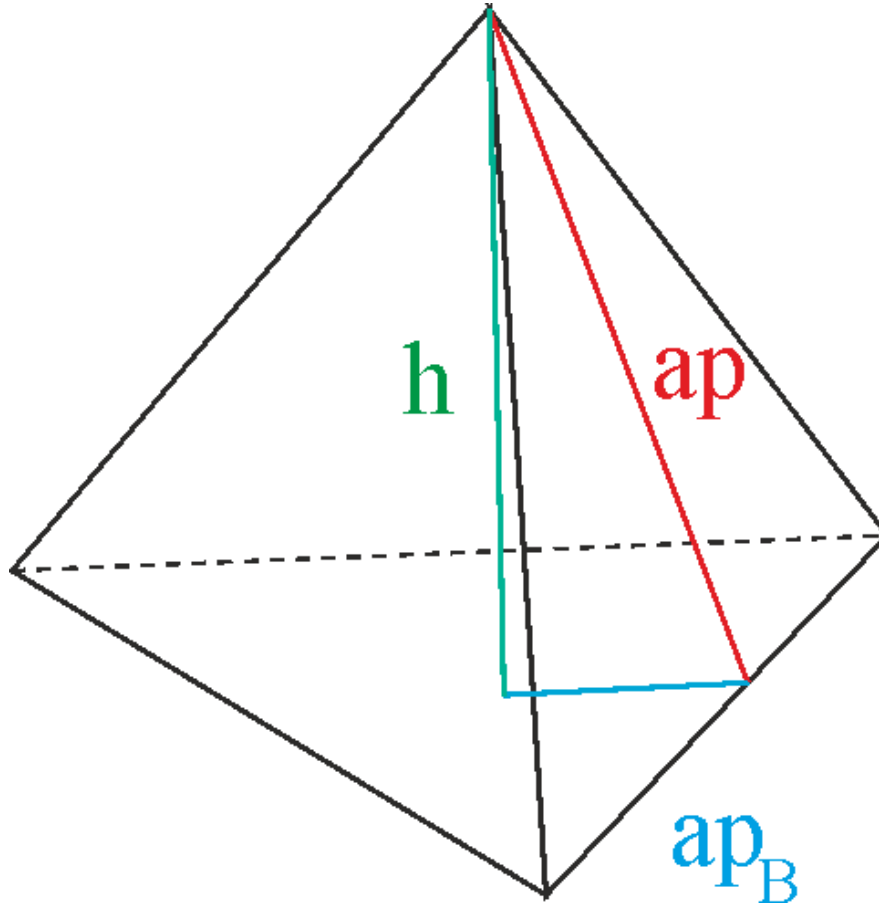


$$\frac{b}{a} = \Phi$$

$$\frac{ap}{a} = \frac{\Phi}{2}$$

$$ap = \frac{\Phi}{2} a = \frac{1 + \sqrt{5}}{4} a$$

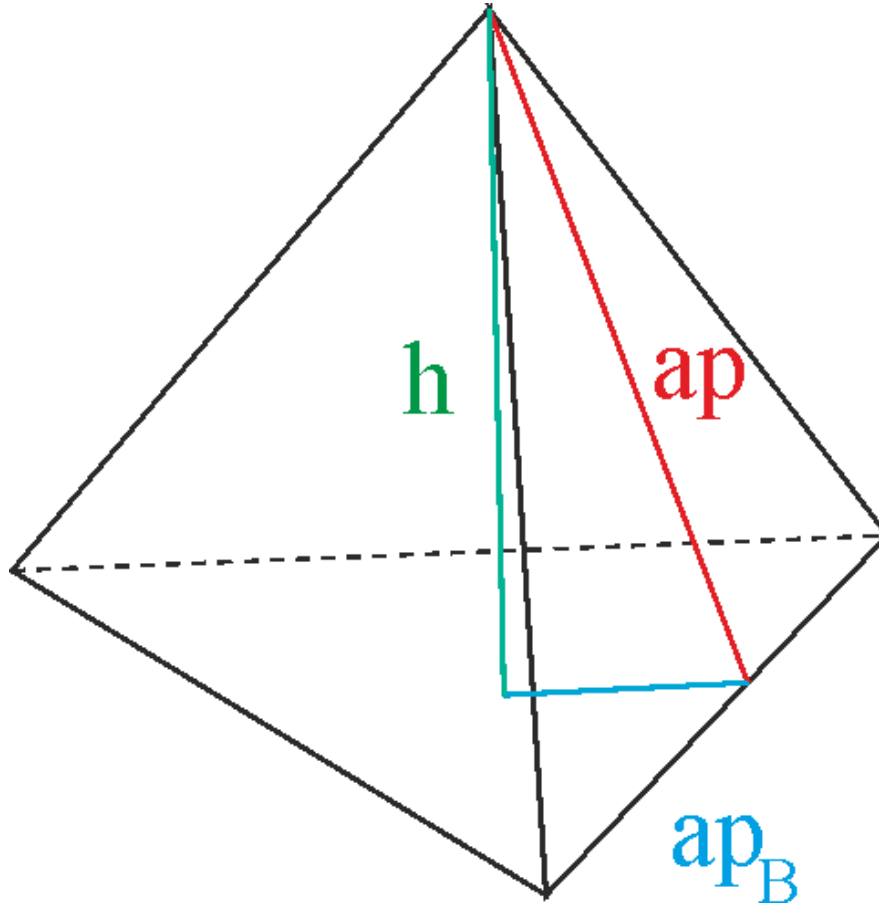
# VOLUM DE L'ICOSAEDRE



$$h^2 = ap^2 - ap_B^2$$



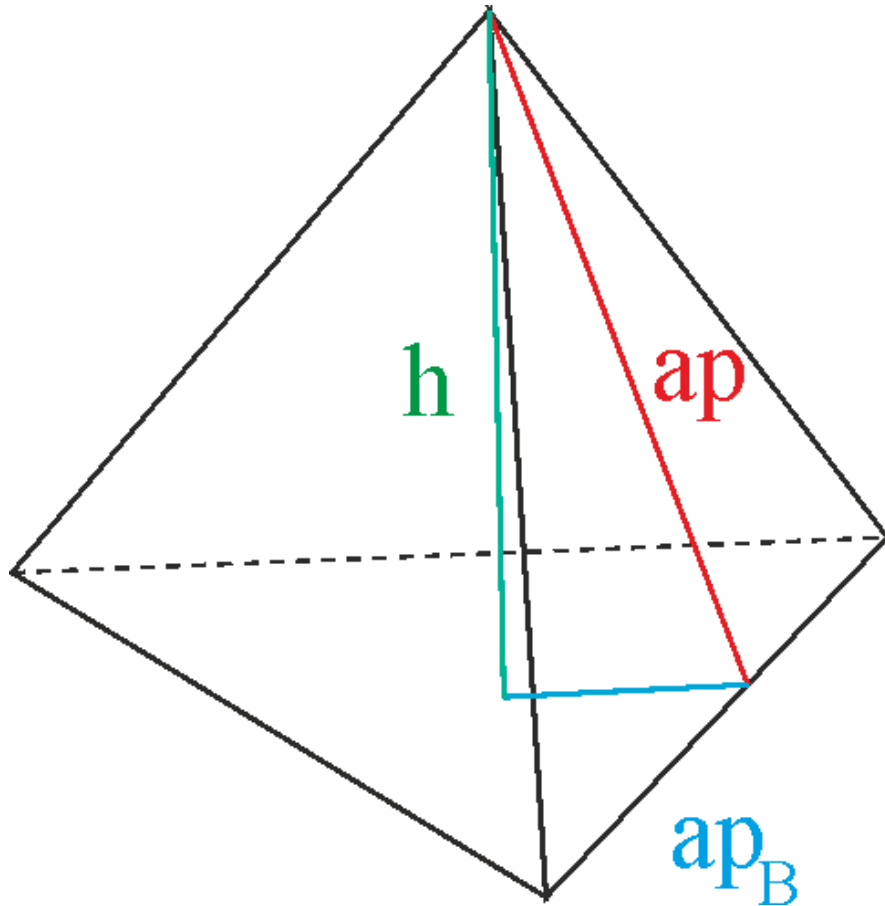
# VOLUM DE L'ICOSAEDRE



$$h^2 = ap^2 - ap_B^2$$

$$h^2 = \left(\frac{1+\sqrt{5}}{4}\right)^2 \cdot a^2 - \left(\frac{\sqrt{3}}{6}\right)^2 \cdot a^2$$

# VOLUM DE L'ICOSAEDRE

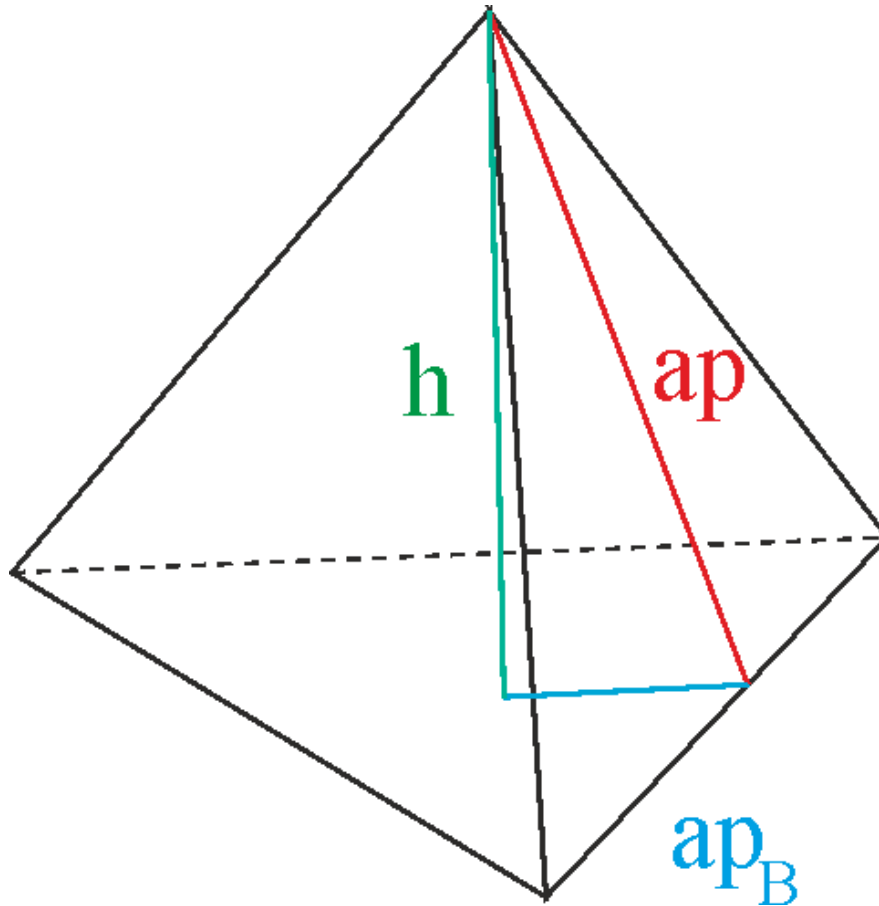


$$h^2 = ap^2 - ap_B^2$$

$$h^2 = \left( \frac{1 + \sqrt{5}}{4} \right)^2 \cdot a^2 - \left( \frac{\sqrt{3}}{6} \right)^2 \cdot a^2$$

$$h^2 = \left( \frac{3\sqrt{5} + 11}{24} \right) \cdot a^2$$

# VOLUM DE L'ICOSAEDRE



$$h^2 = ap^2 - ap_B^2$$

$$h^2 = \left(\frac{1+\sqrt{5}}{4}\right)^2 \cdot a^2 - \left(\frac{\sqrt{3}}{6}\right)^2 \cdot a^2$$

$$h^2 = \left(\frac{3\sqrt{5}+11}{24}\right) \cdot a^2$$

$$h = \sqrt{\left(\frac{3\sqrt{5}+11}{24}\right)} \cdot a$$

# VOLUM DE L'ICOSAEDRE

$$V(\text{Pira}) = \frac{A_B \cdot h}{3} = \frac{\frac{\sqrt{3}}{4} a^2 \sqrt{\left(\frac{3\sqrt{5} + 11}{24}\right)} \cdot a}{3} = \frac{\sqrt{3} \sqrt{\left(\frac{6\sqrt{5} + 22}{3}\right)} \cdot a^3}{12}$$

# VOLUM DE L'ICOSAEDRE

$$V(\text{Pira}) = \frac{A_B \cdot h}{3} = \frac{\frac{\sqrt{3}}{4} a^2 \sqrt{\left(\frac{3\sqrt{5} + 11}{24}\right)} \cdot a}{3} = \frac{\sqrt{3} \sqrt{\left(\frac{6\sqrt{5} + 22}{3}\right)} \cdot a^3}{12}$$

$$V(\text{Icos } a) = 20V(\text{Pira}) = 20 \cdot \frac{\sqrt{3} \sqrt{\left(\frac{6\sqrt{5} + 22}{3}\right)} \cdot a^3}{12}$$

# GRÀCIES PER LA SEVA ATENCIÓ

